

Multi-modal data analysis

- with an application to brain functional genomics

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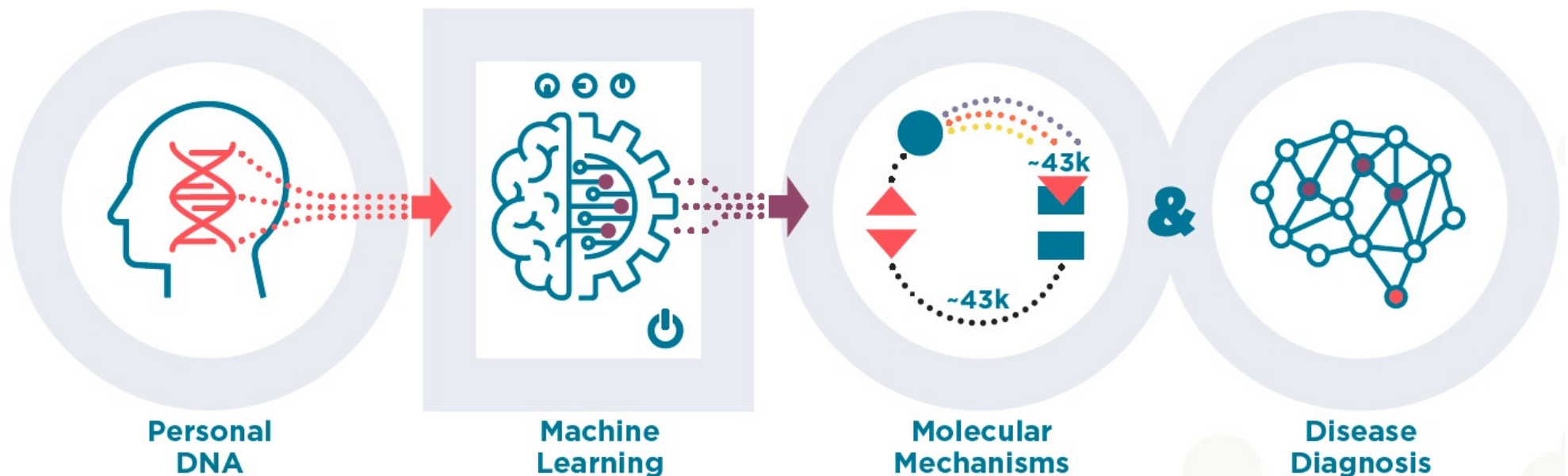
BMI/CS 776

Spring 2022

Machine learning to open “black box” from genotype to phenotype

- Goal
 - *Advance biological knowledge on genomics in brain diseases*
- Approach
 - *Machine learning, Bioinformatics, Computational Biology*

Decoding Genomic Information to Better Understand Molecular Mechanisms and Improve Disease Diagnosis



Outline

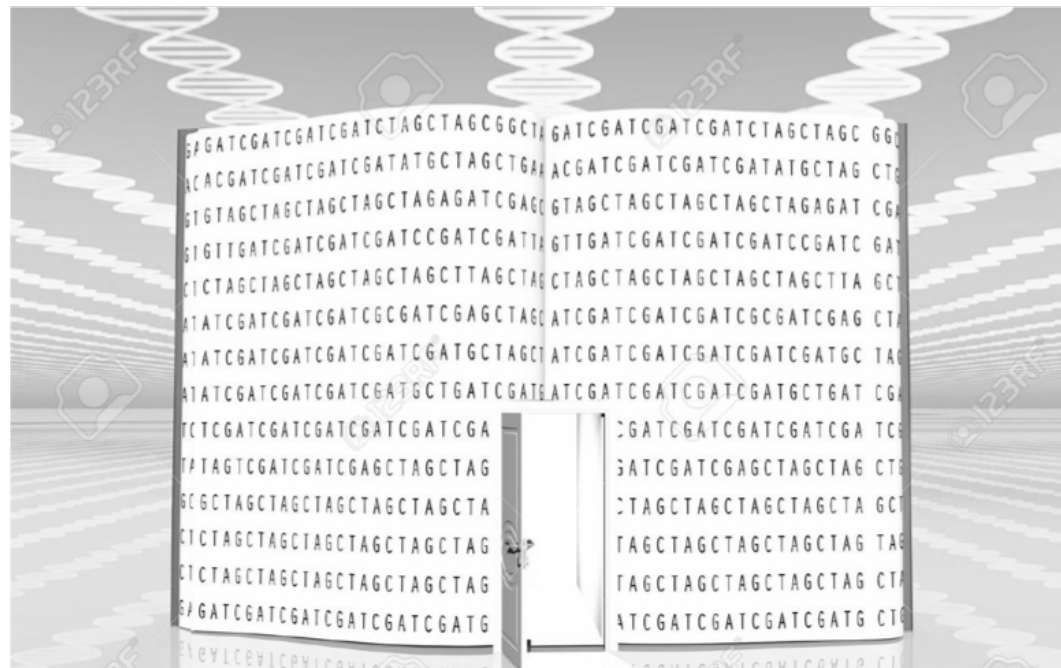
- Background
 - Functional genomics & multi-omics
 - Gene regulation
- Multi-view learning for multi-modal data
 - Multi-view Empirical Risk Minimization (MV-ERM)
 - Manifold alignment
- App 1: *single-cell multi-modal data integration*
 - Predicting neuronal electrophysiology from gene expression
- App 2: *deep manifold-regularized classification*
 - Predicting cortical layers of neurons from multi-modalities
- App 3: *biologically interpretable neural network modeling*
 - Disease prediction and functional prioritization

Your genome is your genetic code book

Book	Genome
Chapters	Chromosomes
Sentences	Genes
Words	Elements
Letters	Bases

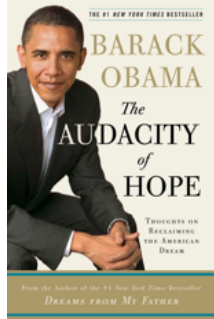
Human

- 46 chromosomes
- ~ 20,000 – 25,000 genes
- ~ Millions elements
- 4 unique bases (A, T, C, G), ~3 billion in total



<https://goo.gl/images/vMaz4T>

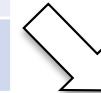
How to read your genetic code book?



Chapter One Republicans and Democrats



Book	Genome
Chapters	Chromosomes
Sentences	Genes
Words	Elements
Letters	Bases

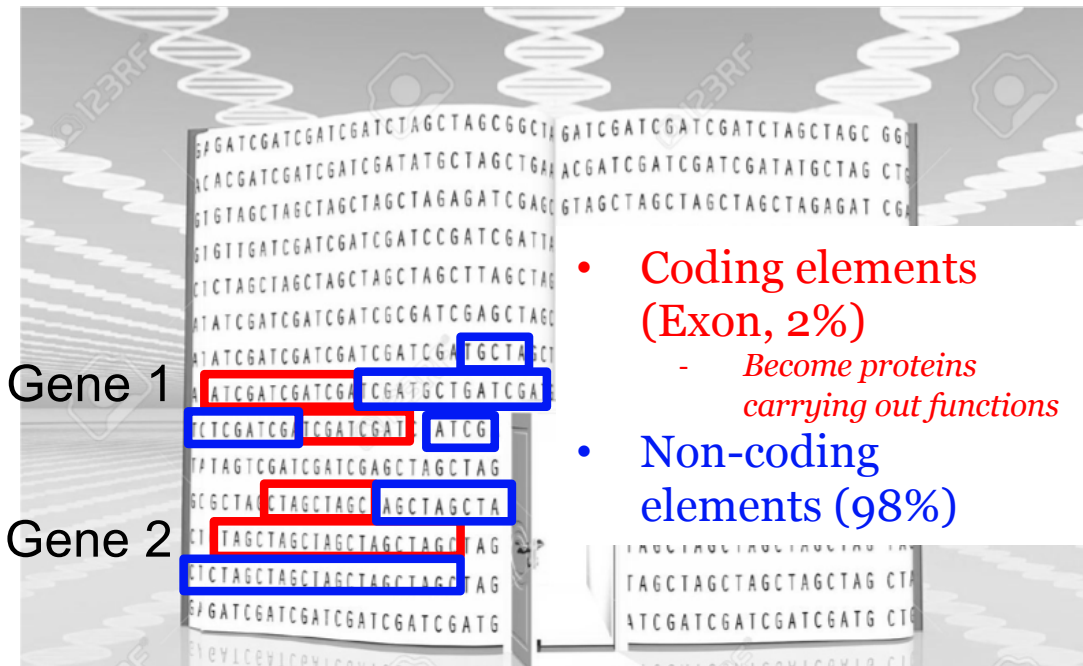


“On most days, I enter the Capitol through the basement. A small subway train carries me from the Hart Building, where ...”

- Key words
- Non-key words

Overhead, the ceiling forms a creamy white oval, with an American eagle etched in its center. Above the visitors' gallery, the busts of the nation's first twenty vice presidents sit in solemn repose.

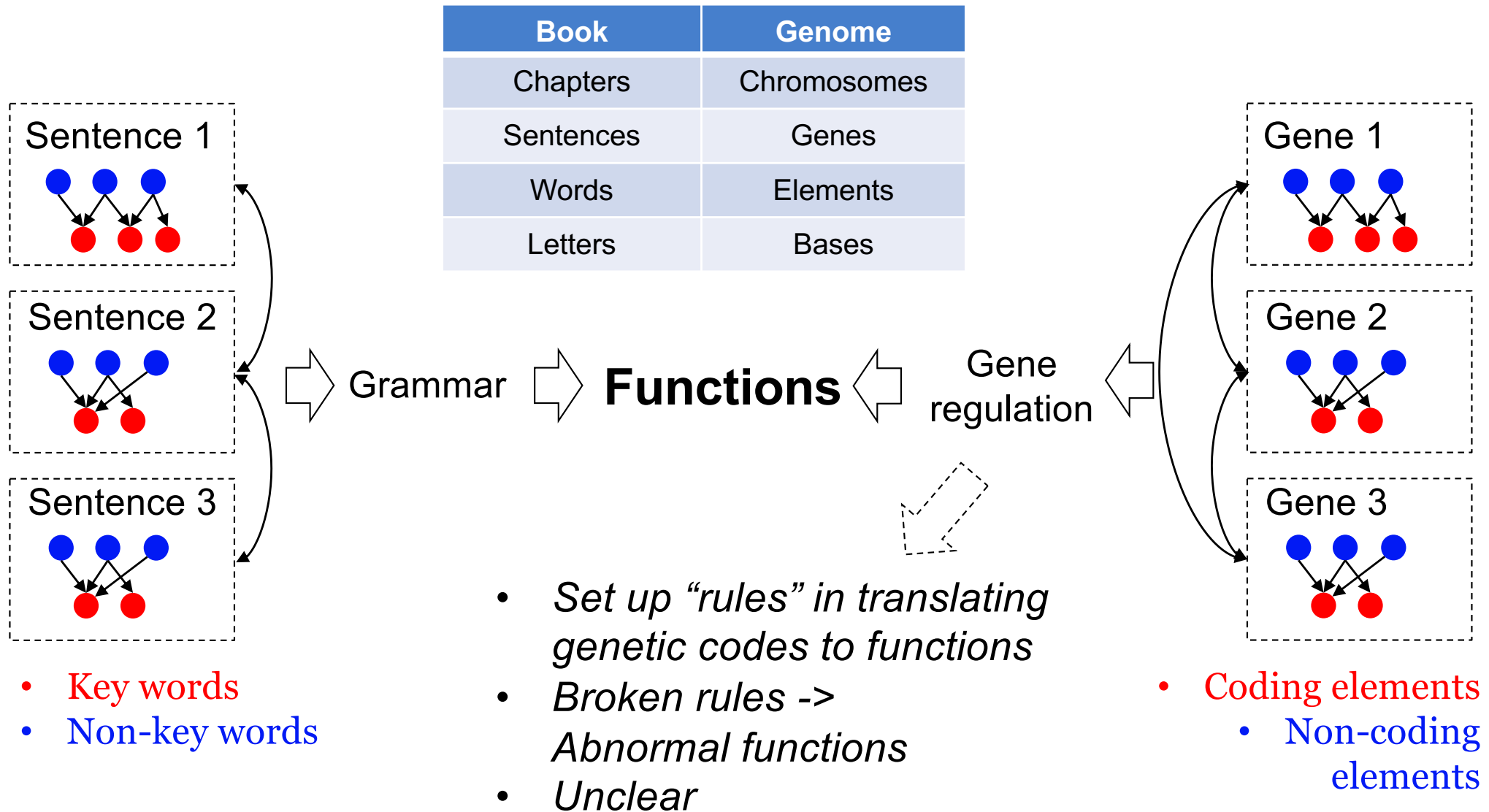
And in gentle steps, one hundred mahogany desks rise from the well of the Senate in four horseshoe-shaped rows. Some of these desks date back to 1819, and atop each desk is a tidy receptacle for inkwells and quills. Open the drawer of any desk, and you will find within the names of the senators who once used it—Taft and Long, Stennis and Kennedy—scratched or penned in the senator's own hand. Sometimes, standing there in



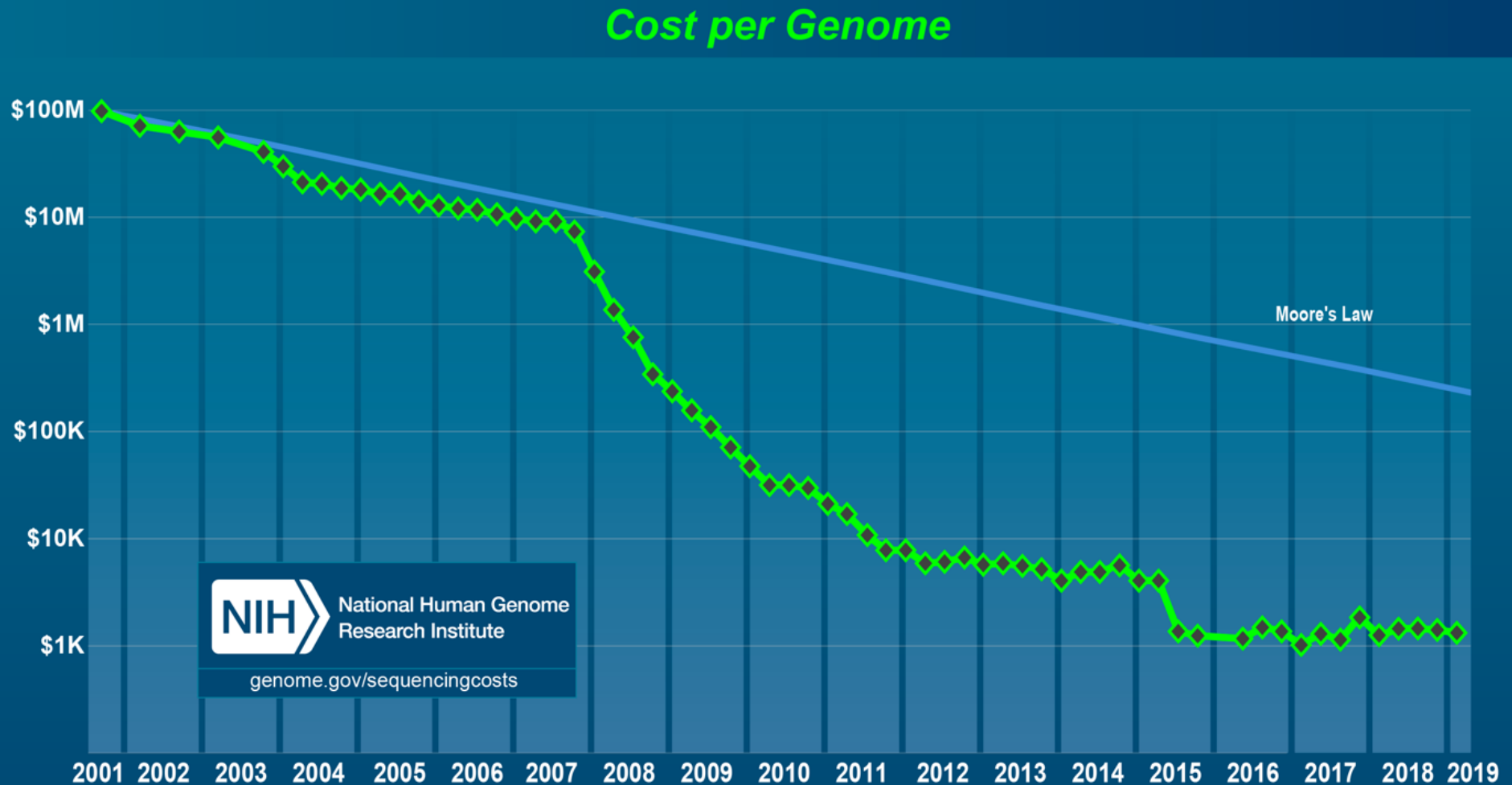
- Coding elements (Exon, 2%)
- Become proteins carrying out functions
- Non-coding elements (98%)

<https://goo.gl/images/vMaz4T>

Grammar for book is clear but not for genome



Low sequencing cost enables reading our whole genome



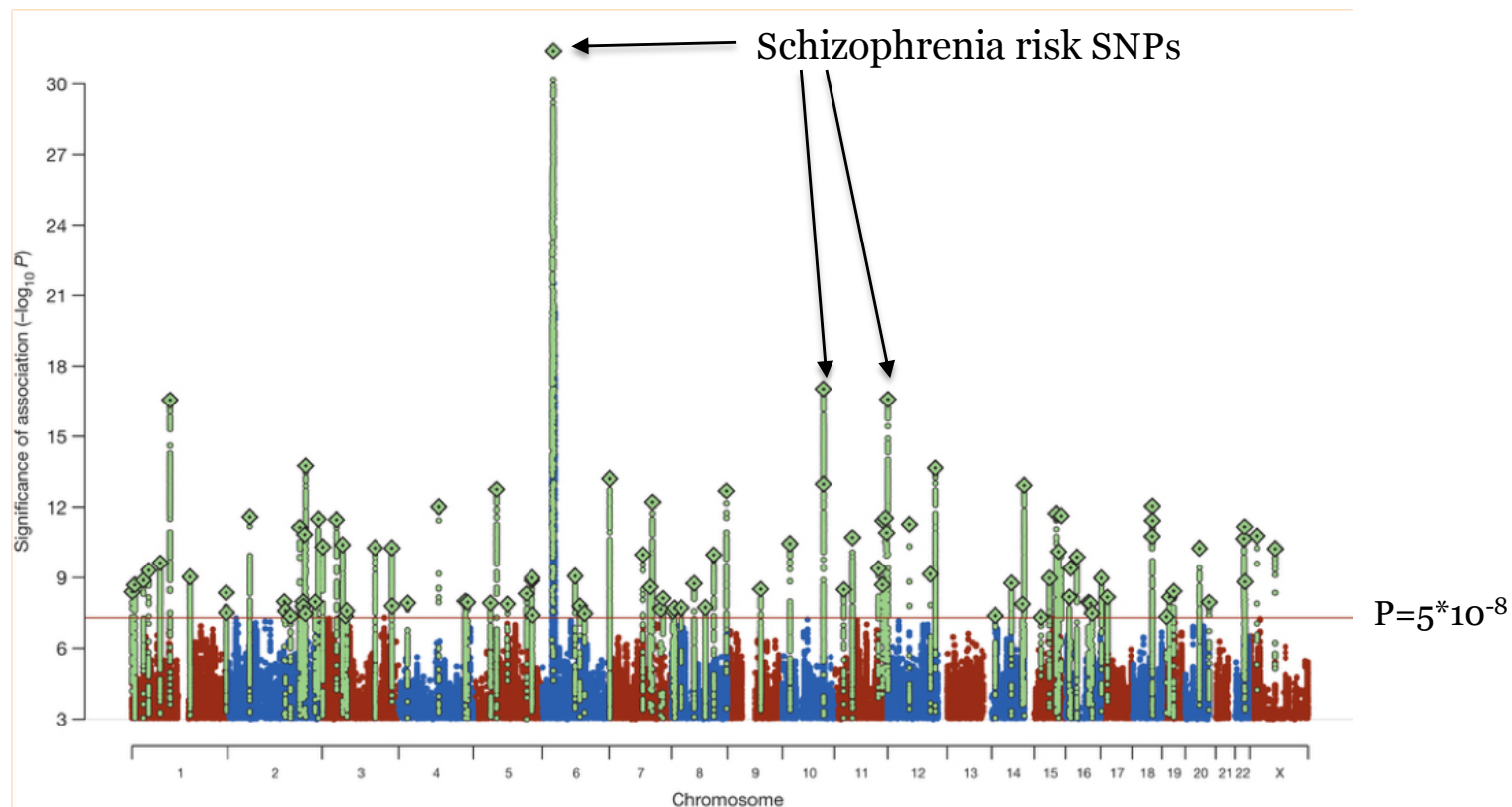
Differences across our genomes: DNA variants

Single Nucleotide Polymorphisms (SNPs) normally happen ~1% on individual human genome.



Genome-Wide Association Study (GWAS) identifies disease associated genetic variants

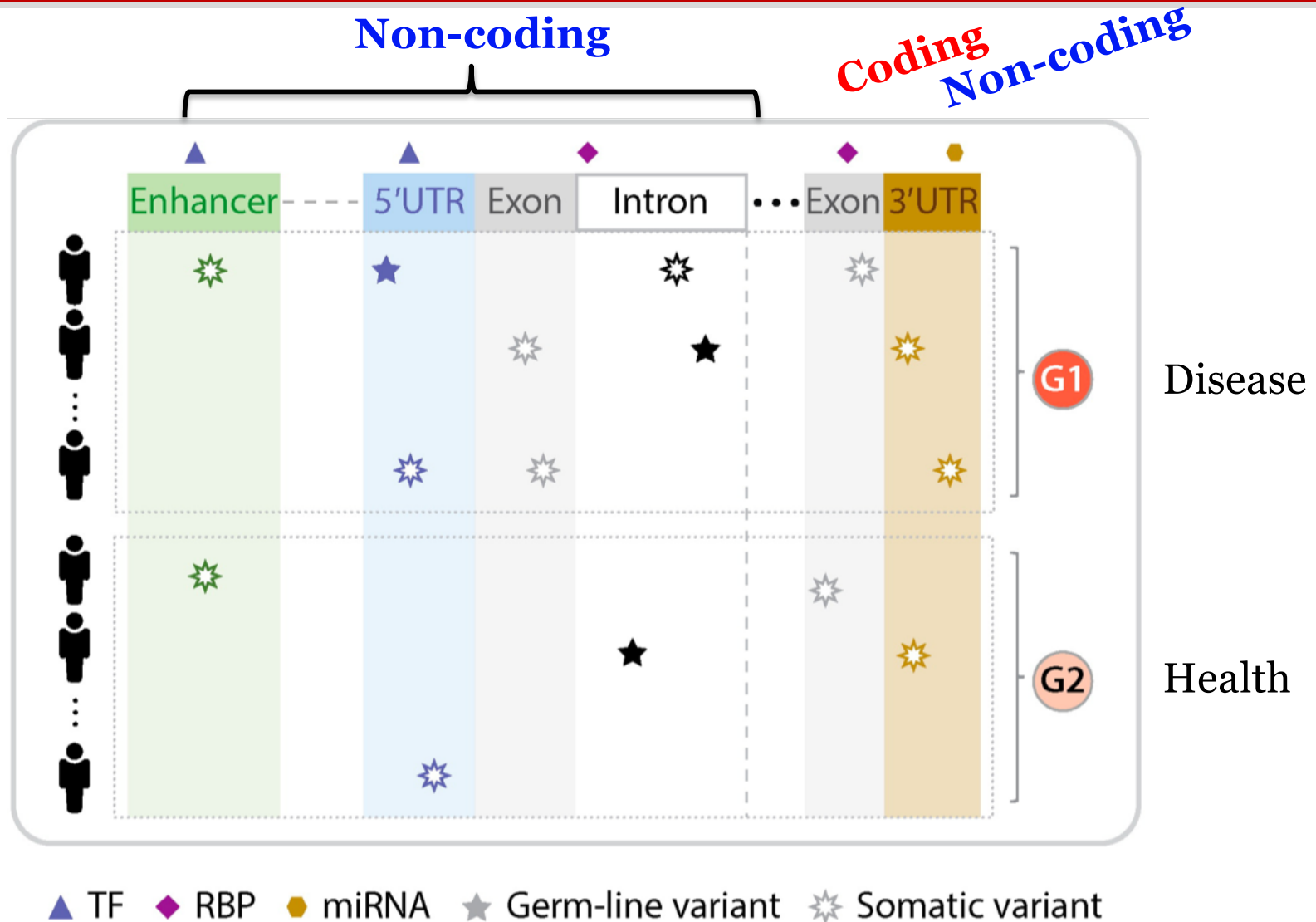
36,989 schizophrenia cases and 113,075 controls
in Psychiatric Genomics Consortium



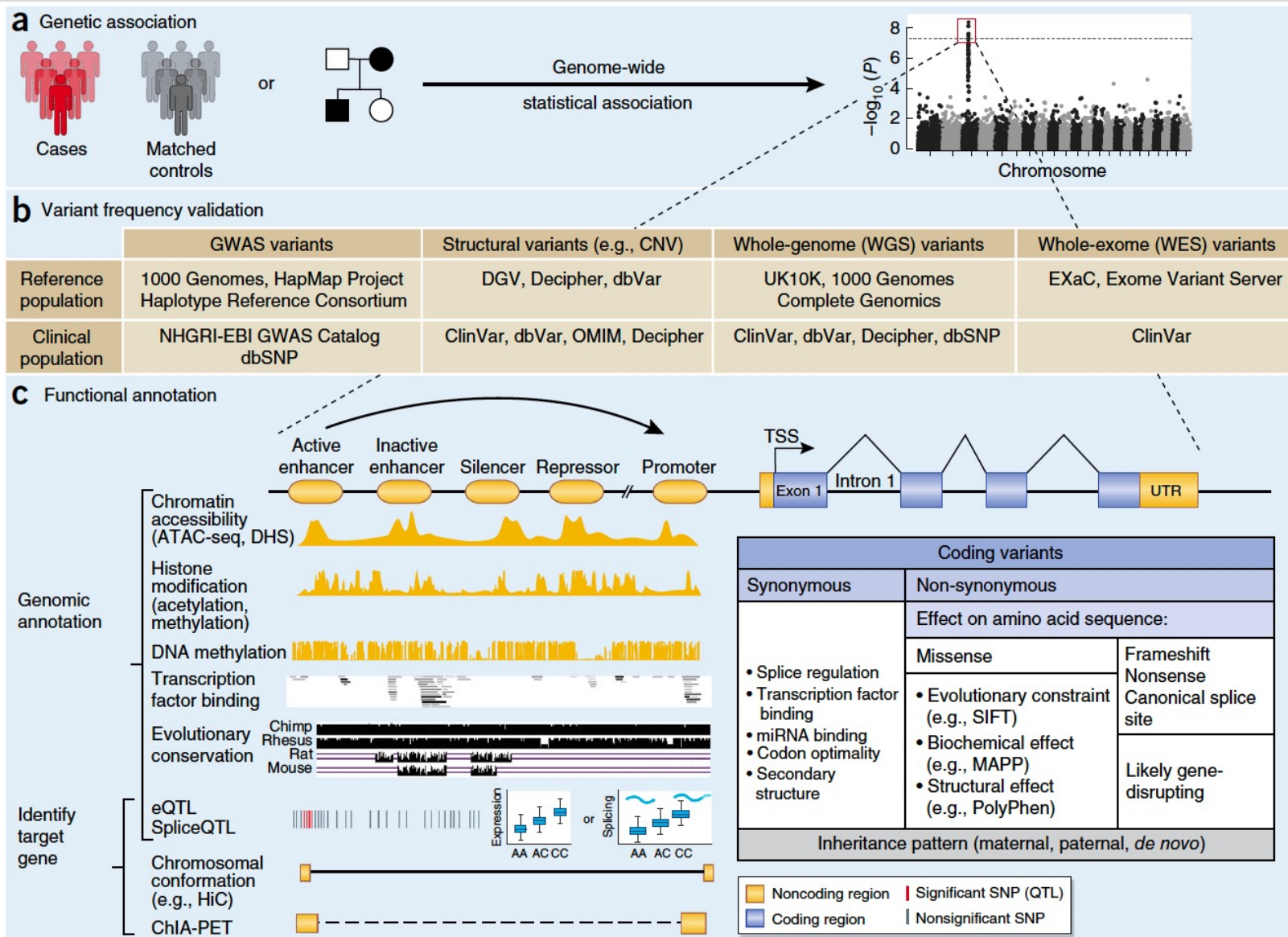
Schizophrenia Working Group of the Psychiatric Genomics Consortium, Nature (2014)

However, genotype-phenotype association can't tell mechanisms

How to link non-coding disease SNPs to genes?



Complex mechanisms from genotype to phenotype

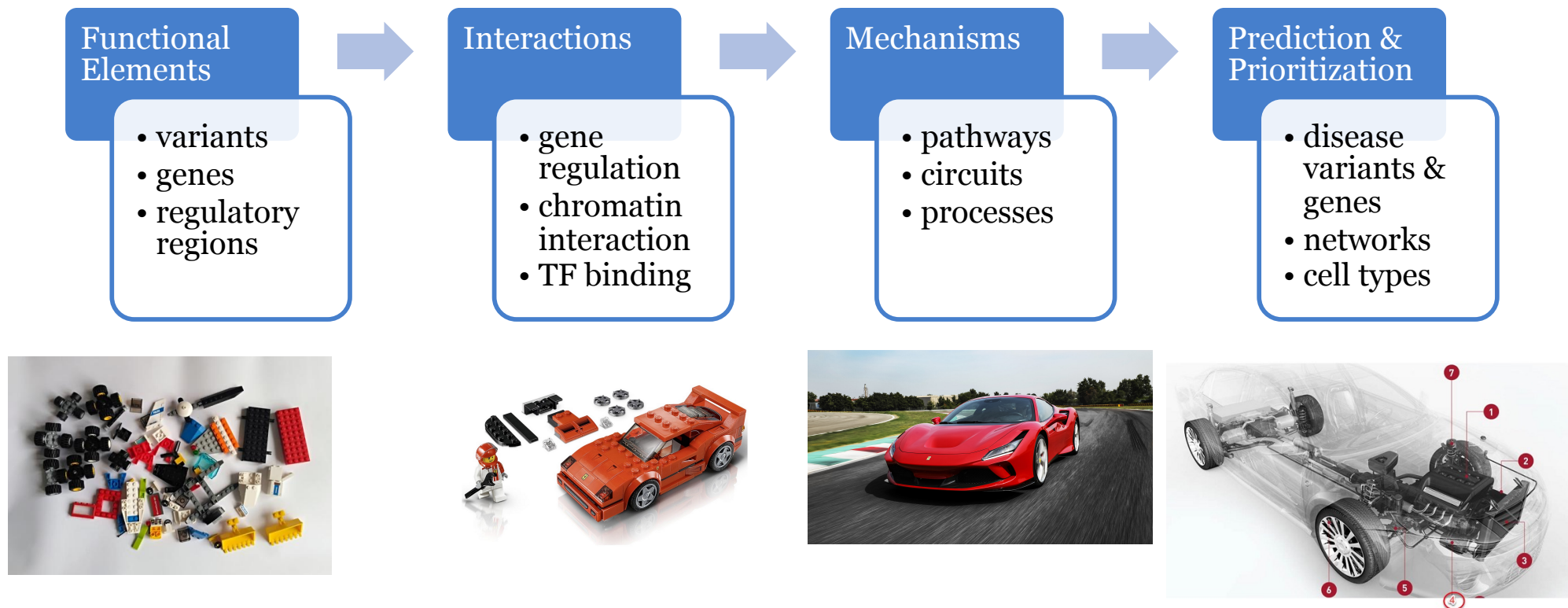


Disease-associated genomic variants

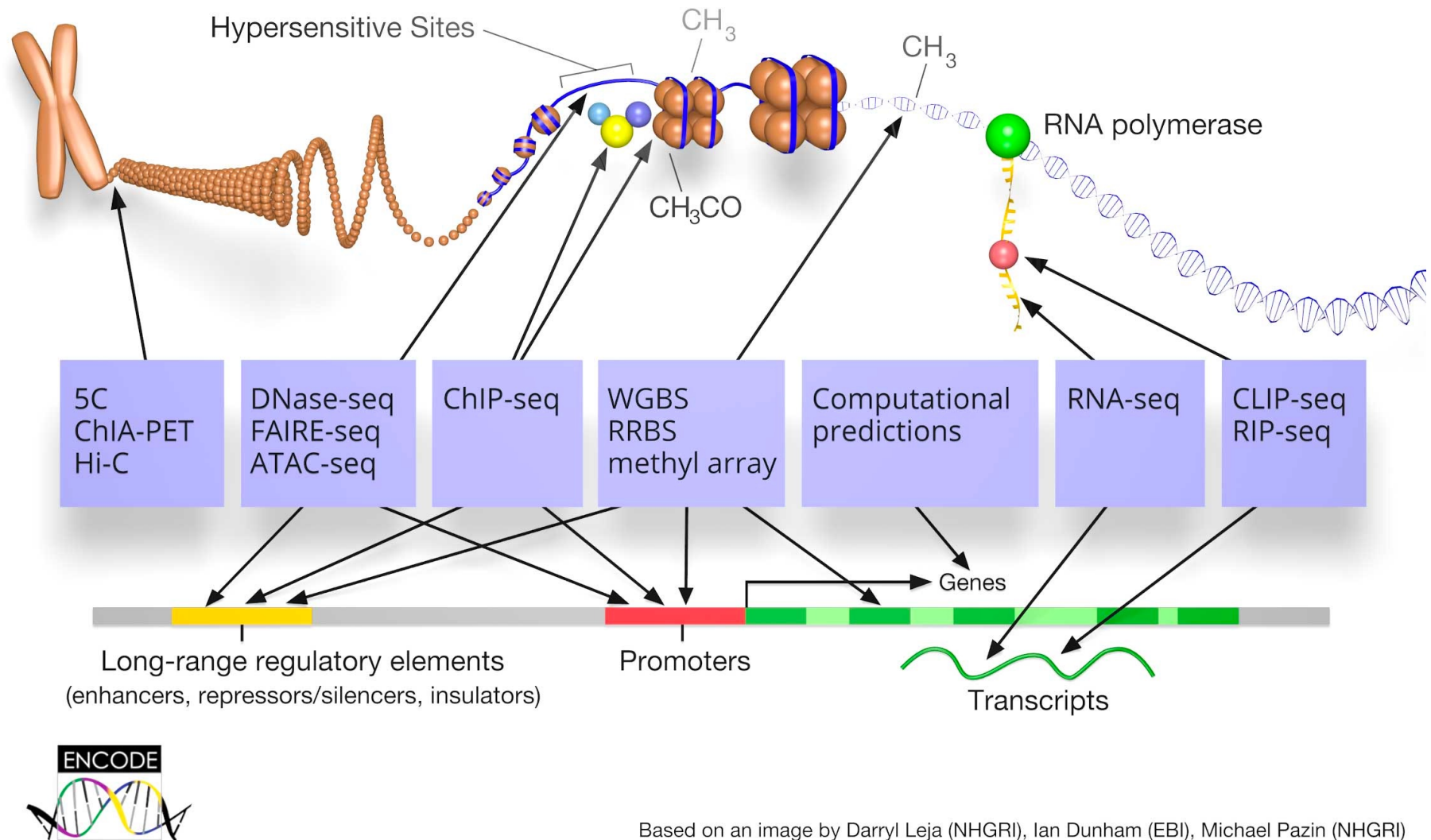


How do variants function?

Hierarchical understanding from genotype to phenotype



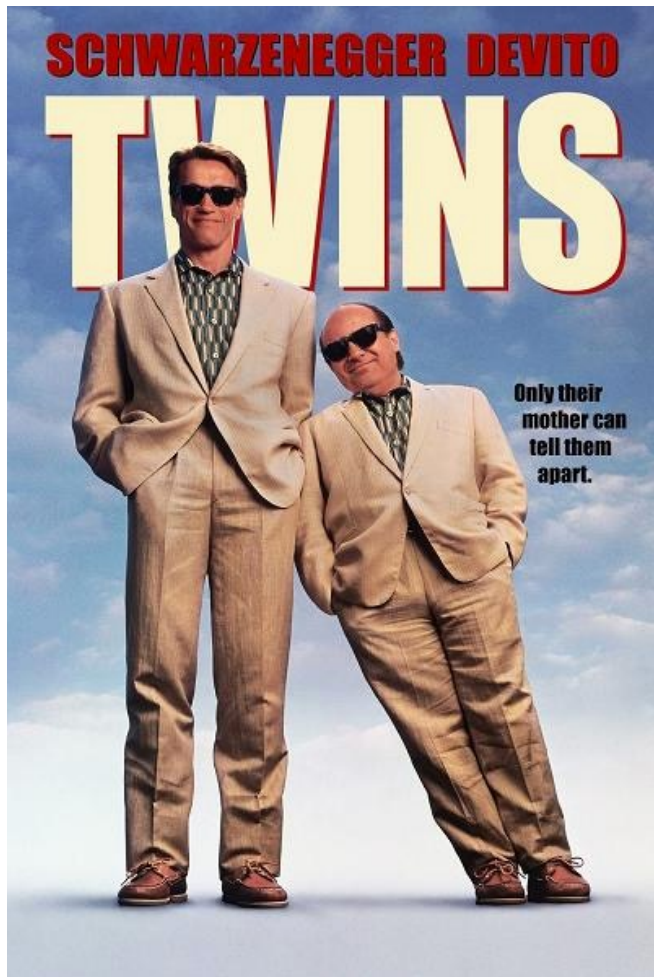
Multi-omics data for various functional elements



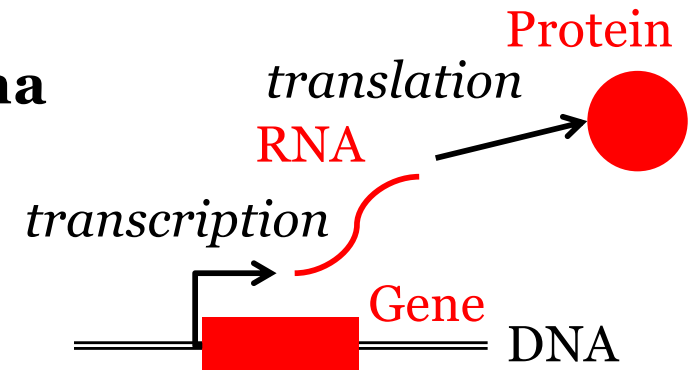
Based on an image by Darryl Leja (NHGRI), Ian Dunham (EBI), Michael Pazin (NHGRI)

Gene expression and regulation

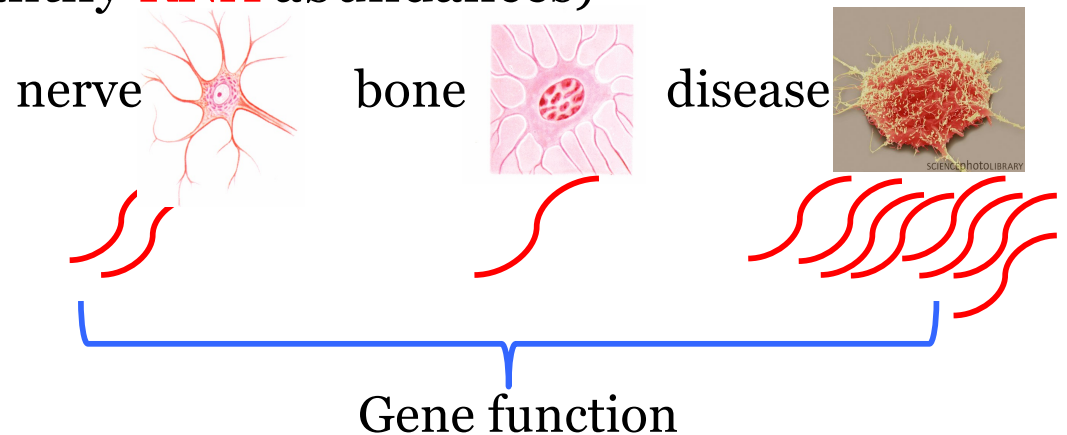
Identical DNA but
different gene expression



Central dogma



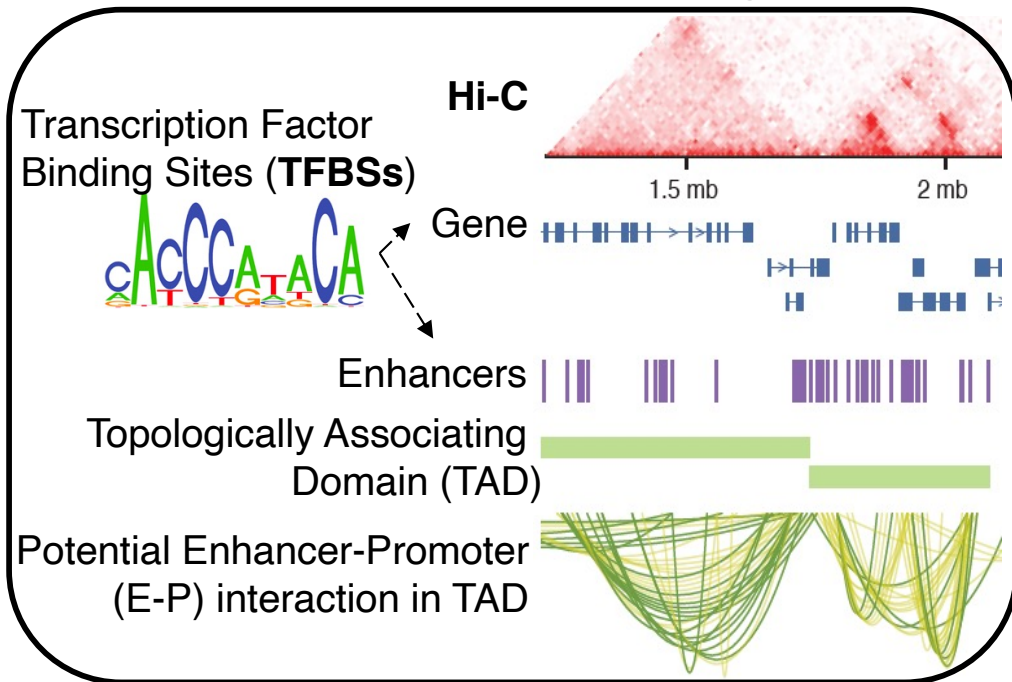
Gene expression levels (e.g., values to
quantify **RNA** abundances)



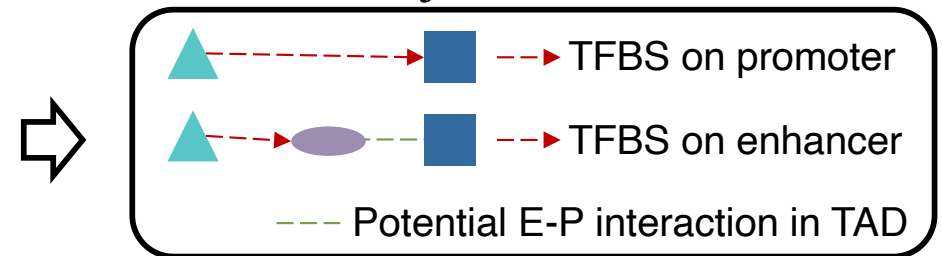
Gene regulation: mechanisms controlling
gene expression levels

Gene regulatory networks linking functional elements from multi-omics

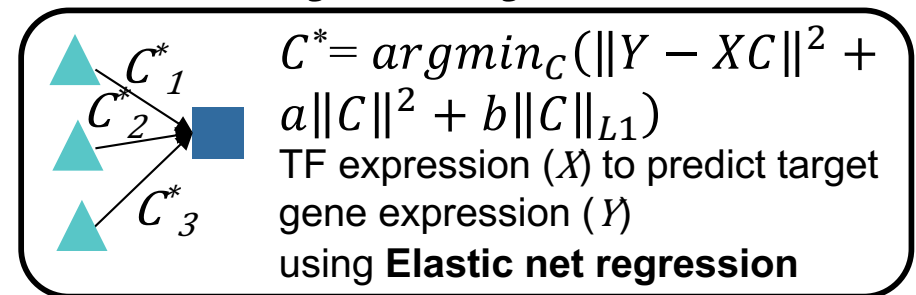
1. Multi-omics data integration



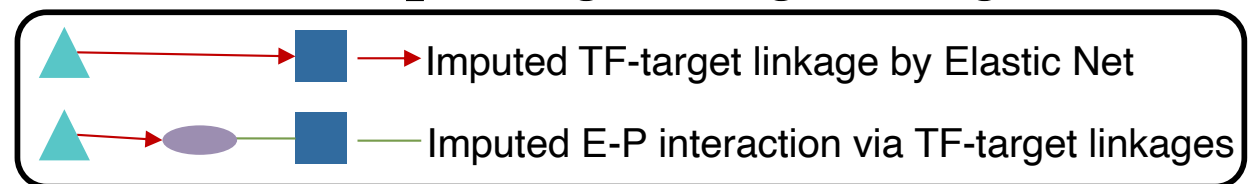
2. Reference network



3. Predicting TF-target via Elastic net

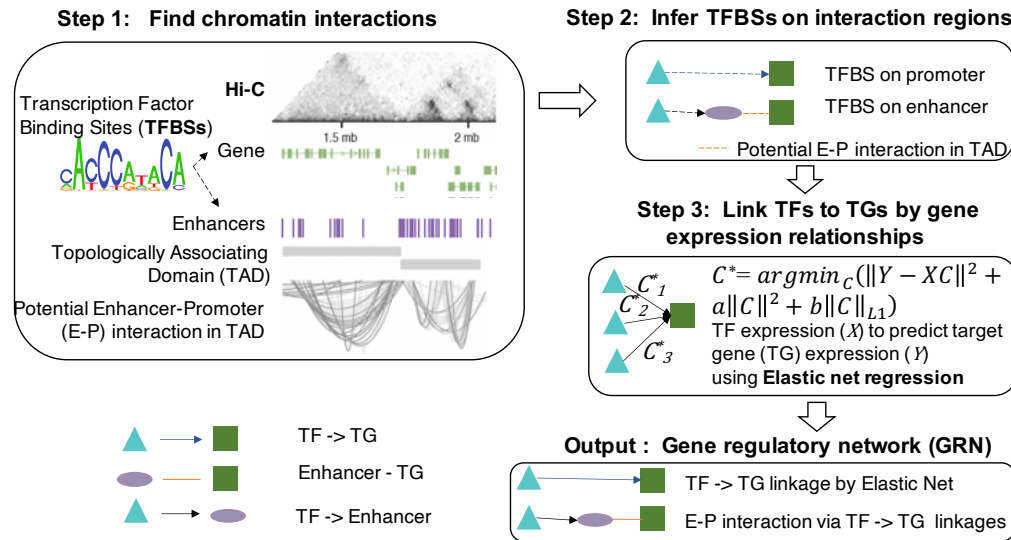


4. Imputed gene regulatory network

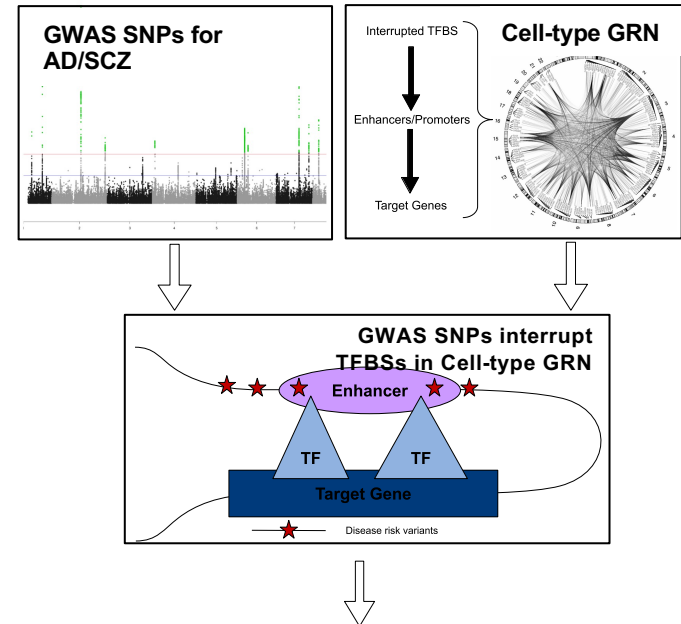


Gene regulatory networks linking GWAS SNPs to disease genes

1. Predicting cell-type gene regulatory networks (GRNs) via multi-omics

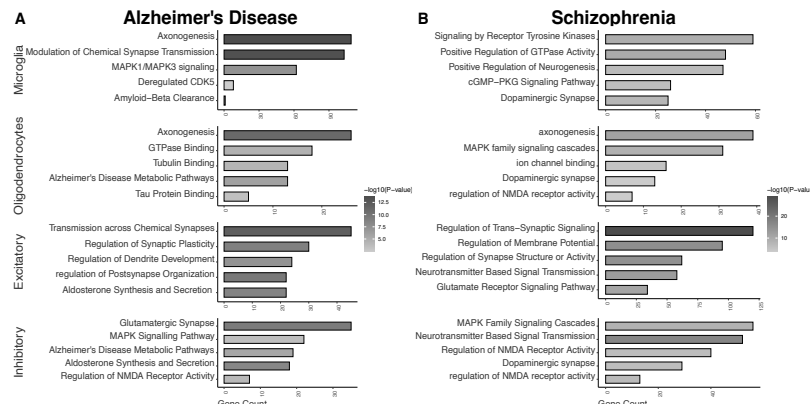
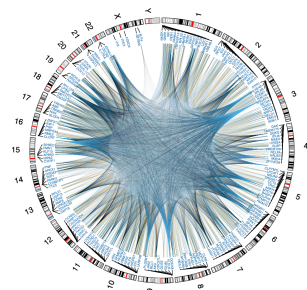


2. Identifying cell-type disease genes via GWAS and cell-type GRNs

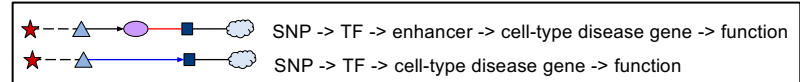


3. Microglia GRN, cell-type disease gene functions

Microglia
4523 TGs, 176 TFs, 12927 enhancers

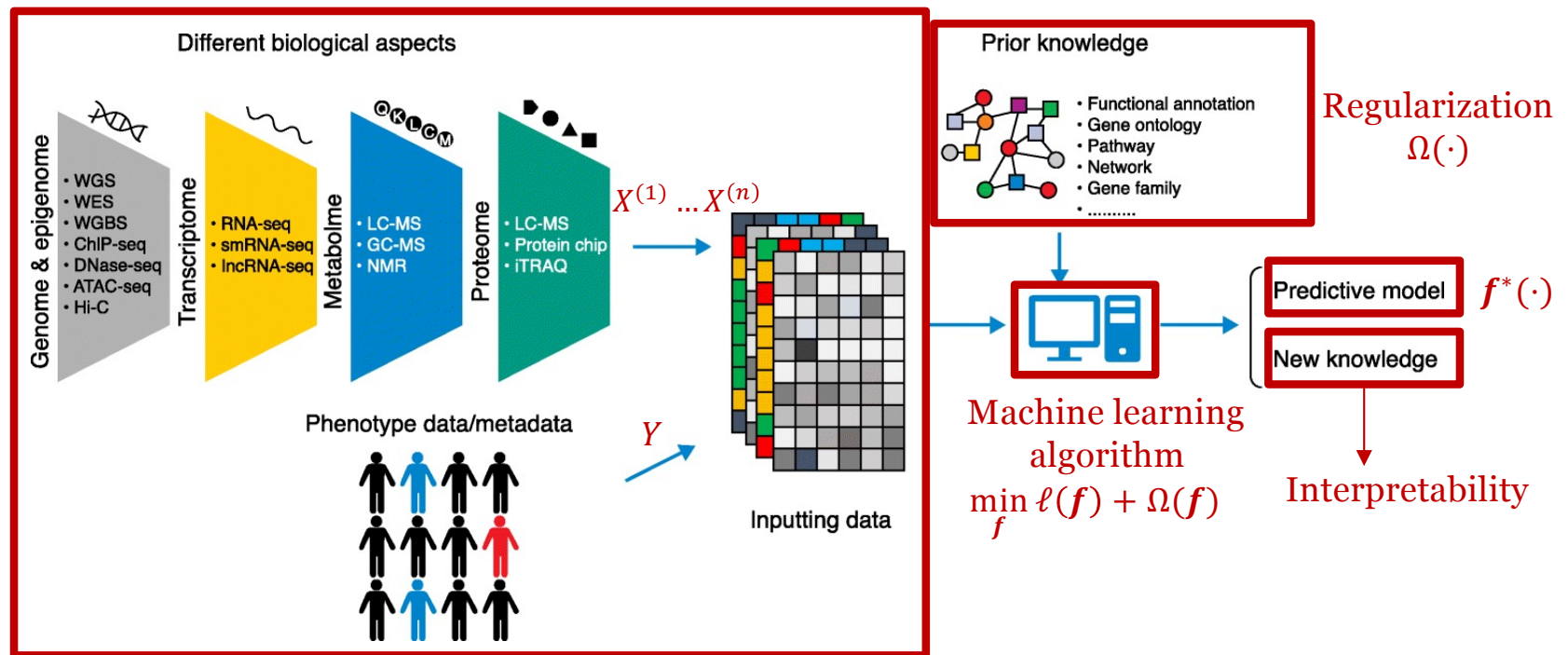


Output: Cell-type disease genes, networks and functions



Ting Jin (Ph.D. student, Biomedical Data Science)

Machine learning for multi-omics analysis, prediction and interpretation

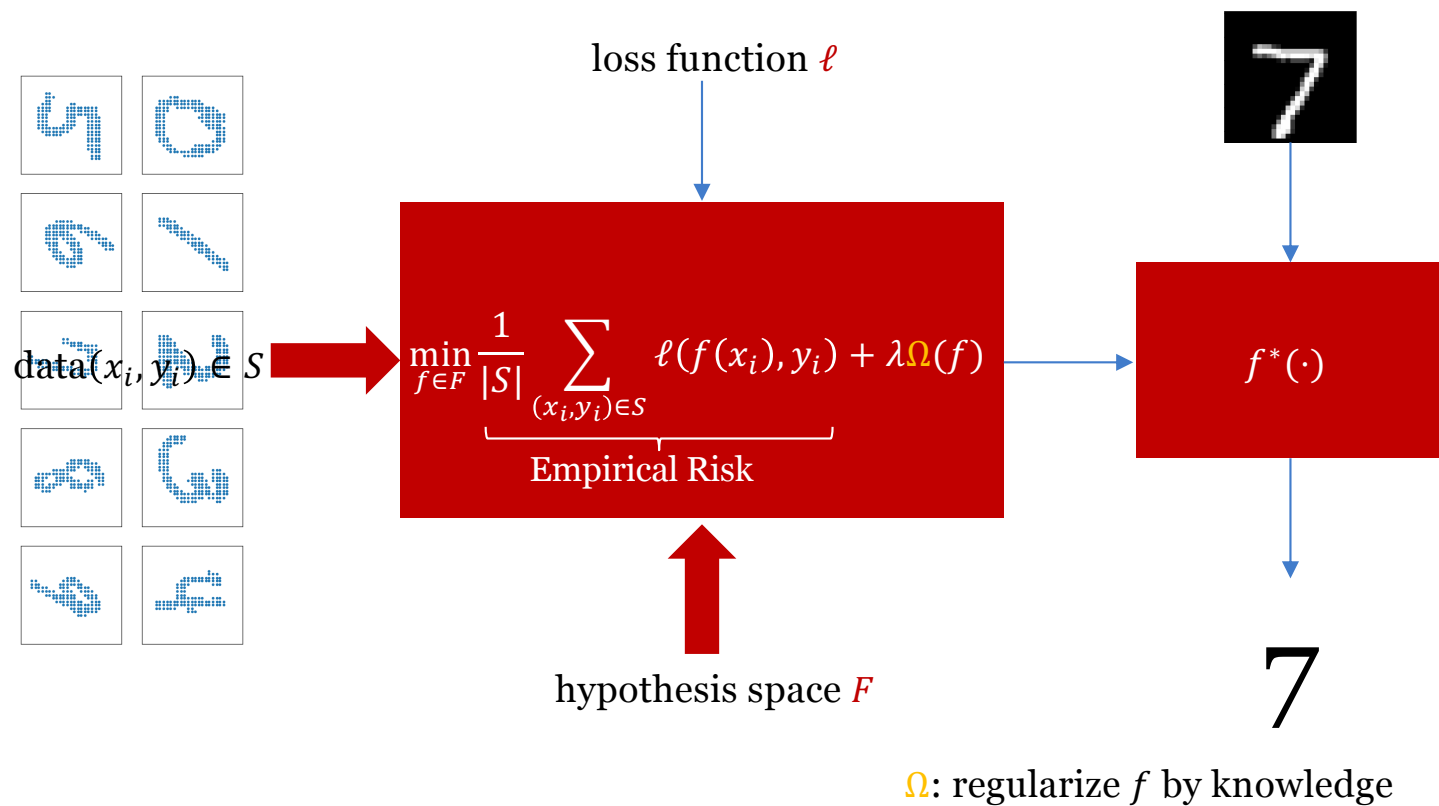


Xu. Genome Bio. 2019

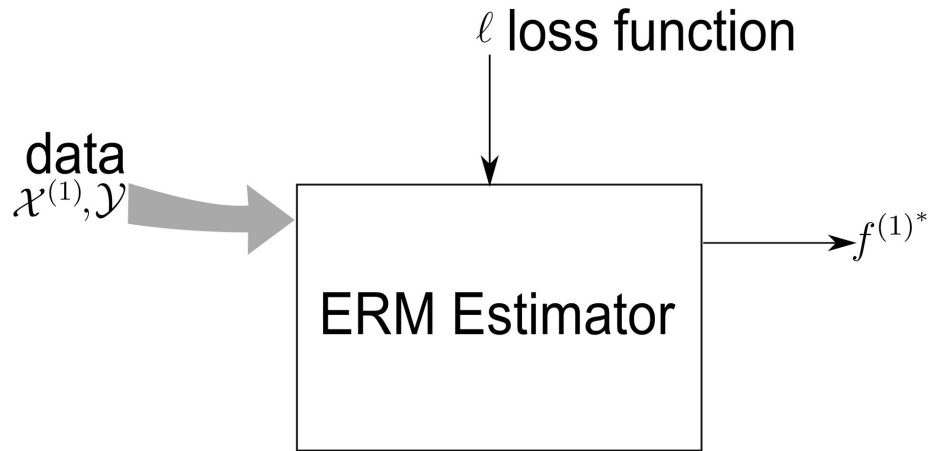
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Empirical Risk Minimization (ERM)



Empirical Risk Minimization (ERM) for single-omics (single-view learning)

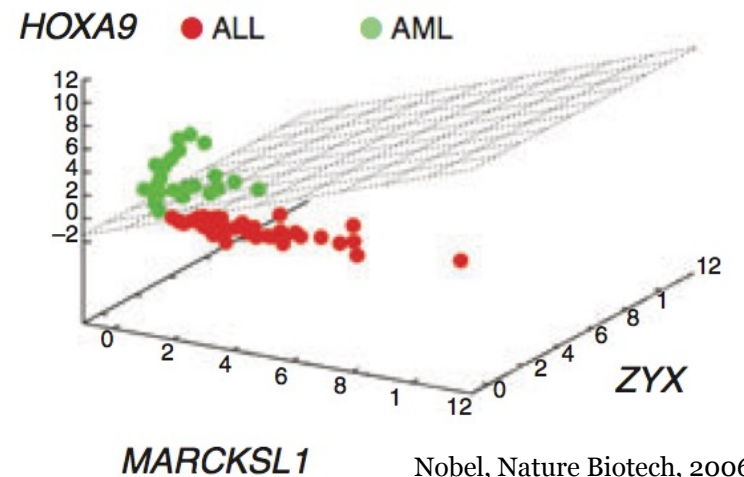


hypothesis space $\mathcal{F}^{(1)}$

$$R(f) = \frac{1}{|S|} \sum_{(x_i, y_i) \in S} \ell(f(x_i), y_i)$$

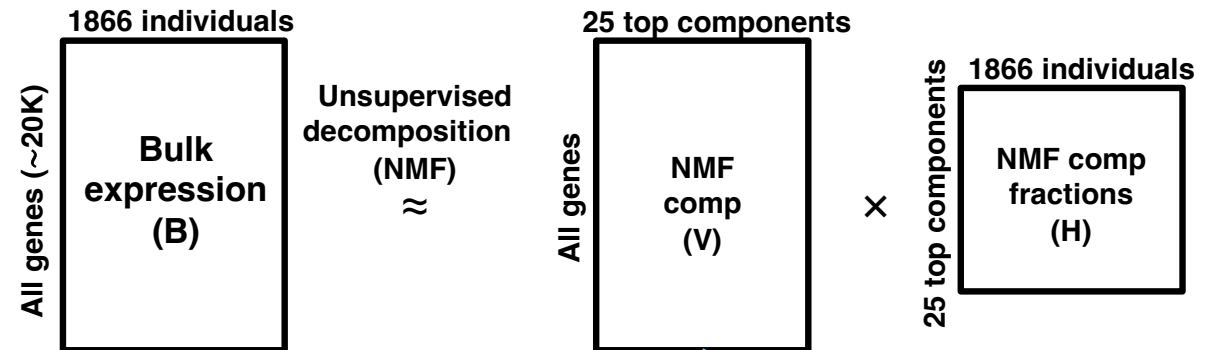
$$f^* \in \operatorname{argmin}_f \{R(f) + \lambda \Omega(f)\}$$

- e.g., Leukemia patient classification
 - y_i : Acute lymphoblastic leukemia (ALL) vs. Acute myeloid leukemia (AML)
 - x_i : gene expression
 - f : SVM



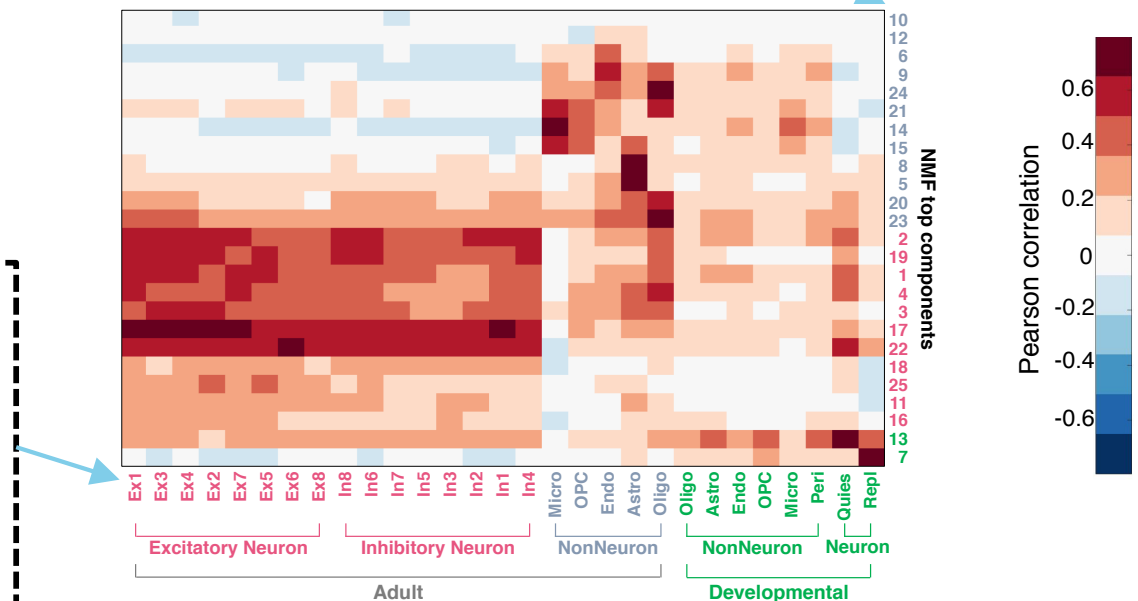
Example: single-view unsupervised learning

Non-negative matrix factorization (NMF)

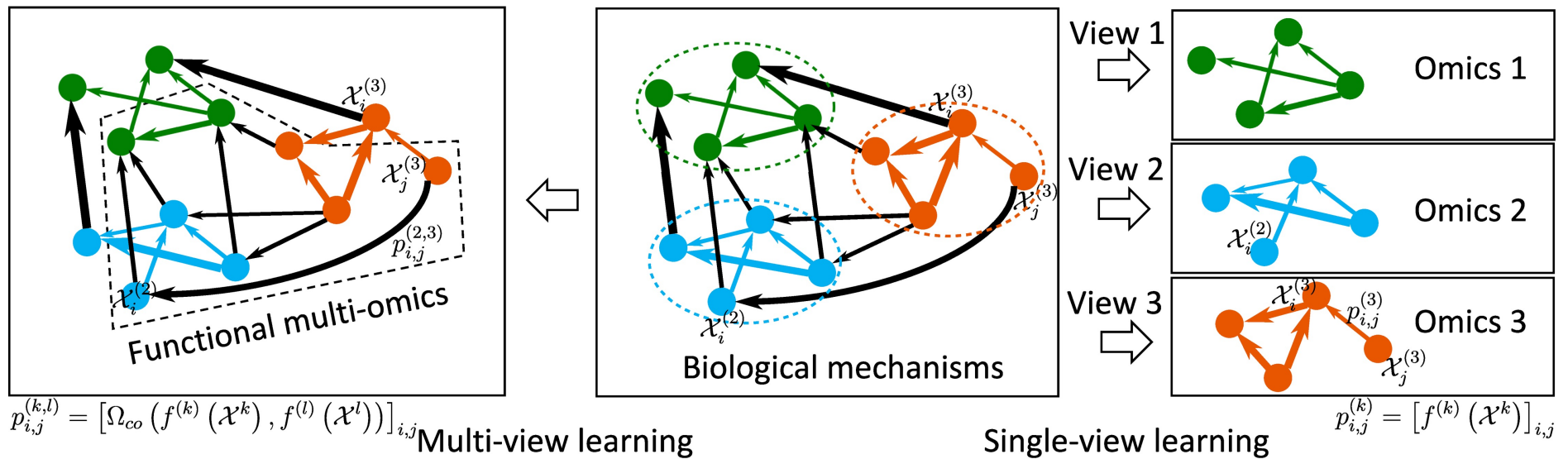


Single cell signatures

- ~14,000 cells (Lake et al., Science, 2016&2018)
- ~400 cells (Darmanis et al., PNAS, 2015)
- ~18,000 cells (PsychENCODE)



Multi-view learning for multi-omics integration



- For example, gene regulation involves
 1. Genomics; e.g., SNPs
 2. Transcriptomics; e.g., genes
 3. Proteomics; e.g., transcription factors (TFs)



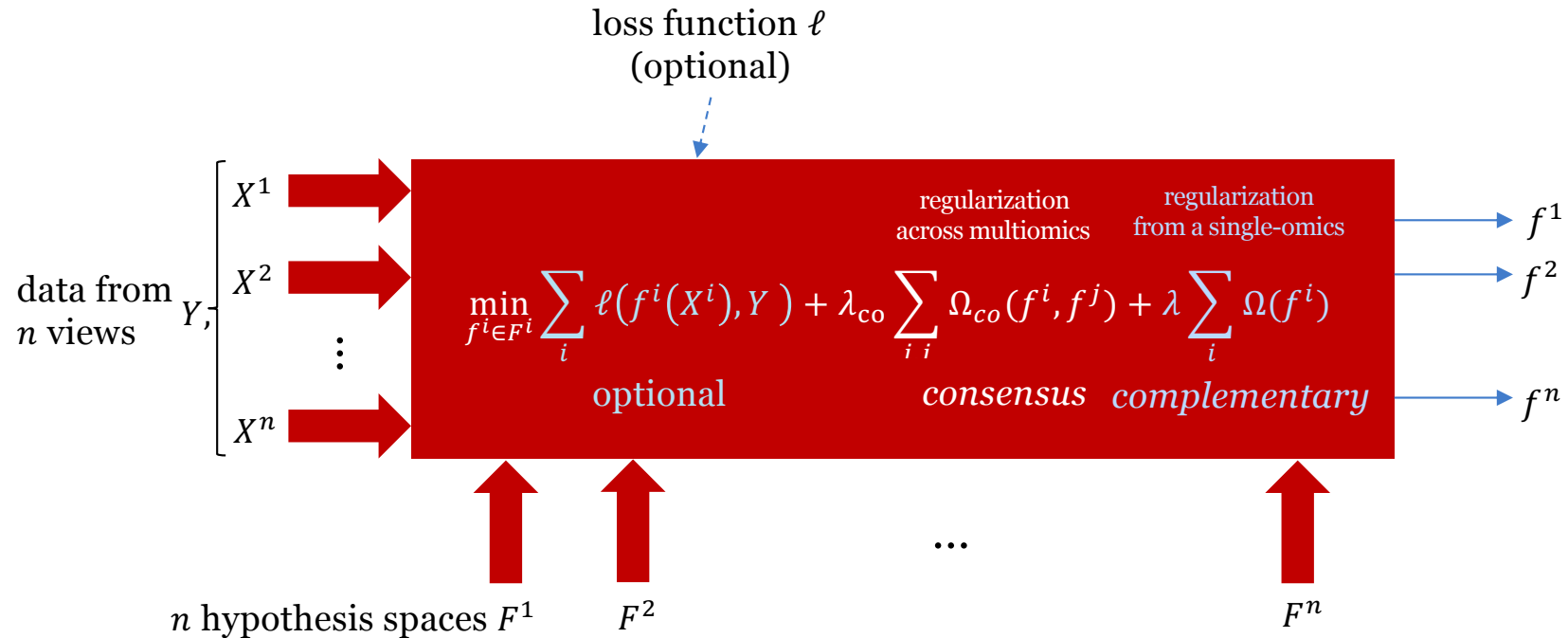
Cross-omics interactions

$\Omega_{co}(f^{(1)}, f^{(3)})$: SNPs break TF binding sites

$\Omega_{co}(f^{(2)}, f^{(3)})$: TFs control gene expression

$\Omega_{co}(f^{(1)}, f^{(2)})$: SNPs associate with gene expression (e.g., eQTLs)

Multiview Empirical Risk Minimization (MV-ERM)



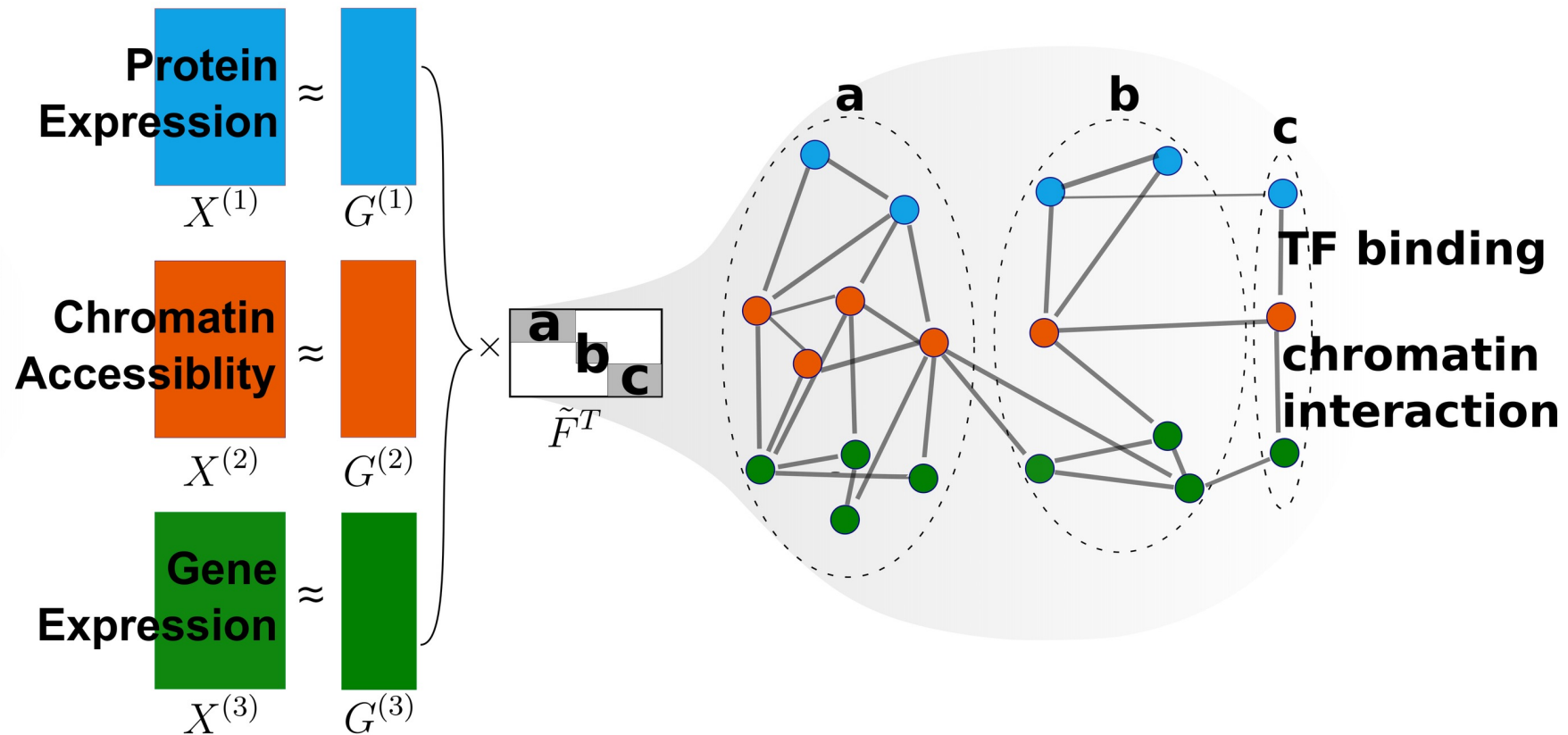
Complementary regularization

- Unique information from each view

Consensus regularization

- Relationship information across views

Factorization-based MV-ERM

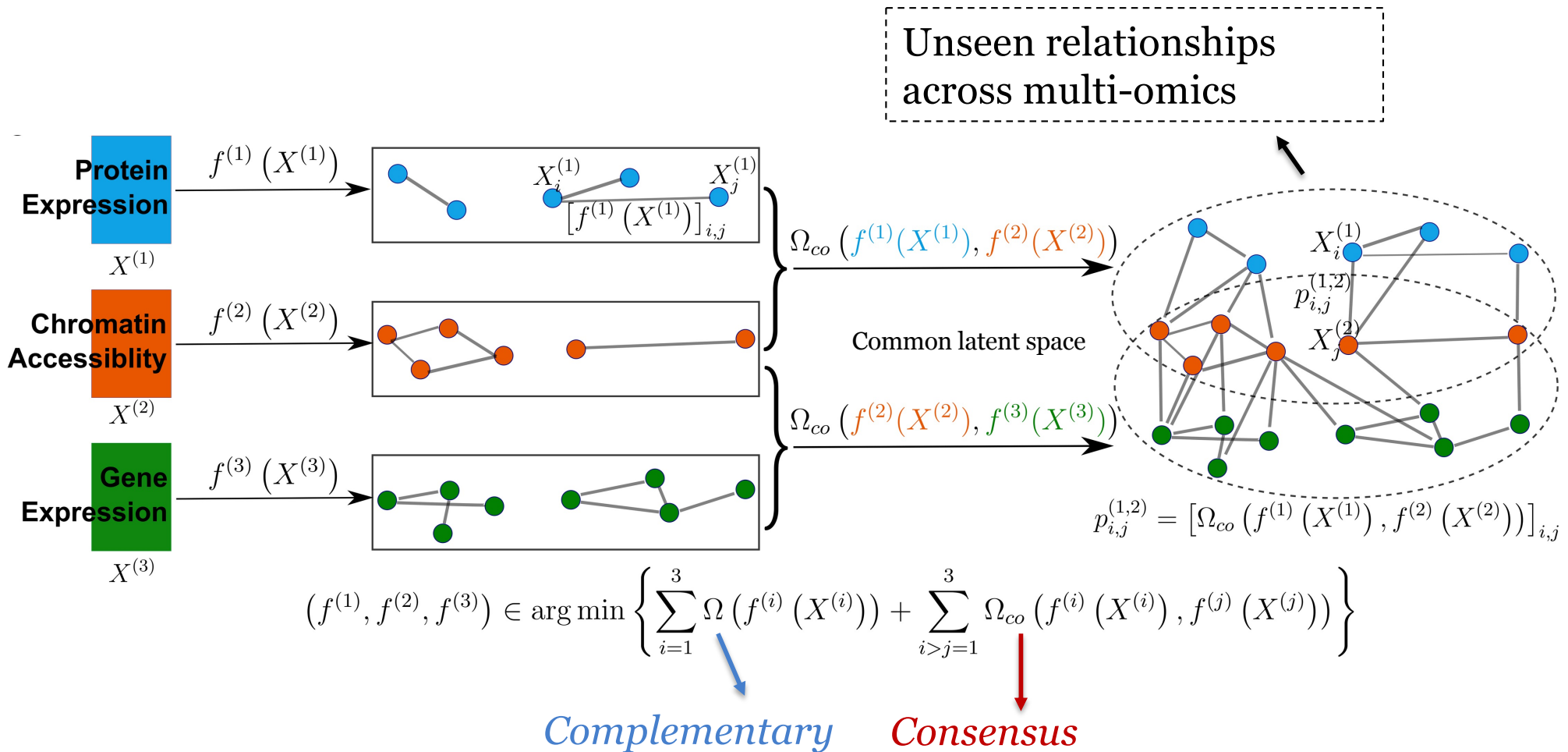


$$\left(G^{(1)*}, G^{(2)*}, G^{(3)*}, \tilde{F}^* \right) \in \arg \min_{G^{(i)}, F^{(i)}, \tilde{F} \geq 0} \sum_{i=1}^3 \left\{ \left\| X^{(i)} - G^{(i)} F^{(i)T} \right\|_F^2 + \lambda \left\| F^{(i)} - \tilde{F} \right\|_F^2 \right\}$$

Complementary $G^{(i)}$
Consensus $\tilde{F}$

- e.g., solved by Multi-view NMF (Liu et al., SIAM ICDM, 2013)

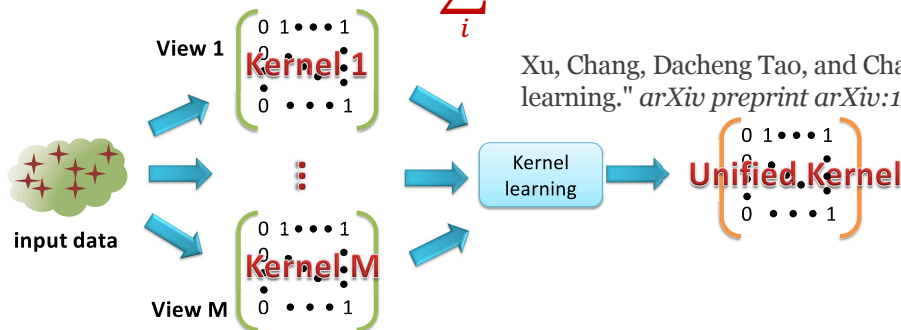
Alignment-based MV-ERM



Alignment-based multi-view learning methods

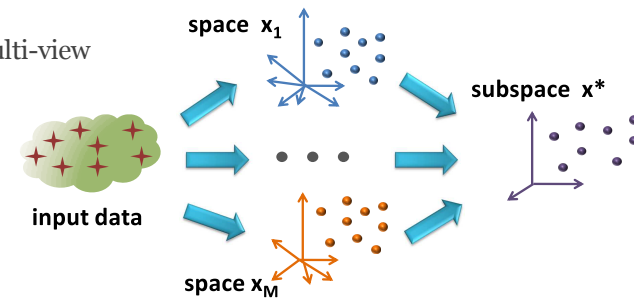
Multiple kernel learning

- learn a combination of predefined kernels
- not data dependent
- expensive
- Only support complementary principle
- **non-linear** $\sum_i \beta_i K^{(i)}$



Subspace learning

- obtains a common latent subspace
- **data dependent** $\rightarrow$ more general
- **non-expensive**
- CCA (Canonical Correlation Analysis)
 - Only support consensus principle
 - linear $\max_{f,g} \text{corr}(f(X), g(Y))$

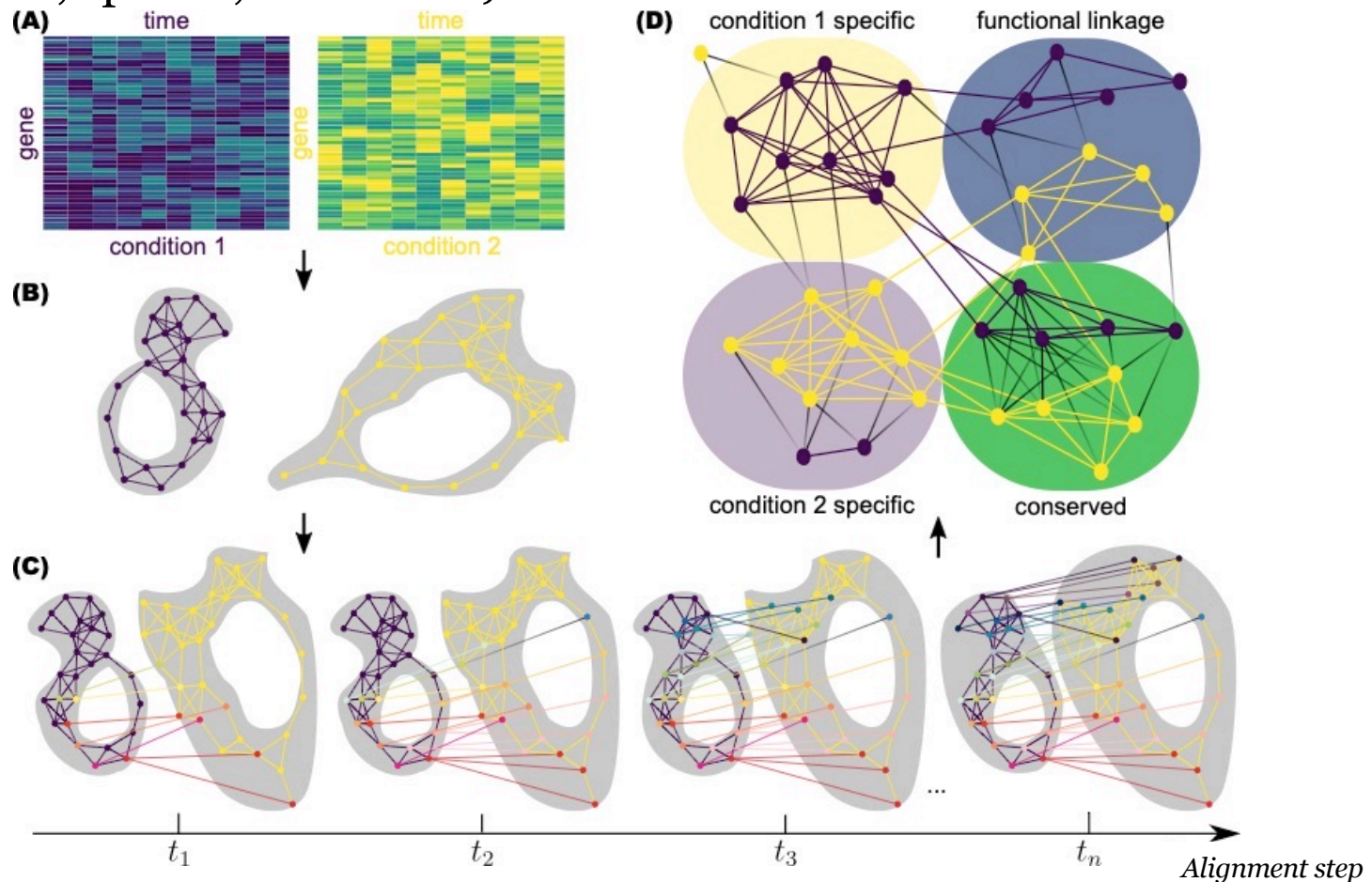


Can we support both principles?

ManiNetCluster: manifold alignment to reveal the functional links between gene networks

Multi-view datasets (e.g., diseases, species, conditions)

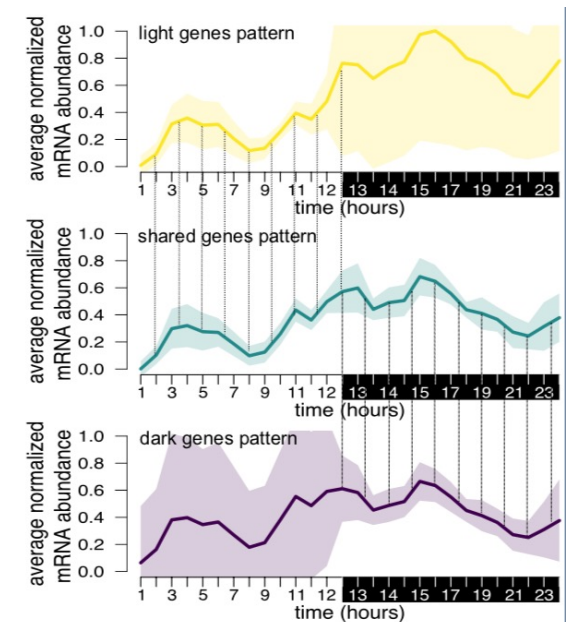
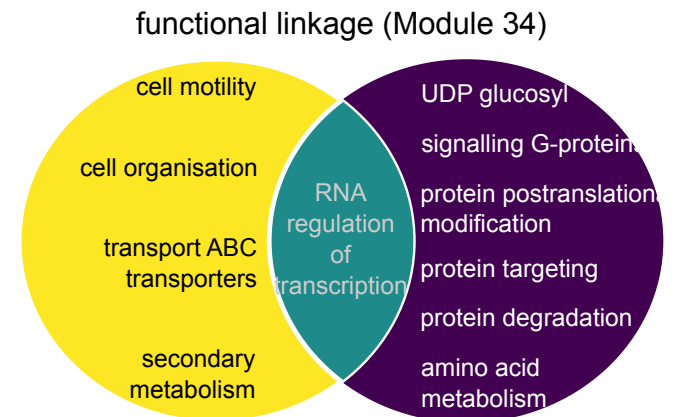
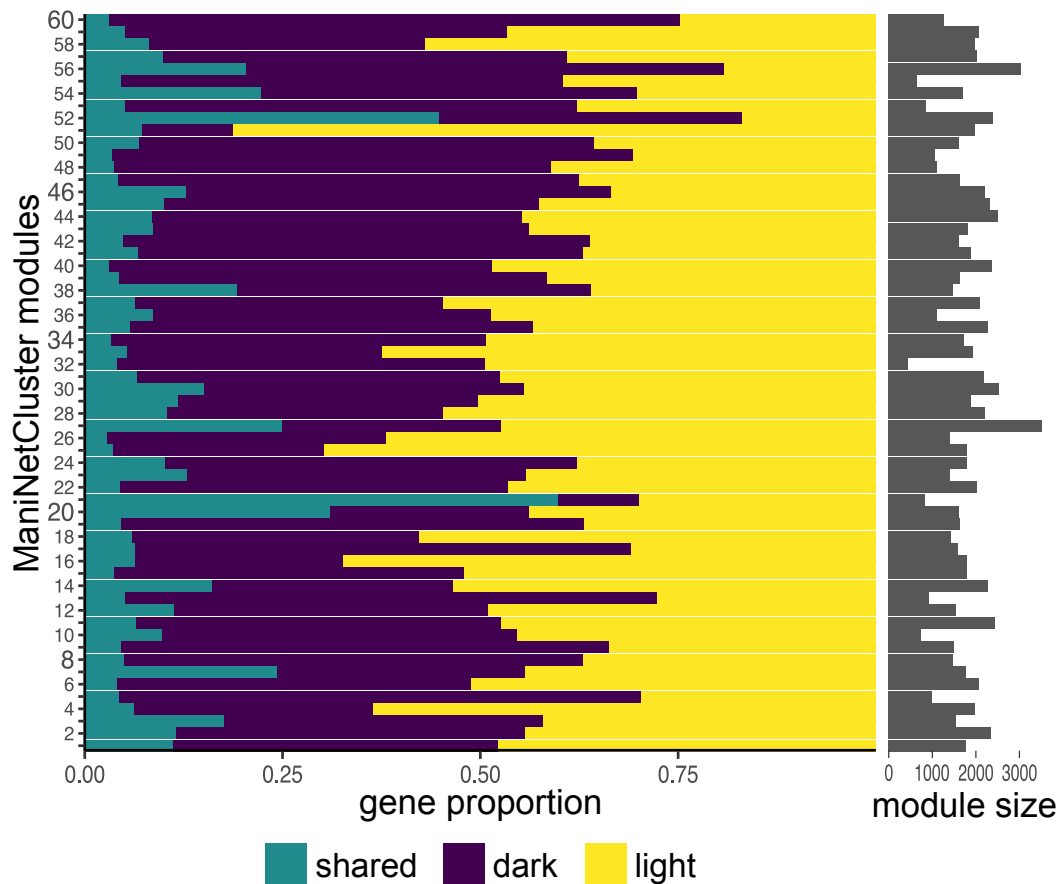
Functional linkages across views



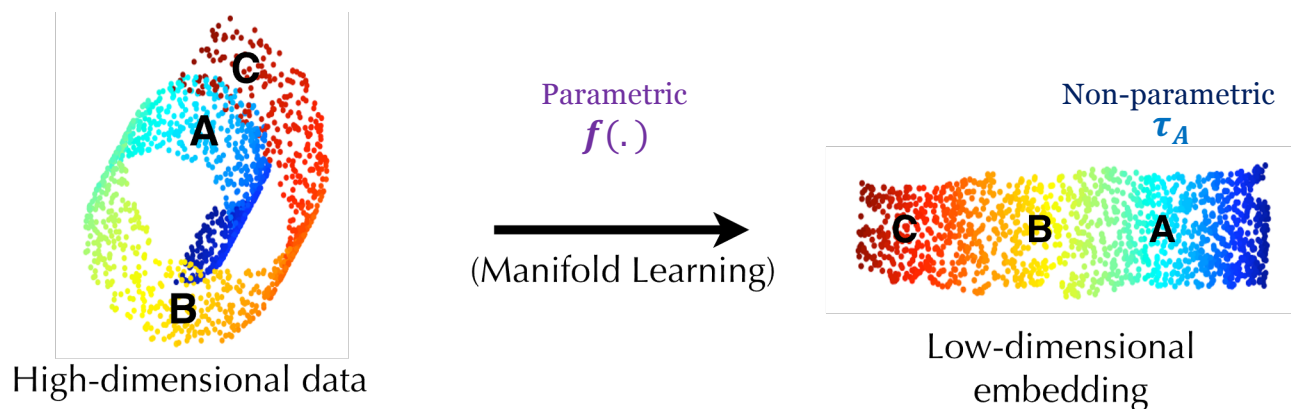
ManiNetCluster is a *subspace learning*, **non-linear** and non-expensive (by employing **manifold learning**) & support both principles

ManiNetCluster: manifold alignment to reveal the functional links between gene networks

Application: genomic functional linkages between light and dark periods of green alga



Manifold Learning



A d dimensional manifold M is embedded in a m dimensional space, and there is an explicit mapping $f: \mathbb{R}^m \rightarrow \mathbb{R}^d$ where $d \leq m$. Given samples $x_i \in \mathbb{R}^m$ with noise

$$\tau_i = f(x_i)$$

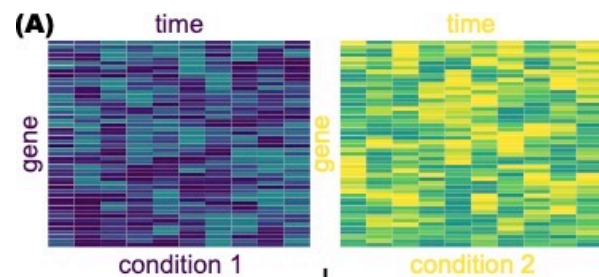
→ find $f(\cdot)$ or τ_i from given x_i

Parametric & generalizable (e.g., linear manifold learning)

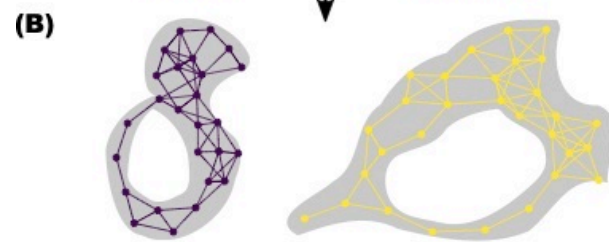
Nonparametric & nongeneralizable (e.g., nonlinear manifold learning)

Manifold Alignment

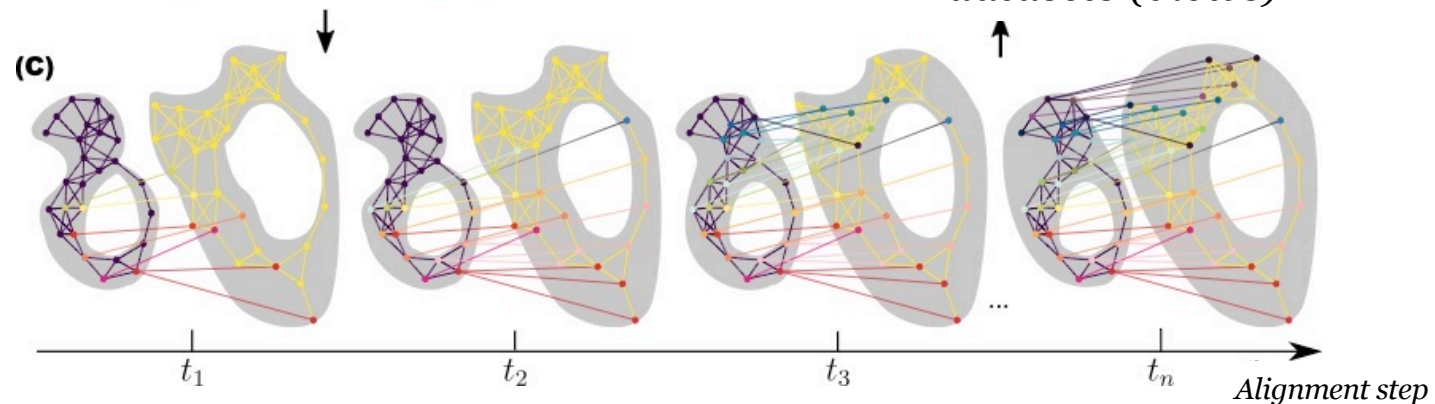
two datasets $X = [x_1, \dots, x_m], x_i \in \mathbb{R}^p$ $x_i \leftrightarrow y_i$ for $i \in [1, l]$
 $Y = [y_1, \dots, y_n], y_j \in \mathbb{R}^q$



To find mapping function
 $f(\cdot), g(\cdot)$



And learn common
 manifolds between two
 datasets (views)



Manifold Alignment framed by MV-ERM

Learn common manifolds between two datasets (views) $X = [x_1, \dots, x_m], x_i \in \mathbb{R}^p$ $Y = [y_1, \dots, y_n], y_j \in \mathbb{R}^q$ $x_i \leftrightarrow y_i$ for $i \in [1, l]$

To find mapping function $f(\cdot), g(\cdot)$ to minimize the cost function

$$\sum_{i,j} \|f(x_i) - g(y_j)\|^2 W^{i,j} + \sum_{i,j} \|f(x_i) - f(x_j)\|^2 W_X^{i,j} + \sum_{i,j} \|g(y_i) - g(y_j)\|^2 W_Y^{i,j}$$

Inter-view correspondence $\rightarrow$ global consistency consensus

Intra-view correspondence $\rightarrow$ local smoothness complementary

- Extract and optimally align **local geometry** to minimize **overall differences**
- Generalization of CCA $\sum_{i,j} \|f(x_i) - g(y_j)\|^2$
- Interpreted as a manifold regularization

$$\sum_{i,j} \|f(x_i) - g(y_j)\|^2 W^{i,j} + \text{tr}(\mathbf{f}^T L_X \mathbf{f}) + \text{tr}(\mathbf{g}^T L_Y \mathbf{g})$$

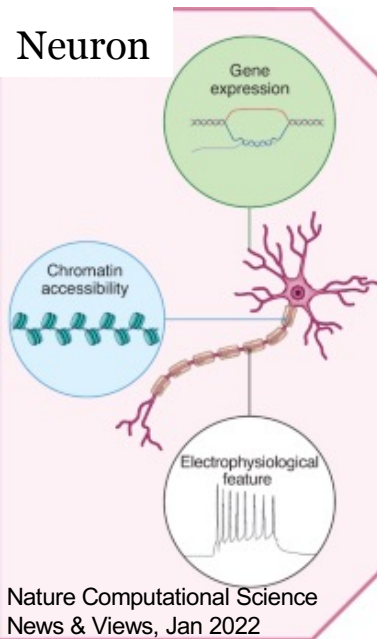
- Eigen-decomposition to solve nonlinear manifold alignment

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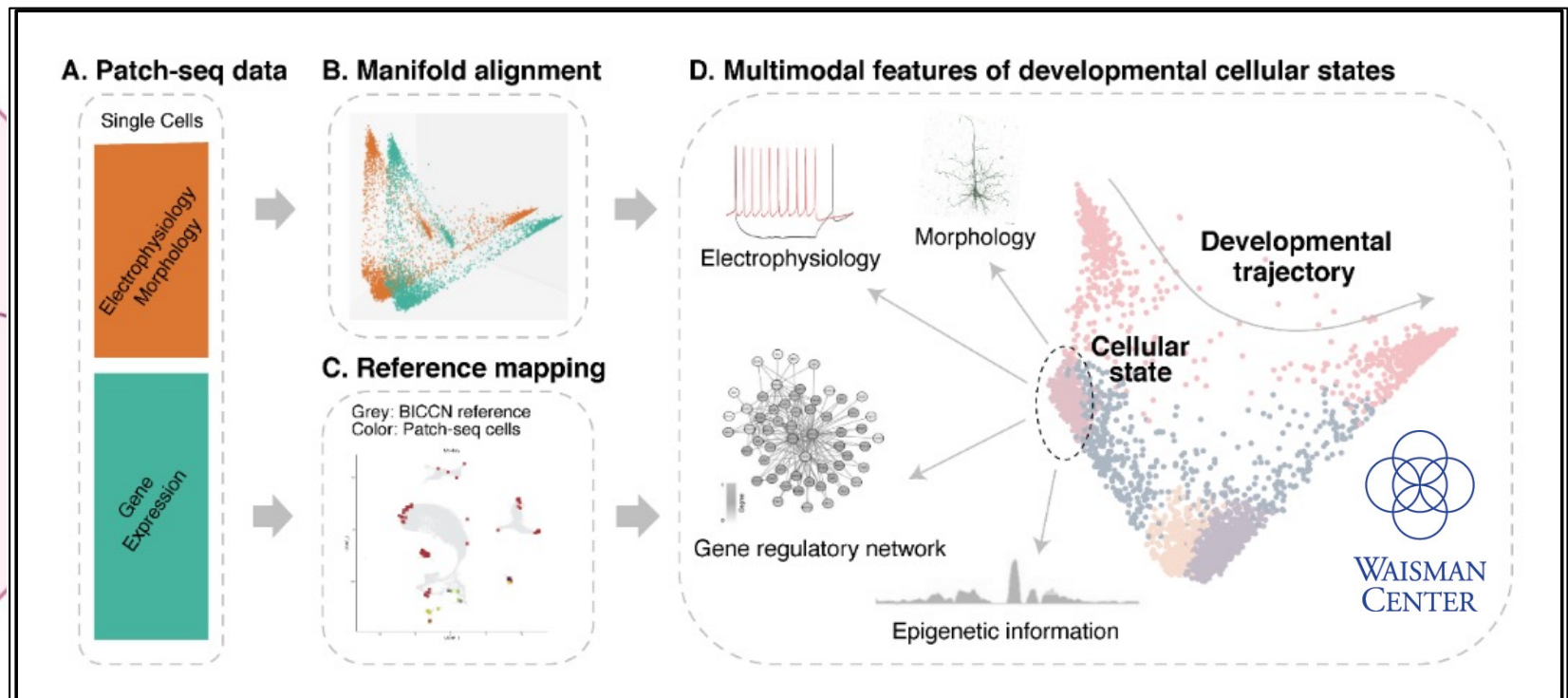
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Single-cell multi-modal data by Patch-seq (beyond omics)

Neuron

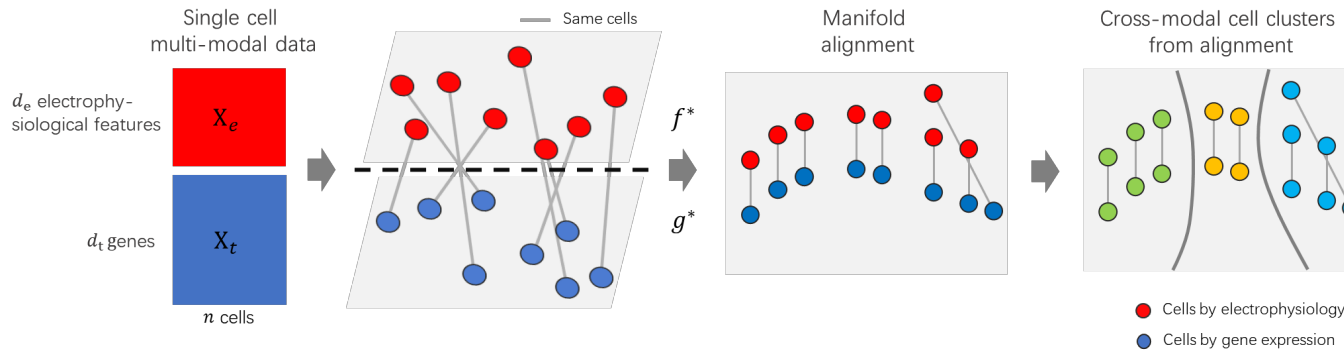


Nature Computational Science
News & Views, Jan 2022

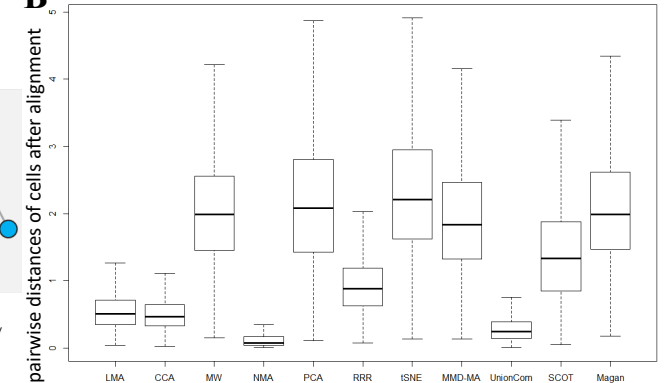


Manifold alignment of single neurons by electrophysiology and gene expression

A

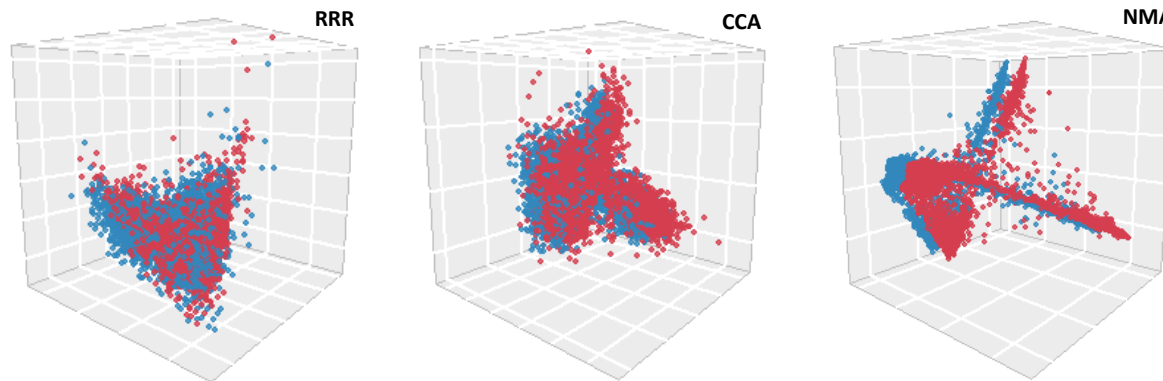


B



LMA = Linear Manifold Alignment
 CCA = Canonical Correlation Analysis
 MW = Manifold Warping
 NMA = Nonlinear Manifold Alignment
 PCA = Principal Component Analysis
 RRR = Reduced Rank Regression
 tSNE = Stochastic Neighbor Embedding
 MMD-MA = Manifold Alignment with maximum mean discrepancy
 UnionCom = Unsupervised Topological Alignment of Single-cell Multi-omics Integration
 SCOT = Single-Cell alignment using Optimal Transport
 MAGAN = Manifold Aligning GAN

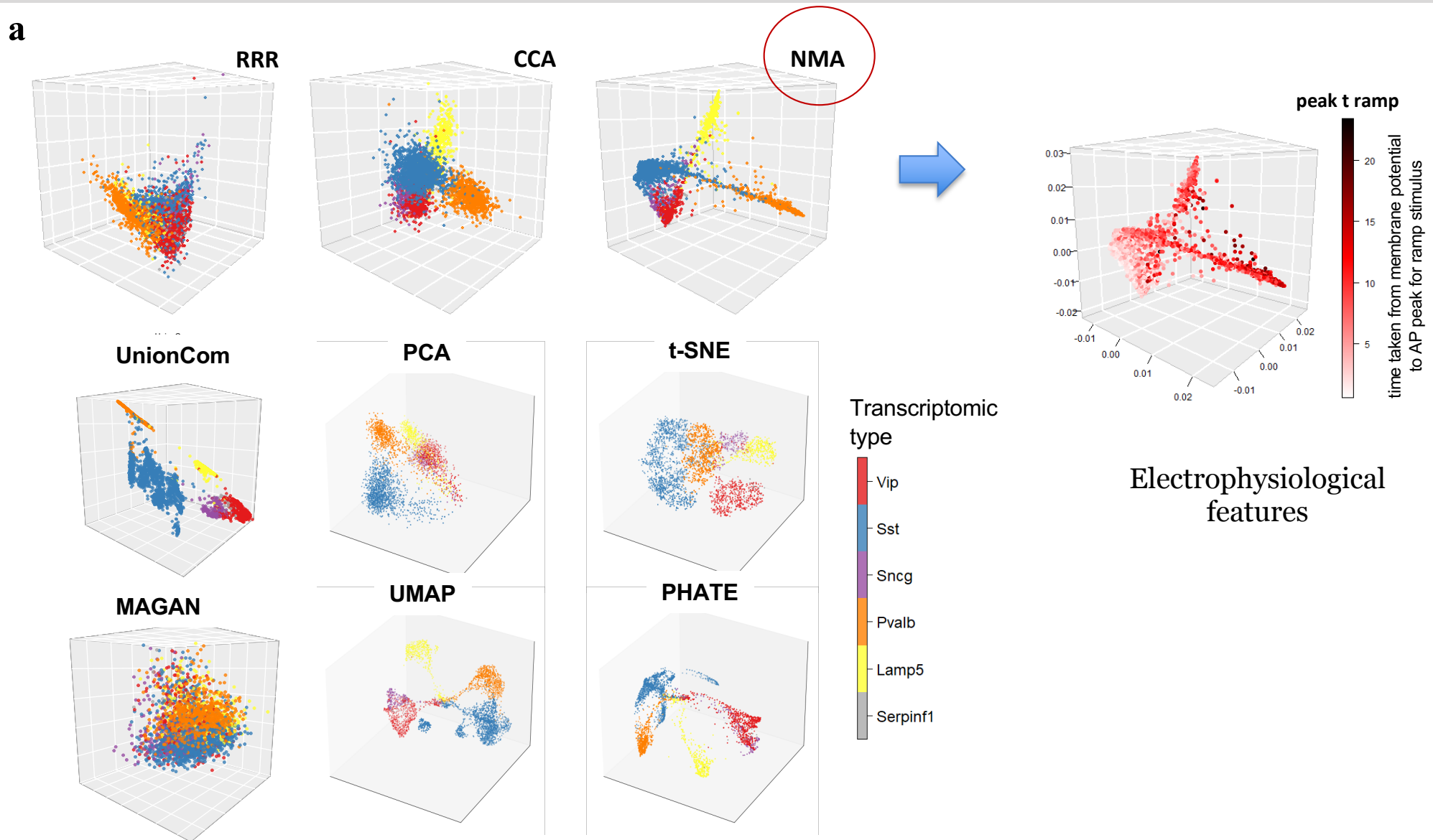
C



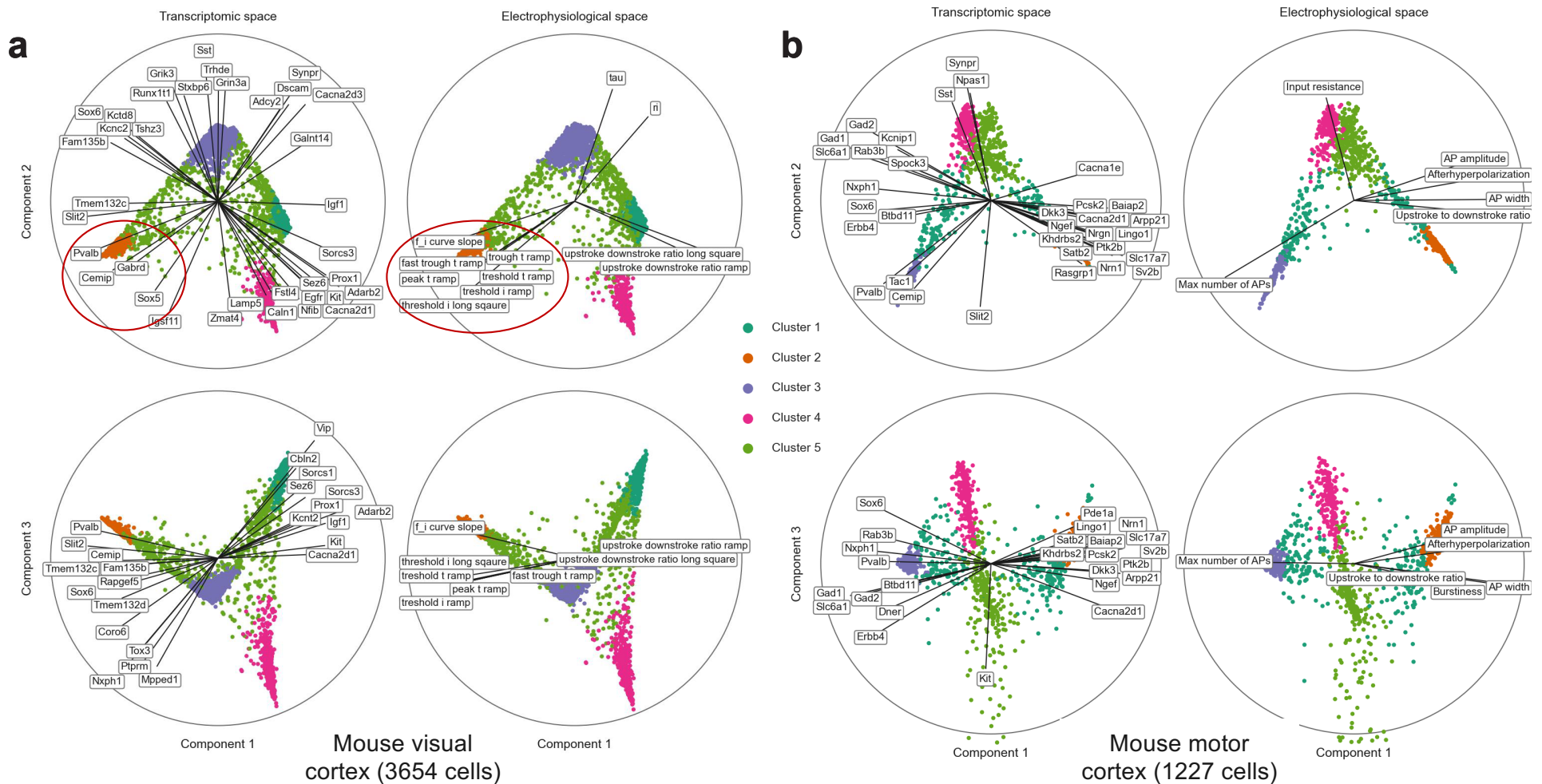
Jiawei Huang (M.S., Statistics, 2021)

Patch-seq data of ~3k neuronal cells in the mouse visual cortex from BRAIN Initiative

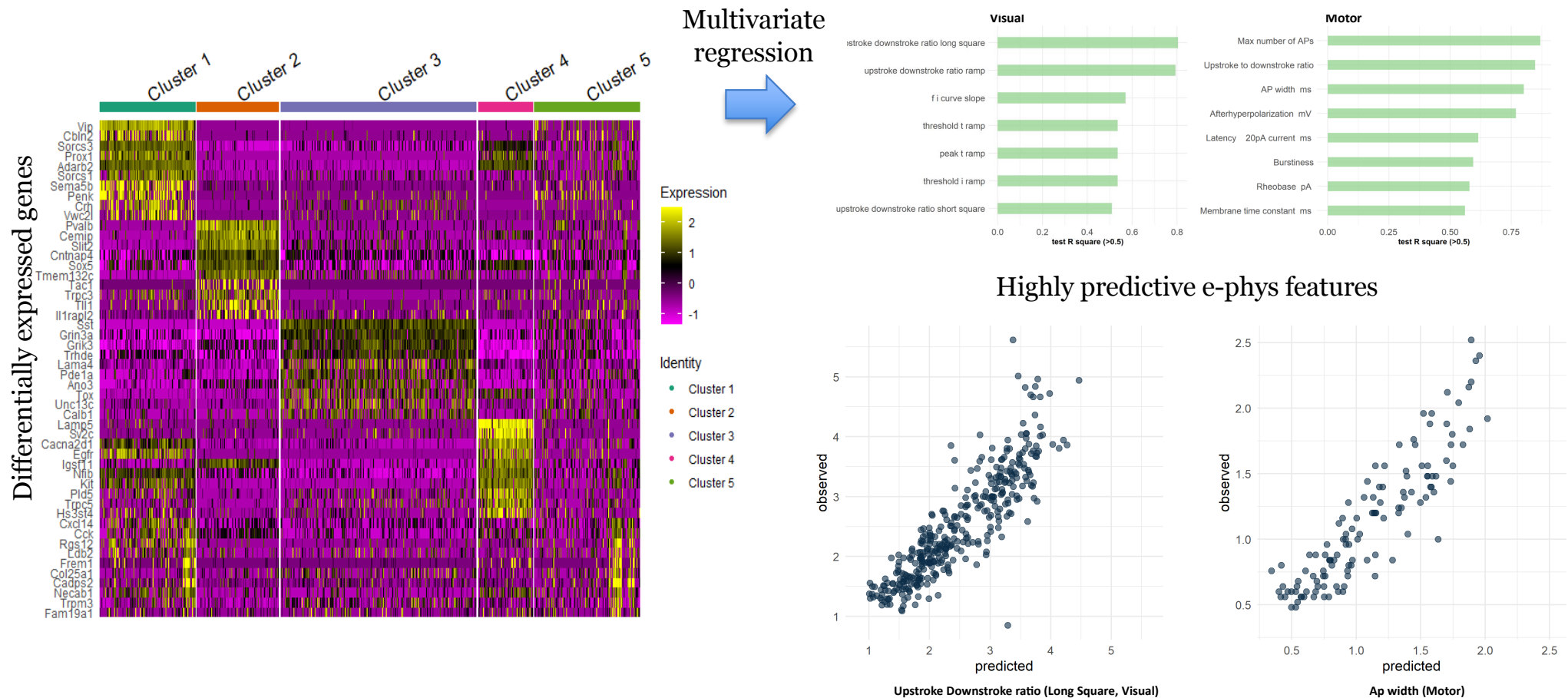
Nonlinear Manifold Alignment (NMA) uncovers trajectory with multi-modal changes



NMA aligned cells form cross-modal clusters, suggesting related genes and electrophysiological features



Predicting electrophysiological features by differentially expressed genes in cross-modal clusters

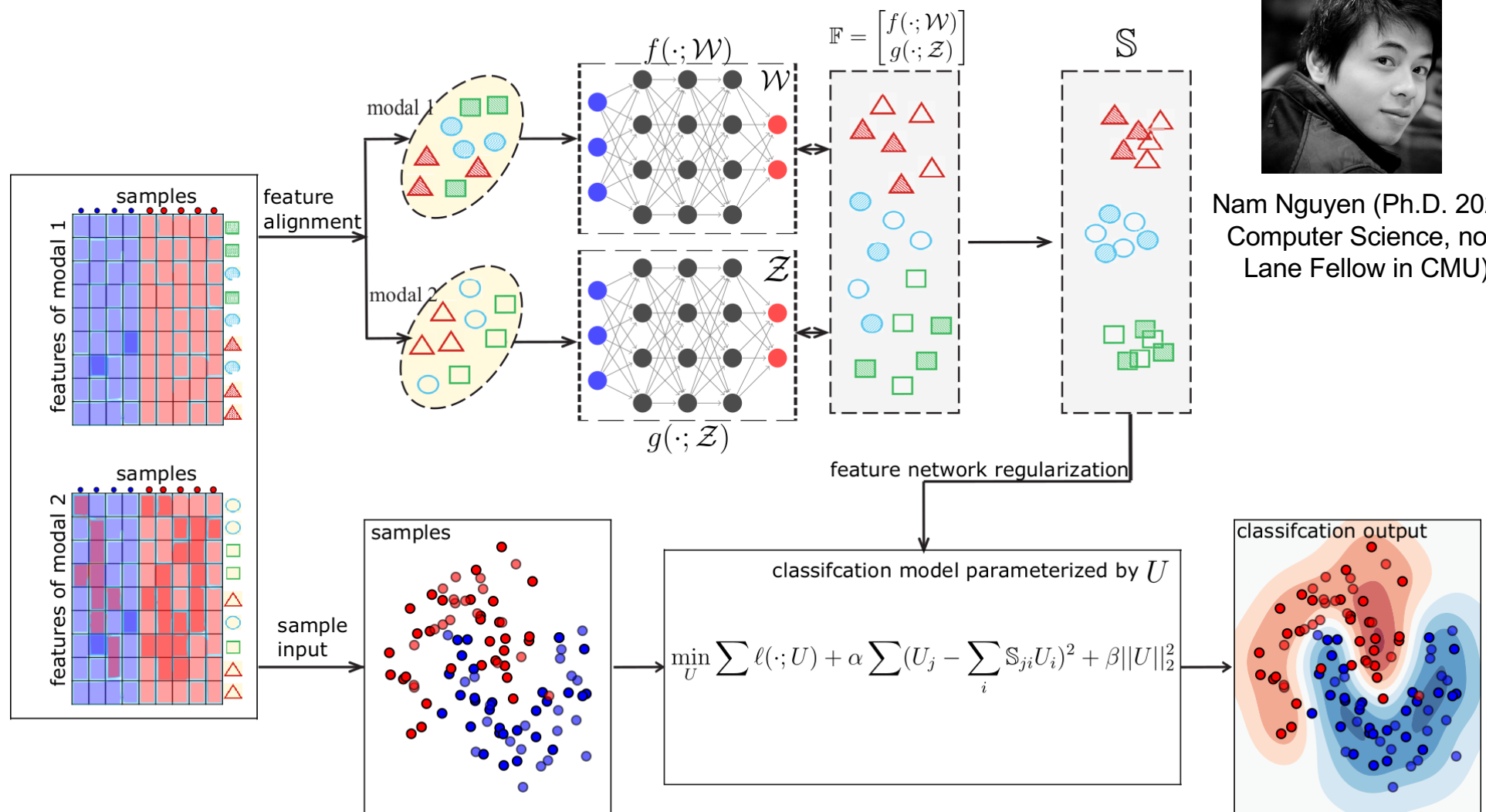


Can we align multi-modal features to improve phenotype prediction?

Outline

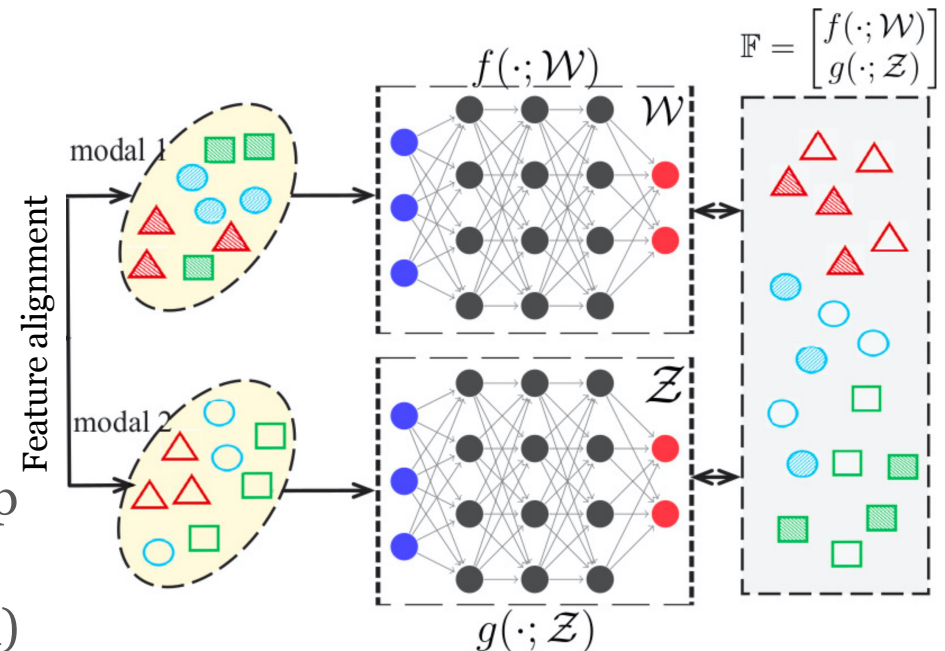
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deepManReg: a deep manifold-regularized learning model for phenotype prediction from multi-modal data



Phase 1: deep manifold alignment of multi-modal features

- Goal: reveal nonlinear relationships across multi-modal features
- Trade-off:
 - Features $\rightarrow$ Parametric
 - Nonlinear $\rightarrow$ Nonparametric
- deepManReg solution:
 - Parameterize $f(\cdot, \mathcal{W})$ & $g(\cdot, \mathcal{Z})$ by deep neural networks
 - Nonlinear manifold alignment (NMA)
- Eigen-decomposition to solve NMA:
 - Computationally intensive
 - Use gradient descent on a non-Euclidean space!



$$\min_{f, g} \text{tr}(\mathbb{F}^T L \mathbb{F})$$

$$\text{s.t. } \mathbb{F}^T D \mathbb{F} = \mathbb{I}.$$

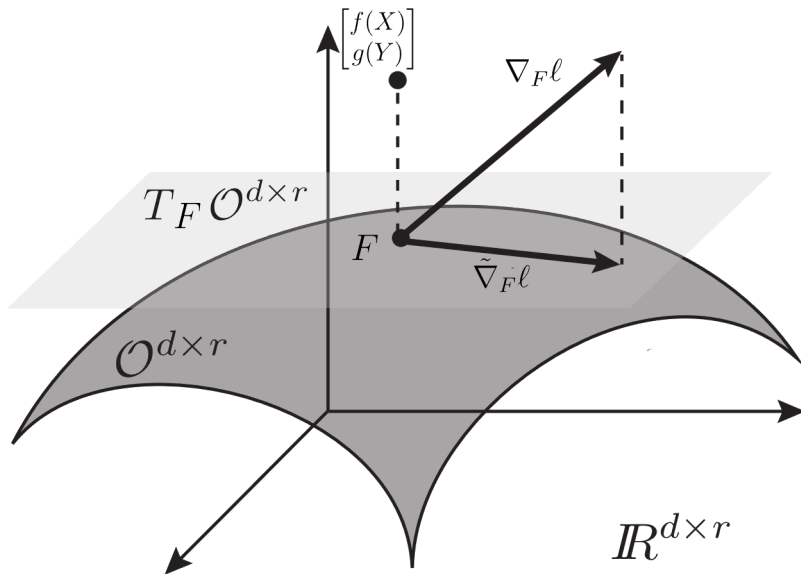
Optimization for deepManReg alignment

$\mathbb{F} = [f(X; \mathcal{W})^T, g(Y; \mathcal{Z})^T]^T$ can be solved by

$$\min_{f,g} \text{tr}(\mathbb{F}^T L \mathbb{F}) \text{ s.t. } \mathbb{F}^T D \mathbb{F} = \mathbb{I},$$

where L and D are joint Laplacian and diagonal matrices of prior correspondence across modalities

→ an optimization problem on Stiefel manifold $\mathcal{O}^{d \times r}$



- Forward pass — project the output $\begin{bmatrix} f(X) \\ g(Y) \end{bmatrix}$ onto Stiefel manifold

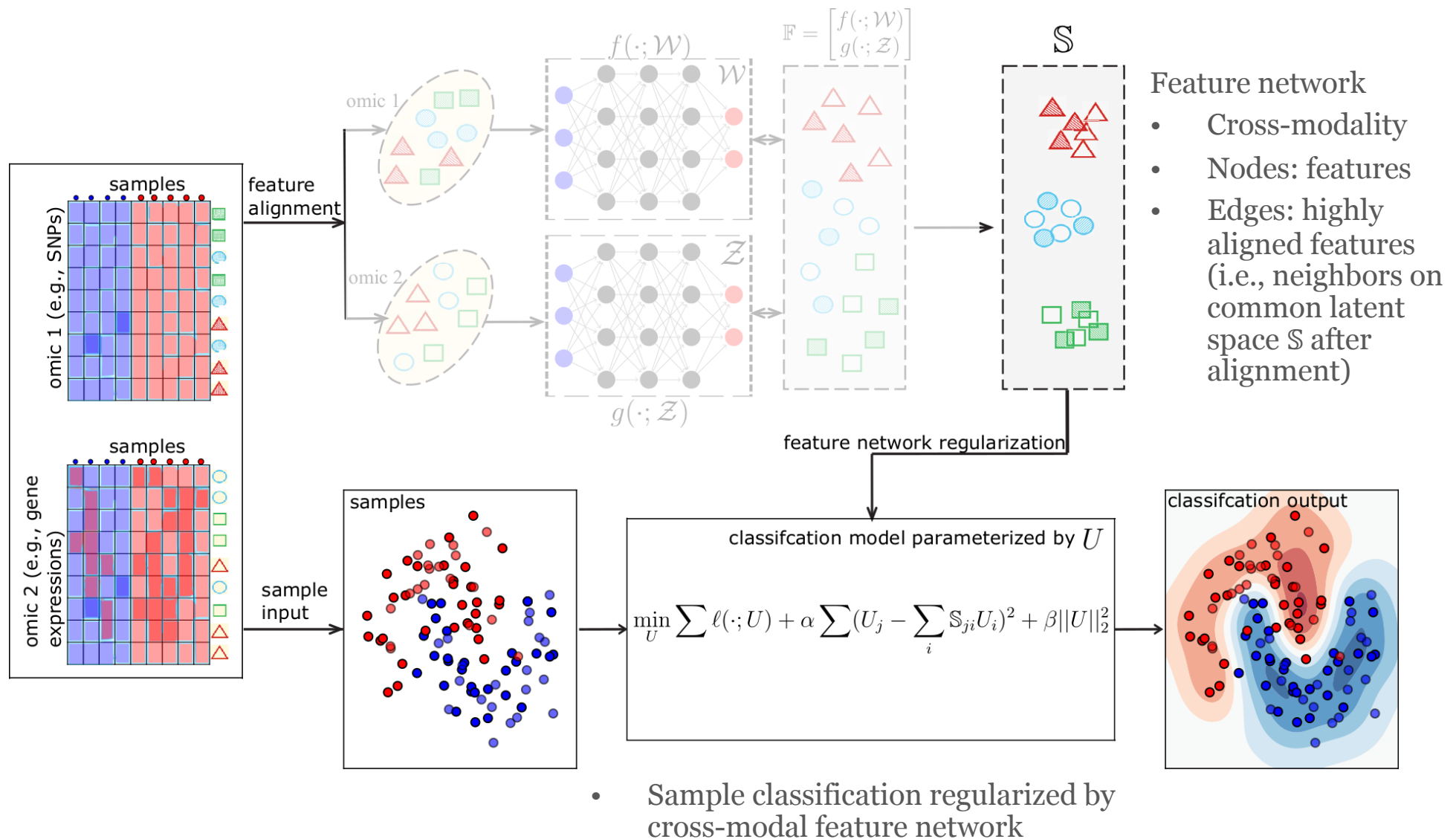
$$F = \pi \circ \begin{bmatrix} f(X) \\ g(Y) \end{bmatrix} = UIV^T$$

, where $\begin{bmatrix} f(X) \\ g(Y) \end{bmatrix} = U\Sigma V^T$ is the SVD of output

- Backward pass
 - Compute Euclidean gradient
- $$\nabla_F \ell = \frac{\partial \text{tr}(F^T L F)}{\partial F} = LF + L^T F$$
- Project Euclidean gradient onto the tangent space of Stiefel manifold
- $$\tilde{\nabla}_F \ell = \pi(\nabla_F \ell) = F \text{skew}(F^T \nabla_F \ell) + (I - FF^T) \nabla_F \ell$$
- Backpropagate the Riemannian gradient $\tilde{\nabla}_F \ell$ to update $\mathcal{W}, \mathcal{Z}$

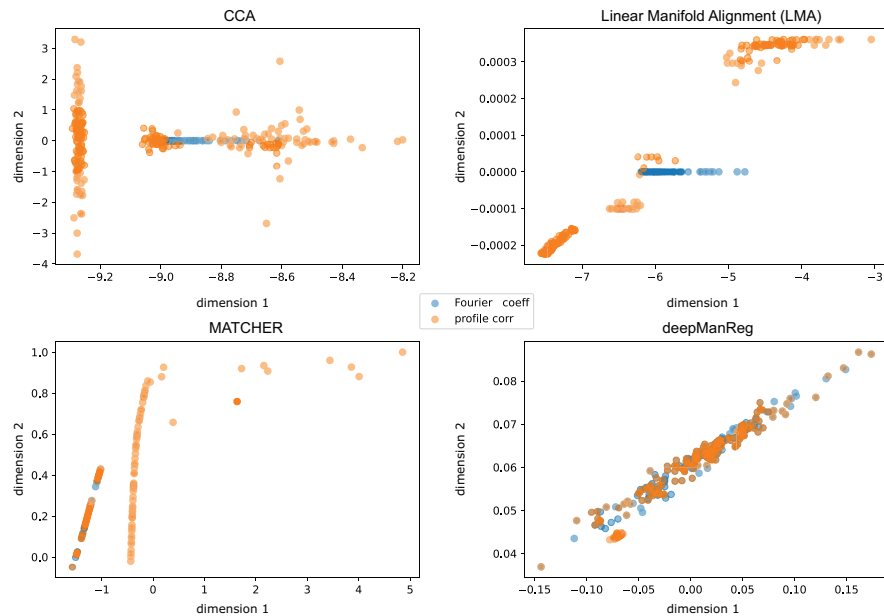
Cunningham et al. *The Journal of Machine Learning Research* 16.1 (2015): 2859-2900.

Phase 2: classification regularized by cross-modal feature network (aligned features)



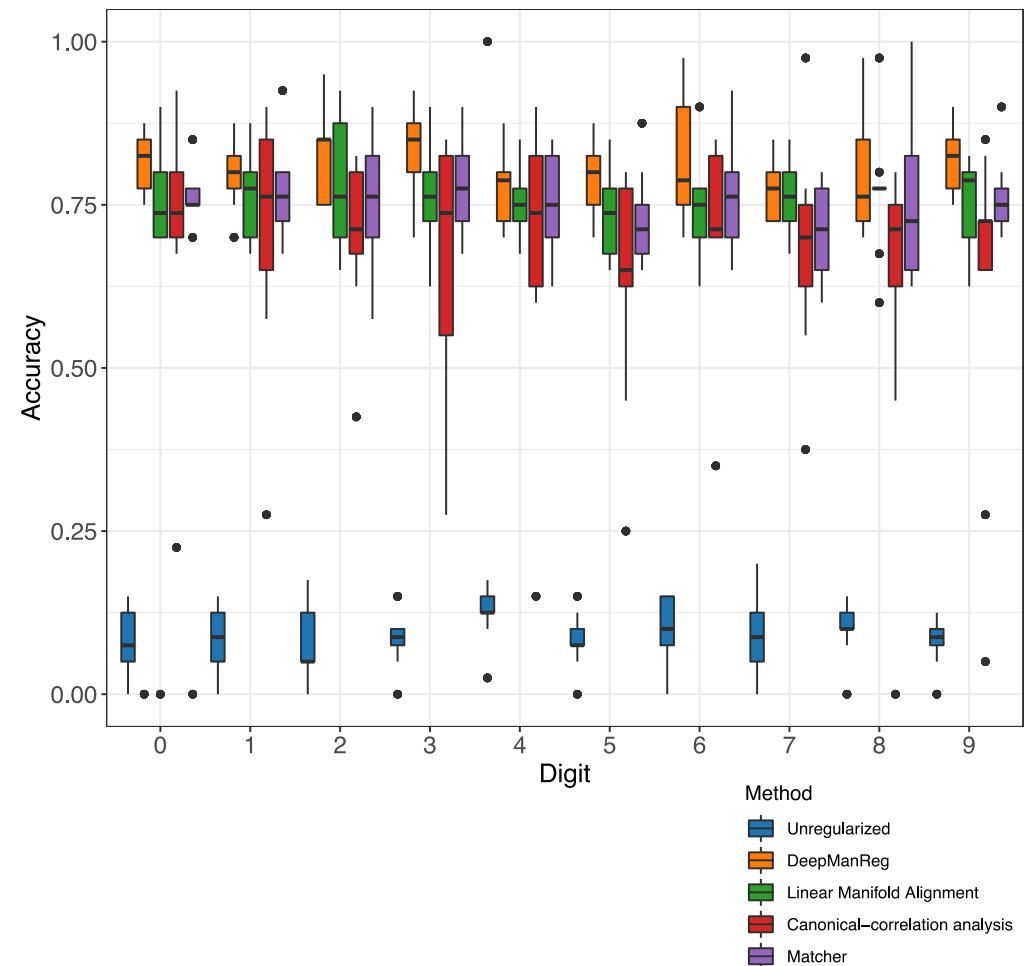
deepManReg alignment & classification of handwritten digits

Multi-modal feature alignment



- 2000 images of handwritten digits 0-9 (mfeat data) Breukelen et al. *Kybernetika*, 34(4):381–386, 1998.
- Two types of features:
216 **profile correlations**, 76 **Fourier coefficients**

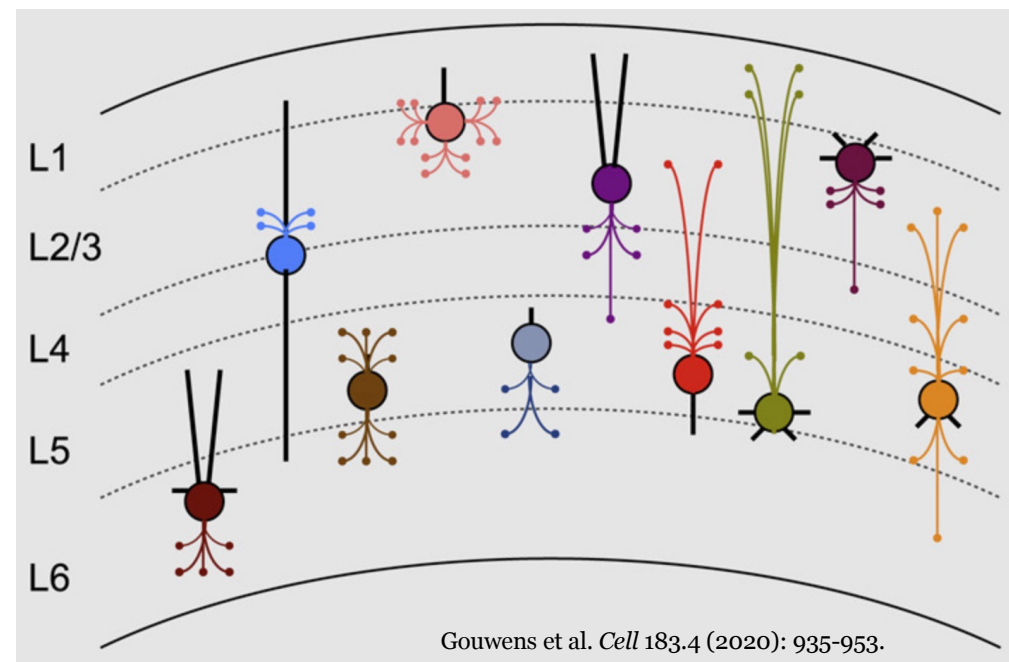
Digit classification



deepManReg alignment & classification of neuronal cells

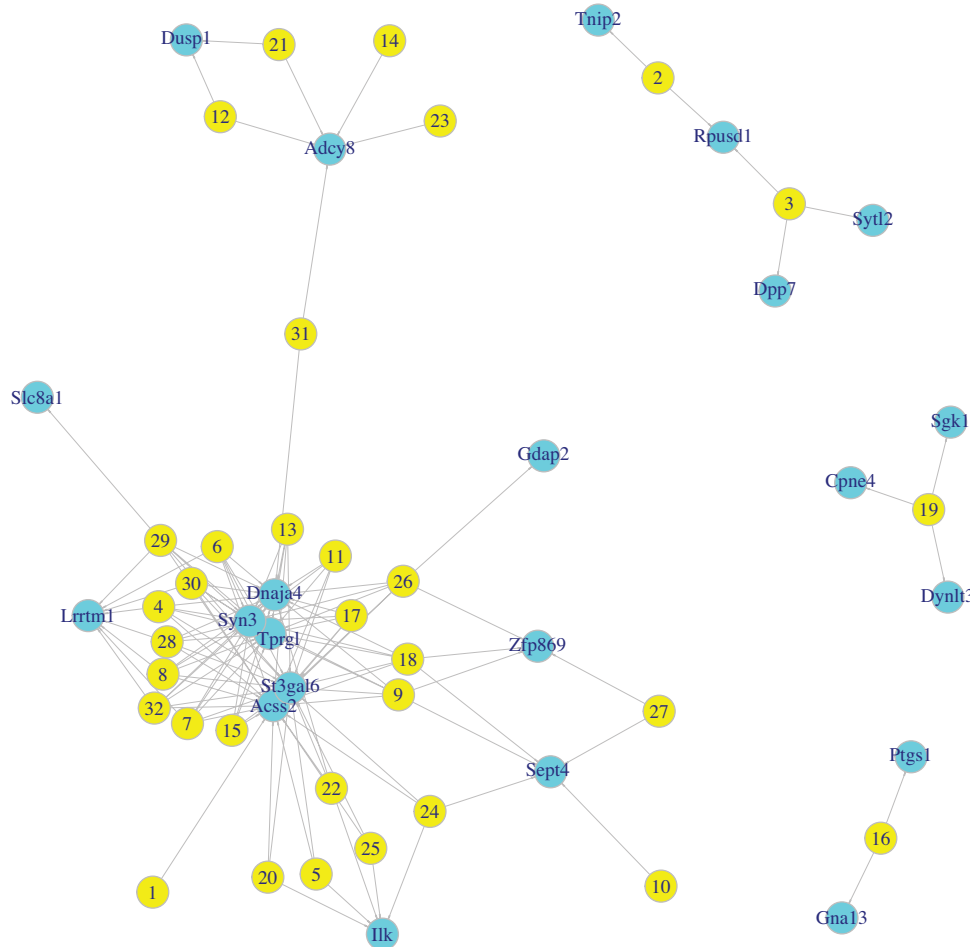
Single-cell multi-modal data by Patch-seq

- 3654 GABAergic cortical neurons in mouse visual cortex
- Modality 1: Electrophysiological features
 - By hyperpolarizing and depolarizing current injection stimuli and responses of short (3 ms) current pulses, long (1 s) current steps, and slow (25 pA/s) current ramps.
- Modality 2: Genes
 - Expression levels
- Phenotype: 5 cortical layers, L1, L2/3, L4, L5, and L6
- Running time (alignment only)
 - CCA (725.96 seconds)
 - Manifold Alignment (663.43 seconds)
 - MATCHER (150.94 seconds)
 - deepManReg (57.90 seconds by GPUs GTX 1060Ti and 90.10 seconds by CPU i5-8250U)



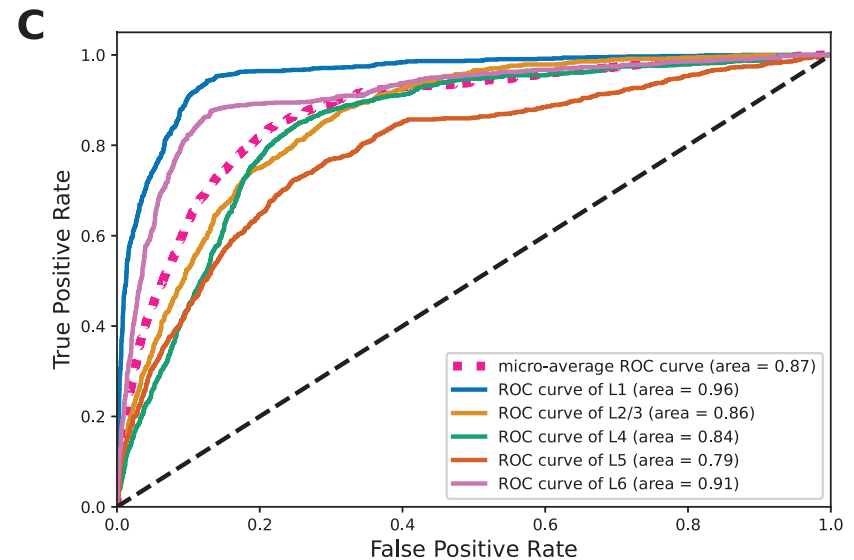
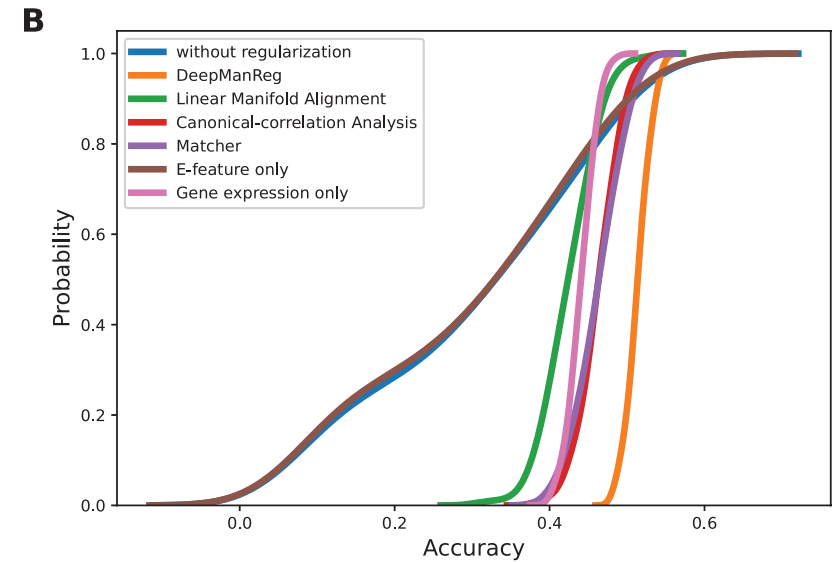
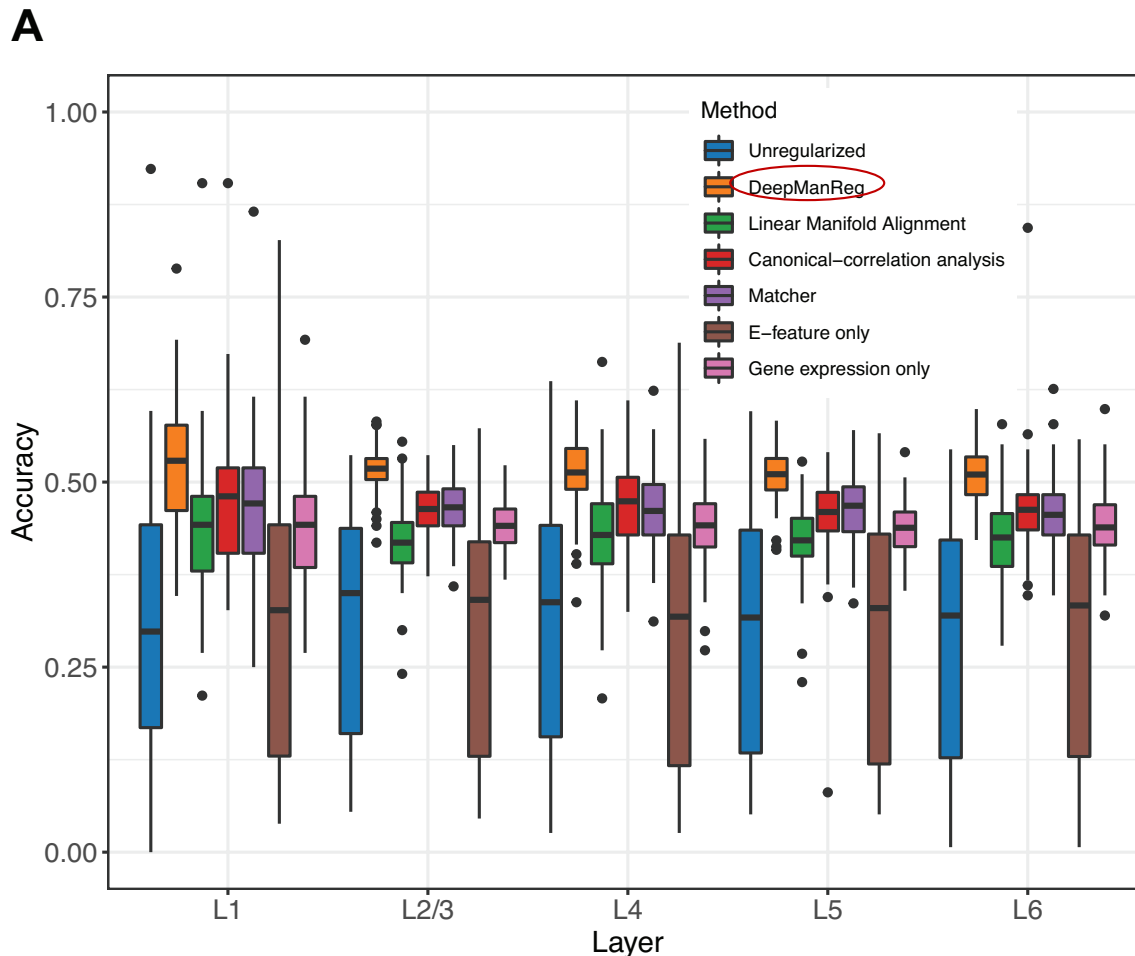
Cross-modal feature network linking aligned genes and electrophysiological features

■ Electrophysiological feature
■ Gene



e-Features	Index
rheobase_sweep_num	1
thumbnail_sweep_num	2
vrest	3
sag	4
tau	5
f_i_curve_slope	6
adaptation	7
latency	8
upstroke_downstroke_ratio_long_square	9
peak_v_long_square	10
peak_t_long_square	11
trough_v_long_square	12
trough_t_long_square	13
fast_trough_v_long_square	14
fast_trough_t_long_square	15
threshold_i_long_square	16
threshold_t_long_square	17
upstroke_downstroke_ratio_ramp	18
peak_v_ramp	19
peak_t_ramp	20
trough_v_ramp	21
trough_t_ramp	22
fast_trough_v_ramp	23
fast_trough_t_ramp	24
threshold_t_ramp	25
upstroke_downstroke_ratio_short_square	26
peak_v_short_square	27
peak_t_short_square	28
trough_t_short_square	29
fast_trough_t_short_square	30
threshold_v_short_square	31
threshold_t_short_square	32

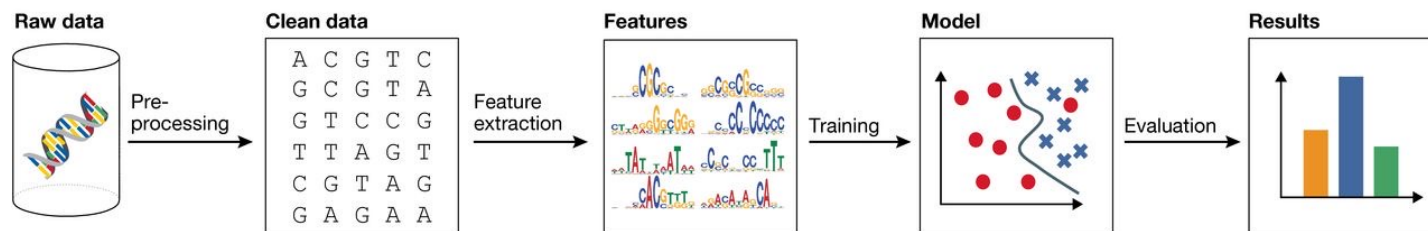
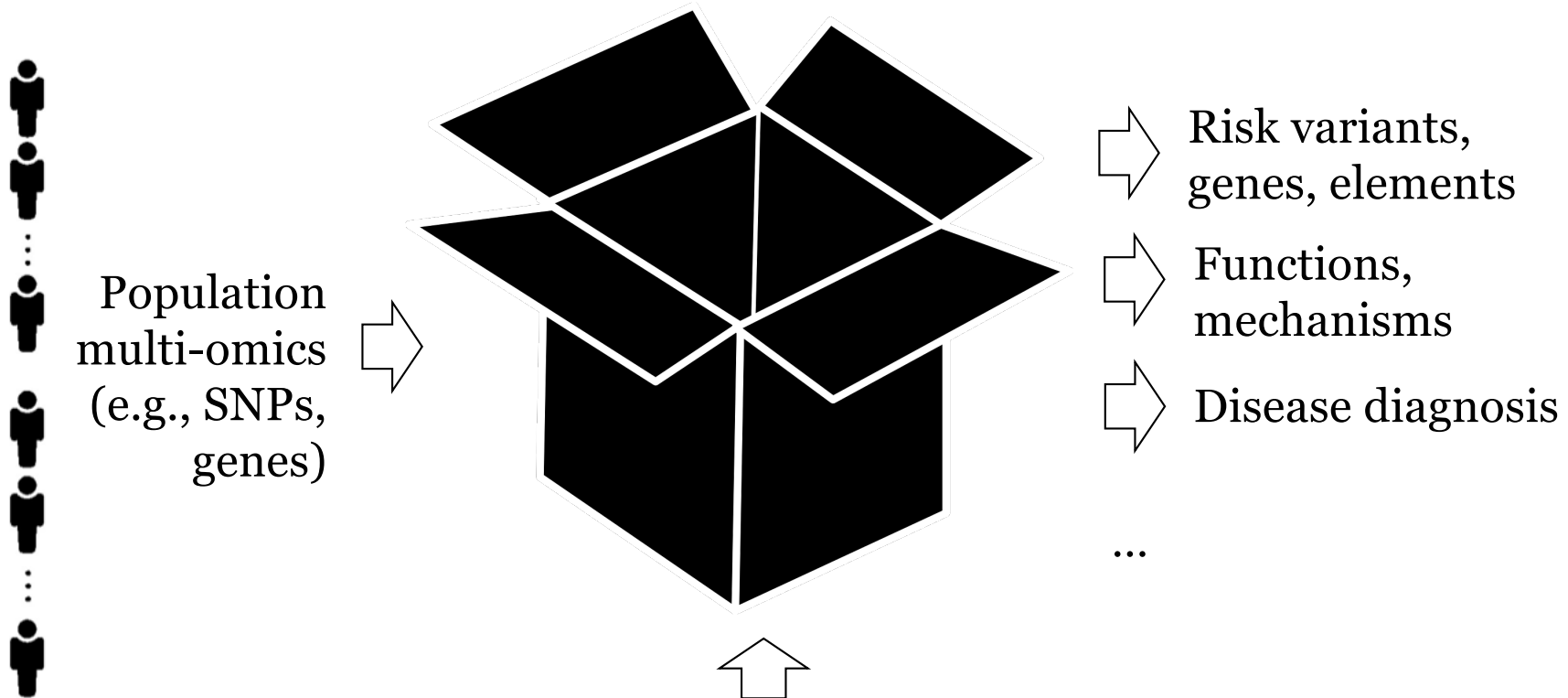
Feature-network-regularized classification of cortical layers of neuronal cells



Outline

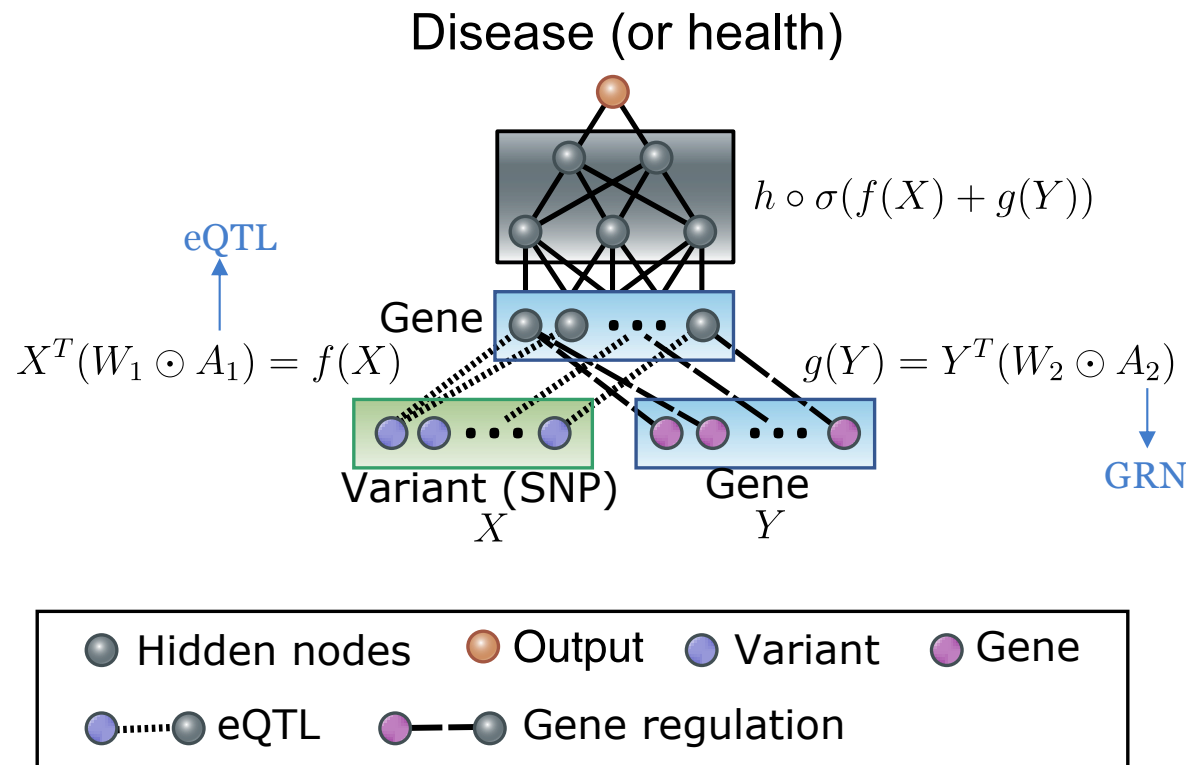
- Background
 - Functional genomics & multi-omics
 - Gene regulation
- Multi-view learning for multi-modal data
 - Multi-view Empirical Risk Minimization (MV-ERM)
 - Manifold alignment
- App 1: *single-cell multi-modal data integration*
 - Predicting neuronal electrophysiology from gene expression
- App 2: *deep manifold-regularized classification*
 - Predicting cortical layers of neurons from multi-modalities
- App 3: *biologically interpretable neural network modeling*
 - Disease prediction and functional prioritization

Population
multi-omics
(e.g., SNPs,
genes)



SLIDE 47

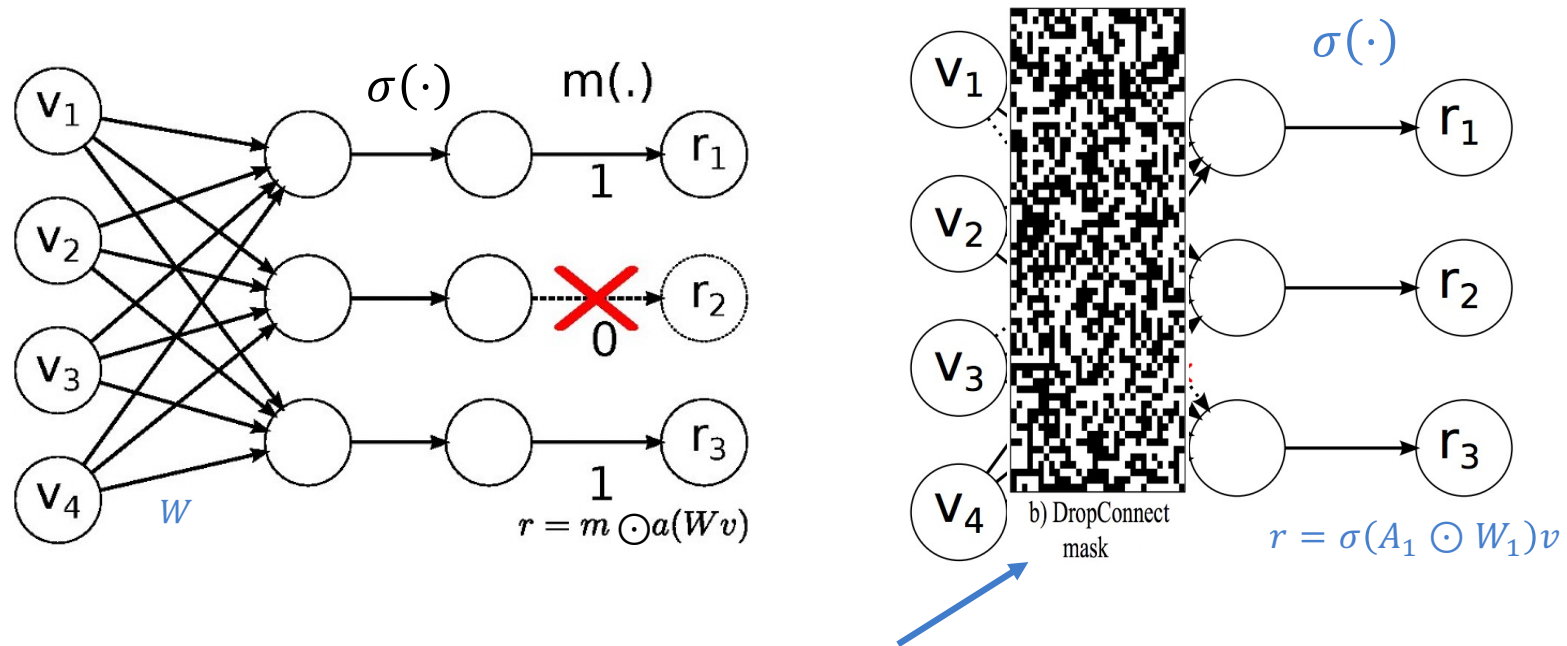
Varmole: Interpretable deep neural network model prioritizes disease variants and genes via DropConnect



- Input form 2 omics, X, Y (SNPs & genes)
- First layer embed A_1 and A_2 – eQTL and gene regulatory network (GRN)
→ From variants (& gene regulations) to gene expression
- Other fully connected hidden layers: h ;
→ From gene expression to phenotypes
- Softmax classification layer:
 $o = \delta \left(h \circ \sigma(f(X) + g(Y)) \right);$
- The Cross-Entropy:
$$L(o, \hat{o}) = - \frac{1}{n \sum_{i=1}^n y_i \log(\hat{y}_i)}$$
- Varmole:
$$\min L(o, \hat{o}) + \|W\|_1$$

Drop-connect

- Drop-out and drop-connect are 2 simple but effective regularization techniques

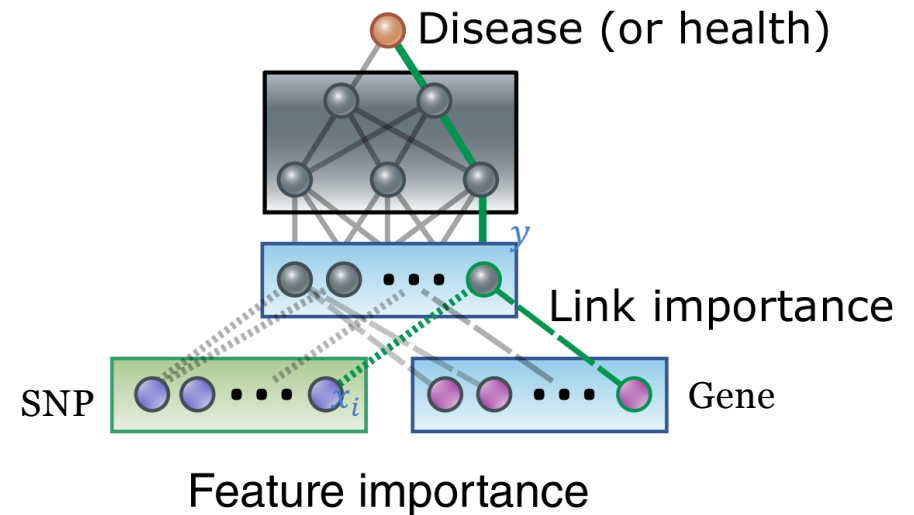


The drop-connect mask is eQTL or GRN (A_1 or A_2)

Interpretation: prioritization via Integrated Gradients

- Given a **model** F , an **input** x , and the **output** $F(x)$ of the model for input in question, an **attribution** methods returns the 'relevance' of each input **feature** i to the output
- How importance a gene (SNP, eQTL link, TF-gene link) to the disease outcome

Interpret with Integrated gradient



$$\text{Cond}_i^y(x) ::= (x_i - x'_i) \cdot \int_{\alpha=0}^1 \frac{\partial F(x' + \alpha(x - x'))}{\partial y} \cdot \frac{\partial y}{\partial x_i} d\alpha$$

Importance score
of link $x_i \rightarrow y$

$$\text{IG}_i(x) ::= (x_i - x'_i) \cdot \int_{\alpha=0}^1 \frac{\partial F(x' + \alpha(x - x'))}{\partial x_i} d\alpha$$

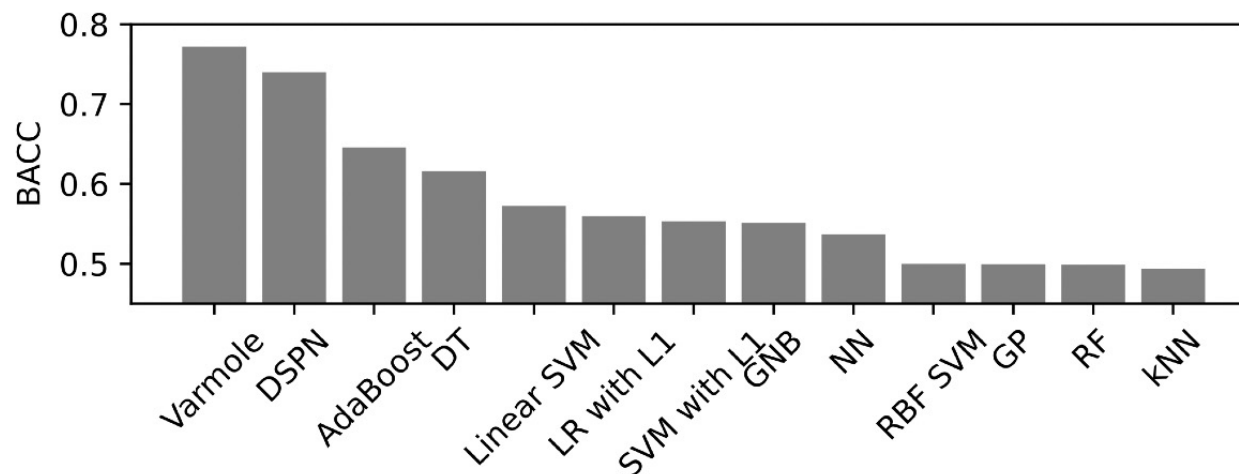
Importance score
of feature i of input x

Sundararajan, M., Taly, A., & Yan, Q. (2017). *arXiv preprint arXiv:1703.01365*.

$\frac{\partial F(x)}{\partial x_i}$ is the gradient of F along the i^{th} dimension at x

Application for schizophrenia

- Dataset:
 - RNA-seq gene expression & genotype data (dosage) for 487 schizophrenia (scz) vs. 891 non-scz human brain samples (front cortex)
 - Embedding GTEx eQTLs & PsychENCODE GRN for human brain front cortex
 - → 127304 SNPs, 2598 genes



Prioritized gene functions & regulatory links for schizophrenia

- A list of enriched functions ($\text{FDR} < 0.05$) from prioritized genes:
 - neuron development
 - axon guidance
 - cell adhesion
 - calcium signaling
 - response to external stimulus
 - NMDA receptor
 - insulin secretion
- Prioritized SNP-gene pairs
 - SNP-gene pairs on the interacting enhancers and promoters (Hi-C) have significantly higher importance scores ($p < 5e-5$)
 - Potential regulatory roles of prioritized SNPs to genes via enhancers

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Thank you!

Current lab members

- Dr. Shuang Liu (Data Scientist III)
- Dr. Pramod Chandrashekar (Postdoc)
- Dr. Chirag Gupta (Postdoc)
- Dr. Chenfeng He (Postdoc)
- Dr. Kalpana H. Arachchilage (Postdoc)
- Saniya Khullar (CIBM fellow & Ph.D. candidate, Biomedical Data Science)
- Ting Jin (Ph.D. student, Biomedical Data Science)
- Sayali Alatar (Ph.D. student, Computer Sciences)
- Noah Cohen Kalafut (Ph.D. student, Computer Sciences)
- Jie Sheng (Biostatistician, Waisman Center)
- Jonathan Bryan (Undergraduate, Neurobiology)

Recent graduates

- Nam Nguyen (Ph.D. 2021, Computer Science, Lane Fellow in Carnegie Mellon University)
- Jiawei Huang (M.S. 2021, Statistics, Ph.D. student in University of Cincinnati)
- Yudi Mu (M.S. 2021, Statistics, Ph.D. student in University of California Riverside)
- Mufang Yin (M.S. 2020, Statistics, Ph.D. student in Rutgers University)
- Peter Rehani (B.S. 2020, Neurobiology, Morgridge Institute for Research)

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- DOE QPSI

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Various positions available!

