

# Measuring transcriptomes with RNA-Seq

---

BMI/CS 776

[www.biostat.wisc.edu/bmi776/](http://www.biostat.wisc.edu/bmi776/)

Spring 2019

Colin Dewey

[colin.dewey@wisc.edu](mailto:colin.dewey@wisc.edu)

# Overview

---

- RNA-Seq technology
- The RNA-Seq quantification problem
- Generative probabilistic models and Expectation-Maximization for the quantification task

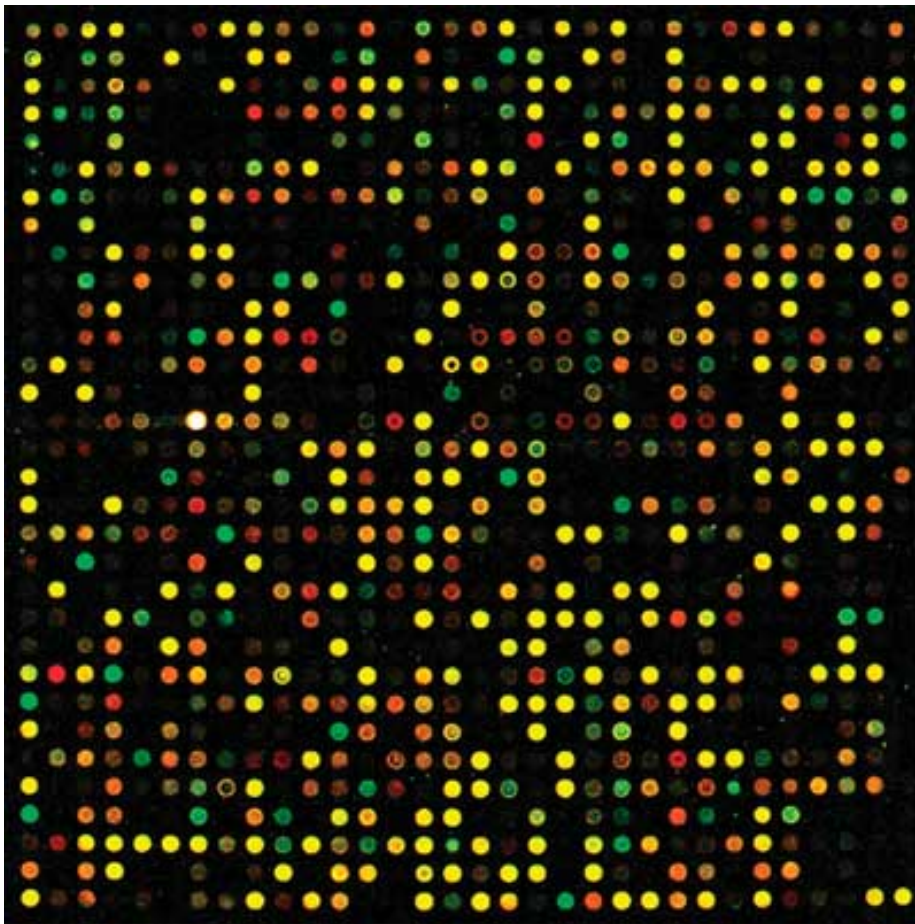
# Goals for lecture

---

- What is RNA-Seq?
- How is RNA-Seq used to measure the abundances of RNAs within cells?
- What probabilistic models and algorithms are used for analyzing RNA-Seq?

# Measuring transcription the old way: microarrays

---



- Each spot has “probes” for a certain gene
- Probe: a DNA sequence complementary to a certain gene
- Relies on complementary hybridization
- Intensity/color of light from each spot is measurement of the number of transcripts for a certain gene in a sample
- Requires knowledge of gene sequences

# Advantages of RNA-Seq over microarrays

---

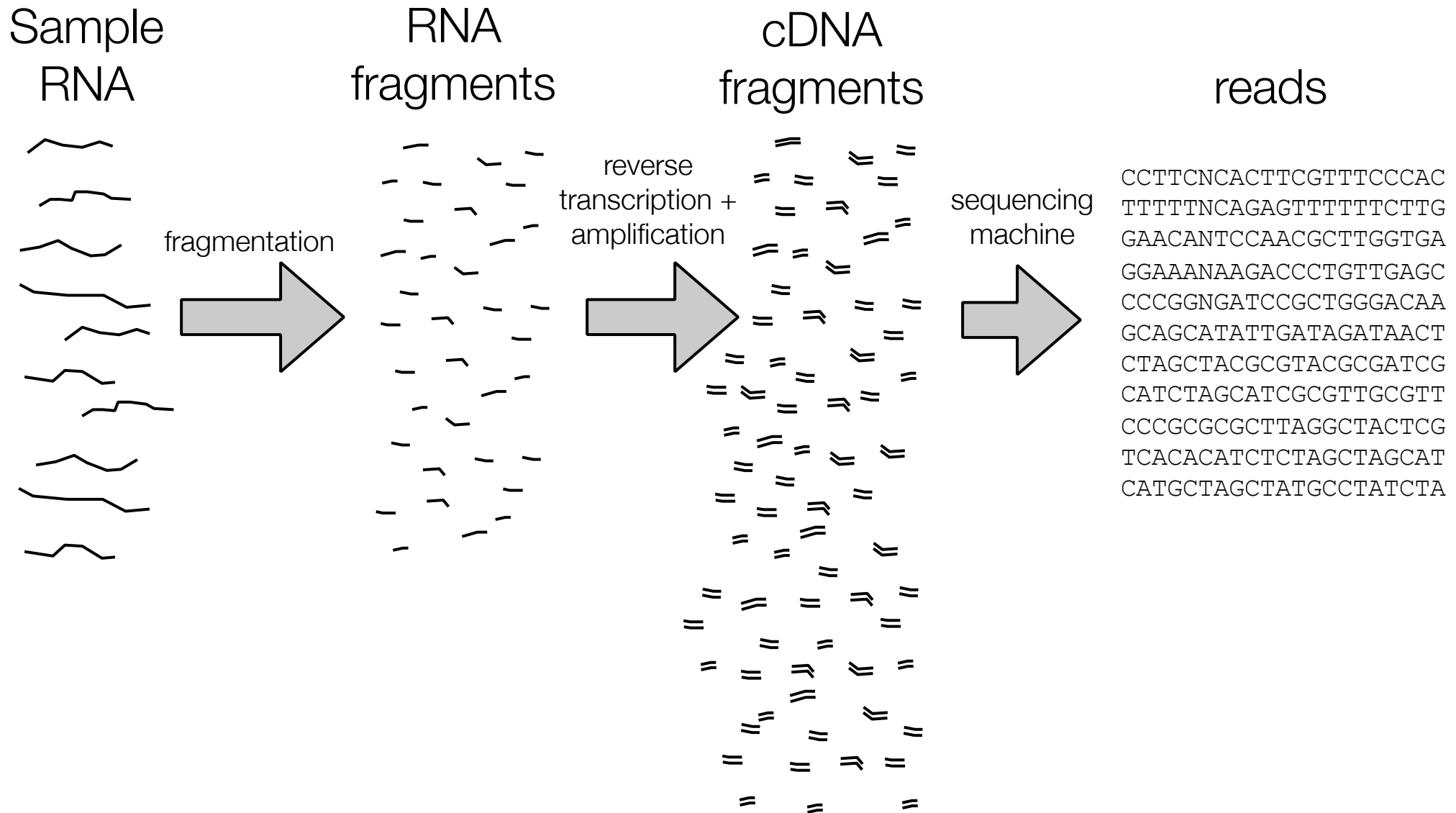
- No reference sequence needed
  - With microarrays, limited to the probes on the chip
- Low background noise
- Large dynamic range
  - $10^5$  compared to  $10^2$  for microarrays
- High technical reproducibility
- Identify novel transcripts and splicing events

# RNA-Seq technology

---

- Leverages rapidly advancing sequencing technology
- Transcriptome analog to whole genome shotgun sequencing
- Two key differences from genome sequencing:
  1. Transcripts sequenced at different levels of coverage - expression levels
  2. Sequences already known (in many cases) - coverage is measurement

# A generic RNA-Seq protocol



# RNA-Seq data: FASTQ format

```
@HWUSI-EAS1789_0001:3:2:1708:1305#0/1
CCTTCNCACTTCGTTTCCCACTTAGCGATAATTTG
+HWUSI-EAS1789_0001:3:2:1708:1305#0/1
VVULVBVYVYZZXZZ\ee[a^b`[a\ a[\a^^\
@HWUSI-EAS1789_0001:3:2:2062:1304#0/1
TTTTTNCAGAGTTTTTTCTTGAAGTGGAAATTTTT
+HWUSI-EAS1789_0001:3:2:2062:1304#0/1
a__[\Bbbb`edeeefd`cc`b]bffff`ffffff
@HWUSI-EAS1789_0001:3:2:3194:1303#0/1
GAACANTCCAACGCTTGGTGAATTCTGCTTCACAA
+HWUSI-EAS1789_0001:3:2:3194:1303#0/1
ZZ[[VBZZY][TWQQZ\ZS\[ZZXV__\OX`a[ZZ
@HWUSI-EAS1789_0001:3:2:3716:1304#0/1
GGAAANAAGACCCTGTTGAGCTTGACTCTAGTCTG
+HWUSI-EAS1789_0001:3:2:3716:1304#0/1
aaXWYBZVTXZX_]Xdccdfbb_\`a\ aY_^]LZ^
@HWUSI-EAS1789_0001:3:2:5000:1304#0/1
CCCGGNGATCCGCTGGGACAAGCAGCATATTGATA
+HWUSI-EAS1789_0001:3:2:5000:1304#0/1
aaaaaBeeeeffffehhhhhhggdhhhhahhhadh
```

← name  
← sequence  
← qualities

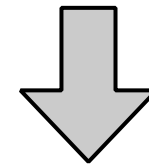
> read

paired-end reads

read1  
→  
←  
read2

1 Illumina HiSeq 2500

lane



~150 million reads



# Tasks with RNA-Seq data

---

- **Assembly:**

- Given: RNA-Seq reads (and possibly a genome sequence)
- Do: Reconstruct full-length transcript sequences from the reads

- **Quantification (our focus):**

- Given: RNA-Seq reads and transcript sequences
- Do: Estimate the relative abundances of transcripts (“gene expression”)

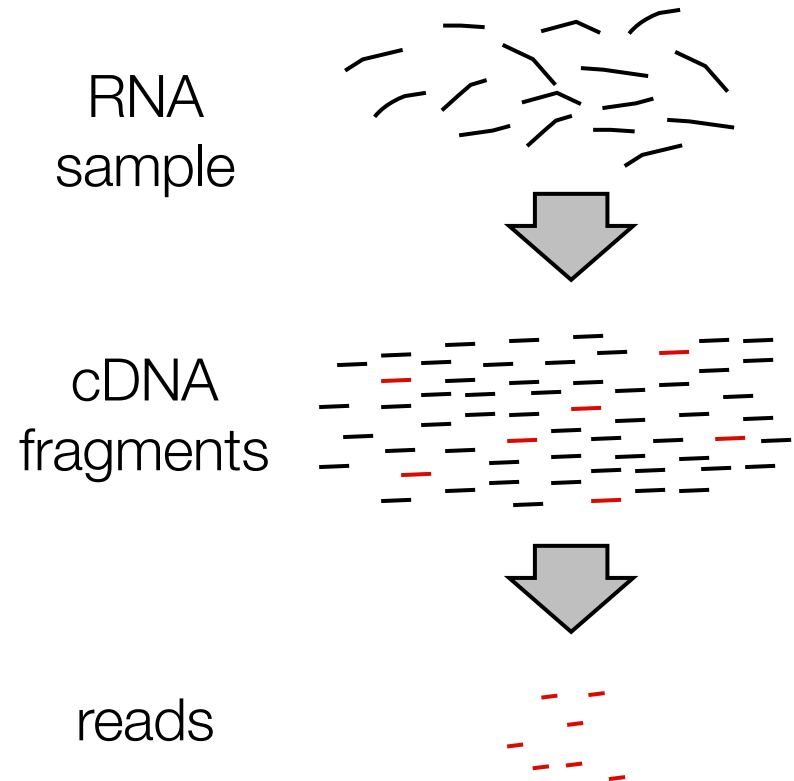
- **Differential expression:**

- Given: RNA-Seq reads from two different samples and transcript sequences
- Do: Predict which transcripts have different abundances between two samples

# RNA-Seq is a *relative* abundance measurement technology

---

- RNA-Seq gives you reads from the ends of a random **sample** of fragments in your library
- Without additional data this only gives information about **relative** abundances
- Additional information, such as levels of “spike-in” transcripts, are needed for absolute measurements



# Issues with relative abundance measures

---

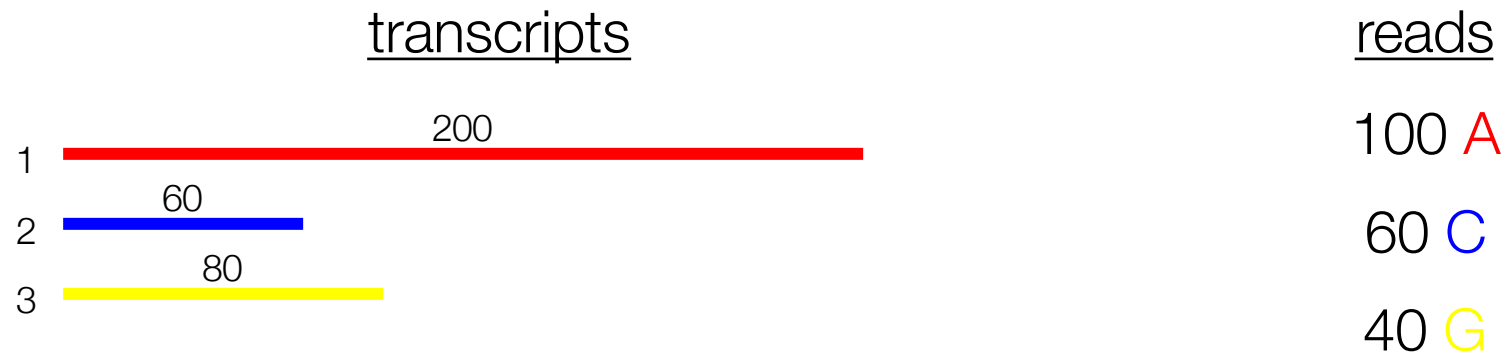
Gene	Sample 1 absolute abundance	Sample 1 relative abundance	Sample 2 absolute abundance	Sample 2 relative abundance
1	20	10%	20	5%
2	20	10%	20	5%
3	20	10%	20	5%
4	20	10%	20	5%
5	20	10%	20	5%
6	100	50%	300	75%

- Changes in absolute expression of high expressors is a major factor
- Normalization is required for comparing samples in these situations

# The basics of quantification with RNA-Seq data

---

- For simplicity, suppose reads are of length **one** (typically they are > 35 bases)



- What relative abundances would you estimate for these genes?
- Relative abundance is relative transcript levels in the cell, not proportion of observed reads

# Length dependence

---

- Probability of a read coming from a transcript  $\propto$  relative abundance  $\times$  length

	<u>transcripts</u>	<u>reads</u>
1	200	100 A
2	60	60 C
3	80	40 G

transcript 1 relative abundance

probability of read from transcript 1 =  
(transcript 1 reads) / (total reads)

$$\hat{f}_1 \propto \frac{\frac{100}{200}}{200} = \frac{1}{400}$$

transcript 1 length

# Length dependence

---

- Probability of a read coming from a transcript  $\propto$  relative abundance  $\times$  length



$$\hat{f}_1 \propto \frac{\frac{100}{200}}{200} = \frac{1}{400}$$

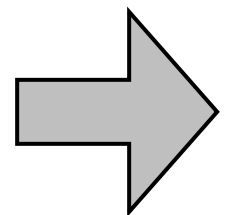
$$\hat{f}_1 = 0.25$$

$$\hat{f}_2 \propto \frac{\frac{60}{200}}{60} = \frac{1}{200}$$

$$\hat{f}_2 = 0.5$$

$$\hat{f}_3 \propto \frac{\frac{40}{200}}{80} = \frac{1}{400}$$

$$\hat{f}_3 = 0.25$$



normalize

# The basics of quantification from RNA-Seq data


---

- Basic assumption:

$$\theta_i = P(\text{read from transcript } i) = Z^{-1} \tau_i \ell'_i$$

expression level  
(relative abundance)

length



- Normalization factor is the mean length of expressed transcripts

$$Z = \sum_i \tau_i \ell'_i$$

# The basics of quantification from RNA-Seq data

---

- Estimate the probability of reads being generated from a given transcript by counting the number of reads that align to that transcript

$$\hat{\theta}_i = \frac{c_i}{N}$$

$\swarrow$  # reads mapping to transcript i  
 $\swarrow$  total # of mappable reads

- Convert to expression levels by normalizing by transcript length

$$\hat{\tau}_i \propto \frac{\hat{\theta}_i}{\ell'_i}$$



# The basics of quantification from RNA-Seq data

---

- Basic quantification algorithm
  - Align reads against a set of reference transcript sequences
  - Count the number of reads aligning to each transcript
  - Convert read counts into relative expression levels

# Counts to expression levels

---

- RPKM - **R**eads **P**er **K**ilobase per **M**illion mapped reads

$$\text{RPKM for gene } i = 10^9 \times \frac{c_i}{\ell'_i N}$$

- TPM - **T**ranscripts **P**er **M**illion

$$(\text{estimate of}) \text{ TPM for isoform } i = 10^6 \times Z \times \frac{c_i}{\ell'_i N}$$

- Prefer TPM to RPKM because of normalization factor
- TPM is a technology-independent measure (simply a fraction)

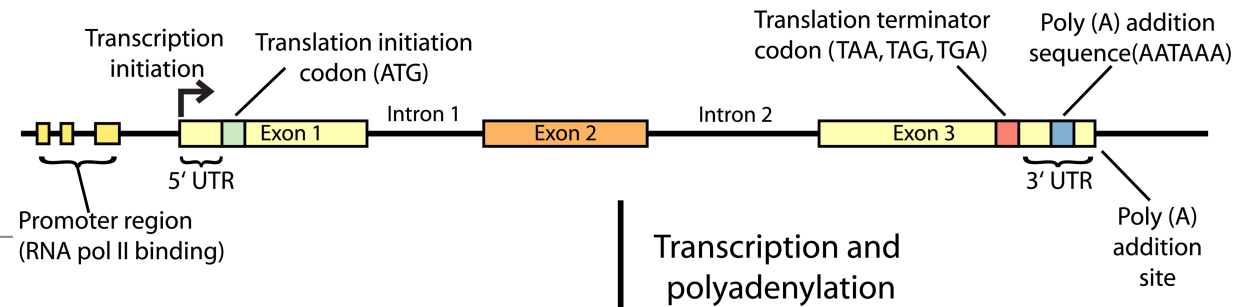
# What if reads do not uniquely map to transcripts?

---

- The approach described assumes that every read can be uniquely aligned to a single transcript
- This is generally not the case
  - Some genes have similar sequences - gene families, repetitive sequences
  - Alternative splice forms of a gene share a significant fraction of sequence

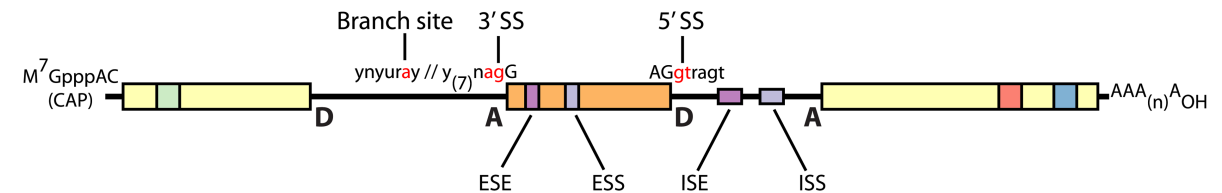
# Central dogma of molecular biology

## Double-stranded genomic DNA template



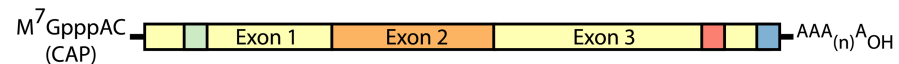
Transcription and polyadenylation

## Single-stranded pre-mRNA (nuclear RNA)



RNA processing

## Mature mRNA

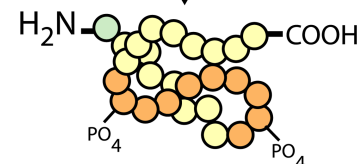


Export to cytoplasm and translation

## Protein (amino acid sequence)

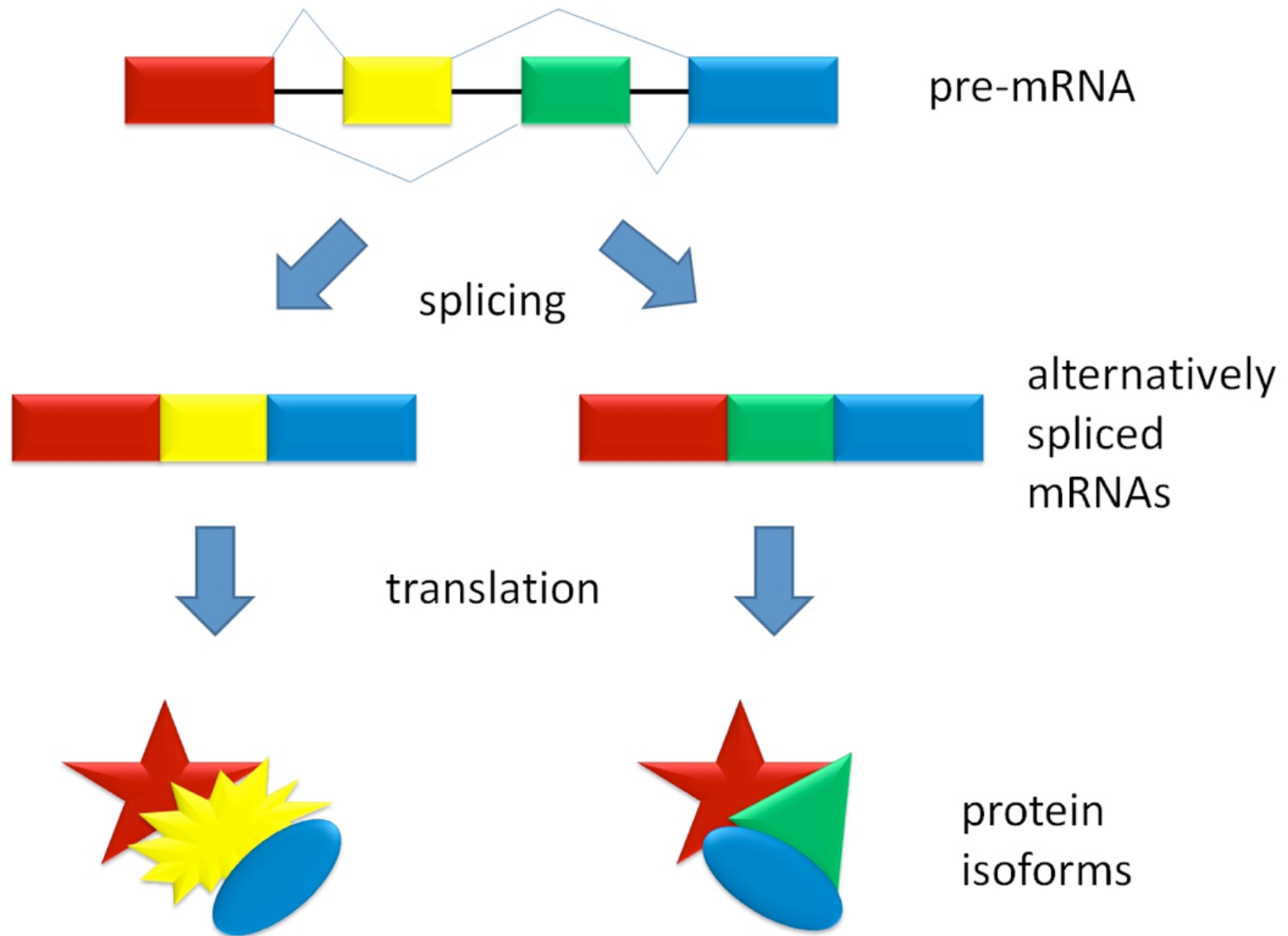


Folding, posttranslational modification, subcellular localization, etc.



# Alternative splicing

---



# Multi-mapping reads in RNA-Seq

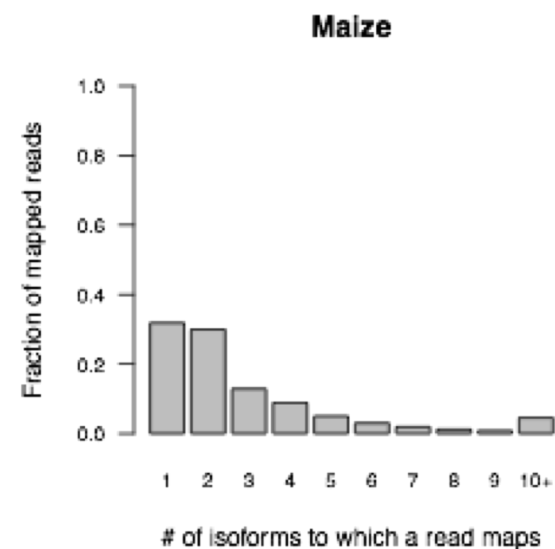
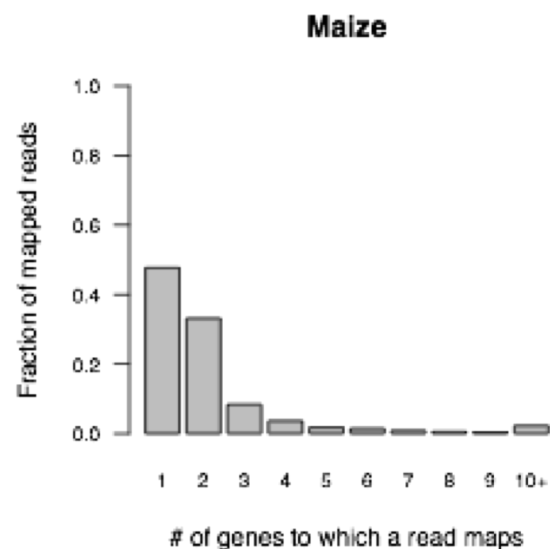
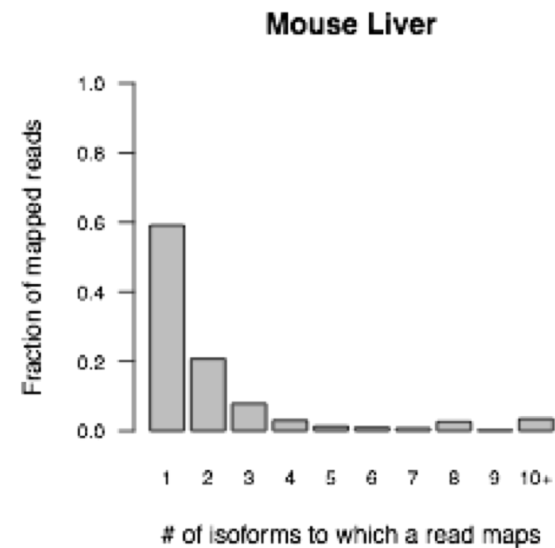
---

Species	Read length	% multi-mapping reads
Mouse	25	17%
Mouse	75	10%
Maize	25	52%
Axolotl	76	23%
Human	50	23%

- Throwing away multi-mapping reads leads to
  1. Loss of information
  2. Potentially biased estimates of abundance

# Distributions of alignment counts

---



# What if reads do not uniquely map to transcripts?

---

- Multiread: a read that could have been derived from multiple transcripts



- How would you estimate the relative abundances for these transcripts?



# Some options for handling multireads

---

- Discard multireads, estimate based on uniquely mapping reads only
- Discard multireads, but use “unique length” of each transcript in calculations
- “Rescue” multireads by allocating (fractions of) them to the transcripts
  - Three step algorithm
    1. Estimate abundances based on uniquely mapping reads only
    2. For each multiread, divide it between the transcripts to which it maps, proportionally to their abundances estimated in the first step
    3. Recompute abundances based on updated counts for each transcript

# Rescue method example - Step 1

---



Step 1

$$\hat{f}_1^{unique} = \frac{\frac{90}{200}}{\frac{90}{200} + \frac{40}{60} + \frac{40}{80}} = 0.278$$

$$\hat{f}_2^{unique} = 0.412$$

$$\hat{f}_3^{unique} = 0.309$$

## Rescue method example - Step 2

---



Step 2

$$c_1^{rescue} = 90 + 30 \times \frac{0.278}{0.278 + 0.412} = 102.1$$

$$c_2^{rescue} = 40 + 30 \times \frac{0.412}{0.278 + 0.412} = 57.9$$

$$c_3^{rescue} = 40 + 0 = 40$$

# Rescue method example - Step 3

---



Step 3

$$\hat{f}_1^{rescue} = \frac{\frac{102.1}{200}}{\frac{102.1}{200} + \frac{57.9}{60} + \frac{40}{80}} = 0.258$$

$$\hat{f}_2^{rescue} = \frac{\frac{57.9}{60}}{\frac{102.1}{200} + \frac{57.9}{60} + \frac{40}{80}} = 0.488$$

$$\hat{f}_3^{rescue} = \frac{\frac{40}{80}}{\frac{102.1}{200} + \frac{57.9}{60} + \frac{40}{80}} = 0.253$$

# An observation about the rescue method

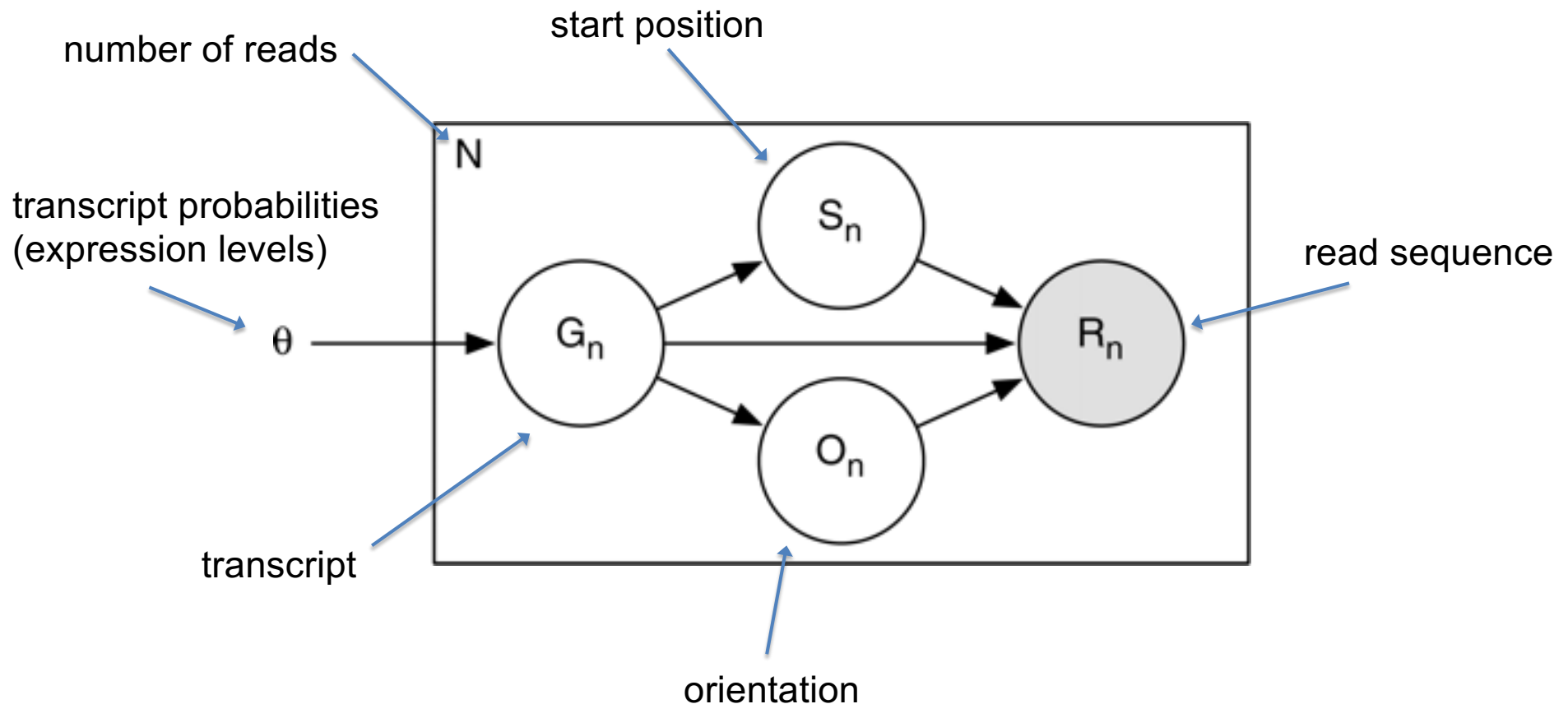
---

- Note that at the end of the rescue algorithm, we have an updated set of abundance estimates
- These new estimates could be used to reallocate the multireads
- And then we could update our abundance estimates once again
- And repeat!
- This is the intuition behind the statistical approach to this problem

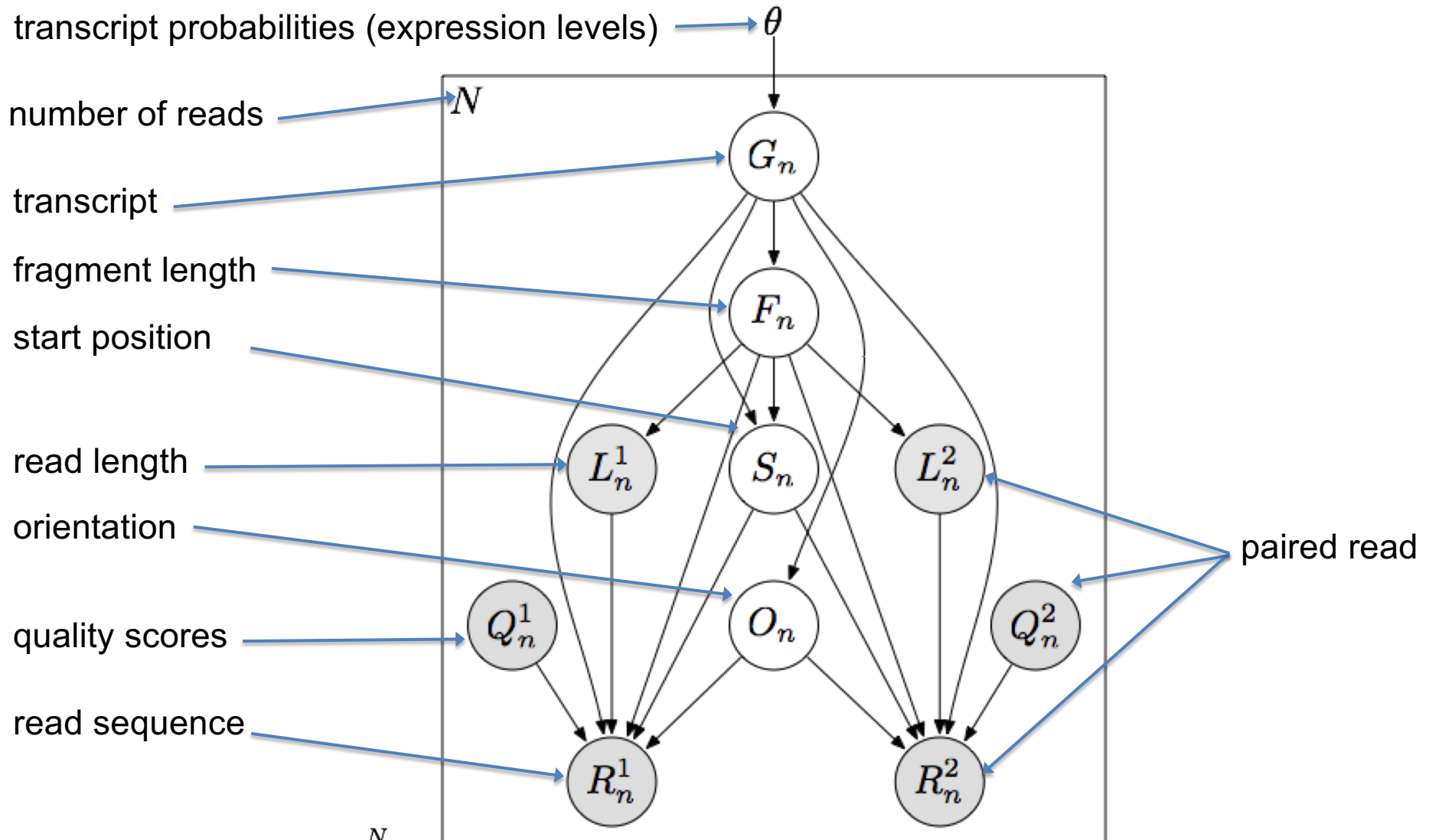
# RSEM (RNA-Seq by Expectation-Maximization) - a generative probabilistic model

---

- Simplified view of the model (plate notation)
  - Grey – observed variable
  - White – latent (unobserved) variables



# RSEM - a generative probabilistic model



$$P(\mathbf{g}, \mathbf{f}, \mathbf{s}, \mathbf{o}, \mathbf{\ell}, \mathbf{q}, \mathbf{r} | \theta) = \prod_{n=1}^N P(g_n | \theta) P(f_n | g_n) P(s_n | f_n, g_n) P(o_n | g_n) P(q_n) P(\ell_n | f_n) P(r_n | g_n, f_n, s_n, o_n, \ell_n, q_n)$$

# Quantification as maximum likelihood inference

---

- Observed data likelihood

$$P(\mathbf{r}, \ell, \mathbf{q} | \theta) = \prod_{n=1}^N \sum_{i=0}^M \theta_i \sum_{j=0}^{L_i} \sum_{k=0}^{L_i} \sum_{o=0}^1 P(R_n = r_n, L_n = \ell_n, Q_n = q_n, S_n = j, F_n = k, O_n = o | G_n = i)$$

- Likelihood function is concave with respect to  $\theta$ 
  - Has a global maximum (or global maxima)
- Expectation-Maximization for optimization

*“RNA-Seq gene expression estimation with read mapping uncertainty”*

Li, B., Ruotti, V., Stewart, R., Thomson, J., Dewey, C.

Bioinformatics, 2010



# Approximate inference with read alignments

---

$$P(\mathbf{r}, \ell, \mathbf{q} | \theta) = \prod_{n=1}^N \sum_{i=0}^M \theta_i \sum_{j=0}^{L_i} \sum_{k=0}^{L_i} \sum_{o=0}^1 P(R_n = r_n, L_n = \ell_n, Q_n = q_n, S_n = j, F_n = k, O_n = o | G_n = i)$$

- Full likelihood computation requires  $O(NML^2)$  time

- N (number of reads)  $\sim 10^7$

- M (number of transcripts)  $\sim 10^4$

- L (average transcript length)  $\sim 10^3$

- Approximate by alignment

$$P(\mathbf{r}, \ell, \mathbf{q} | \theta) = \prod_{n=1}^N \sum_{(i,j,k,o) \in \pi_n^x} \theta_i P(R_n = r_n, L_n = \ell_n, Q_n = q_n, Z_{nijko} = 1 | G_n = i)$$



all local alignments of read n with at most x mismatches

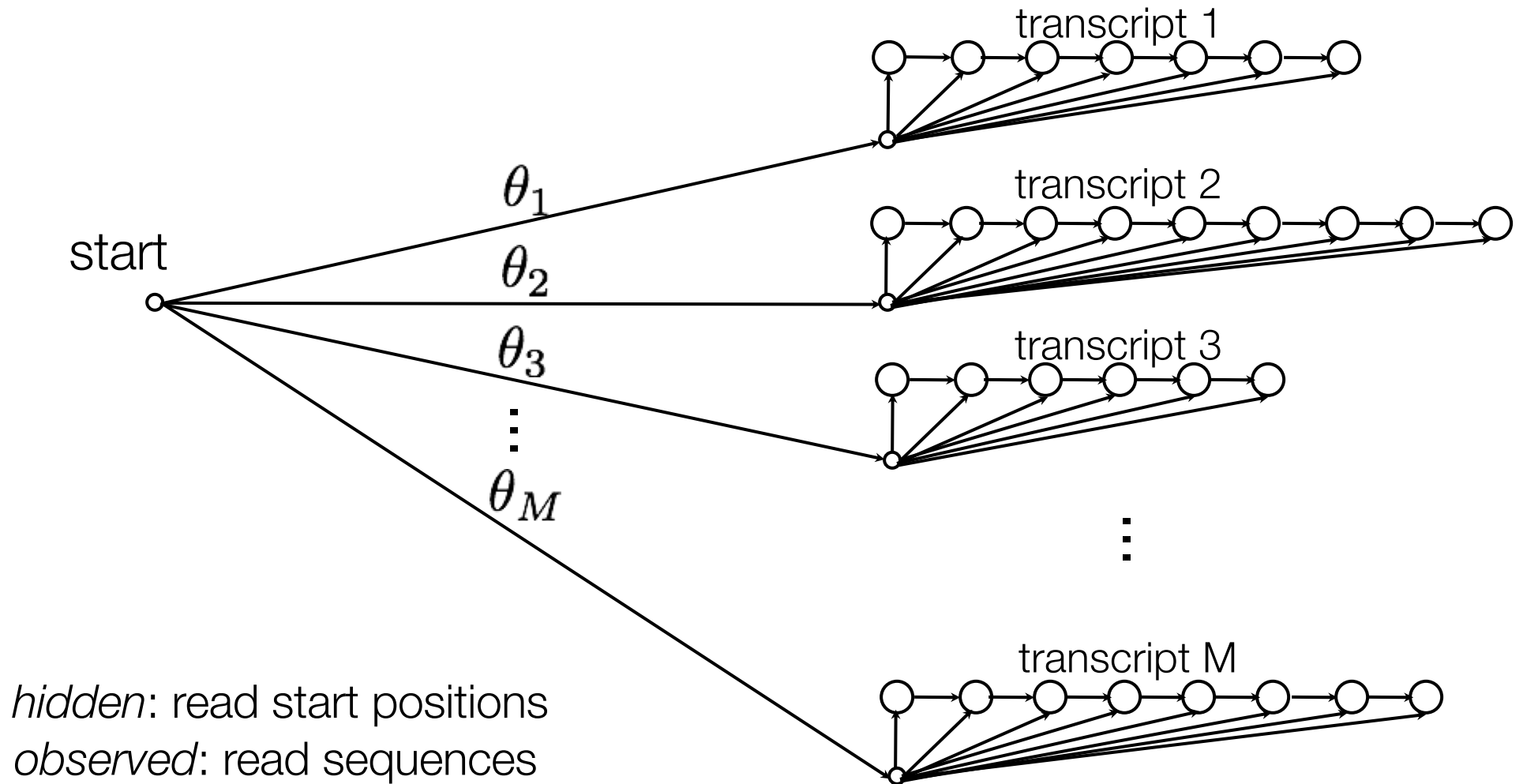
# EM Algorithm

---

- Expectation-Maximization for RNA-Seq
  - E-step: Compute expected read counts given current expression levels
  - M-step: Compute expression values maximizing likelihood given expected read counts
- Rescue algorithm  $\approx$  1 iteration of EM

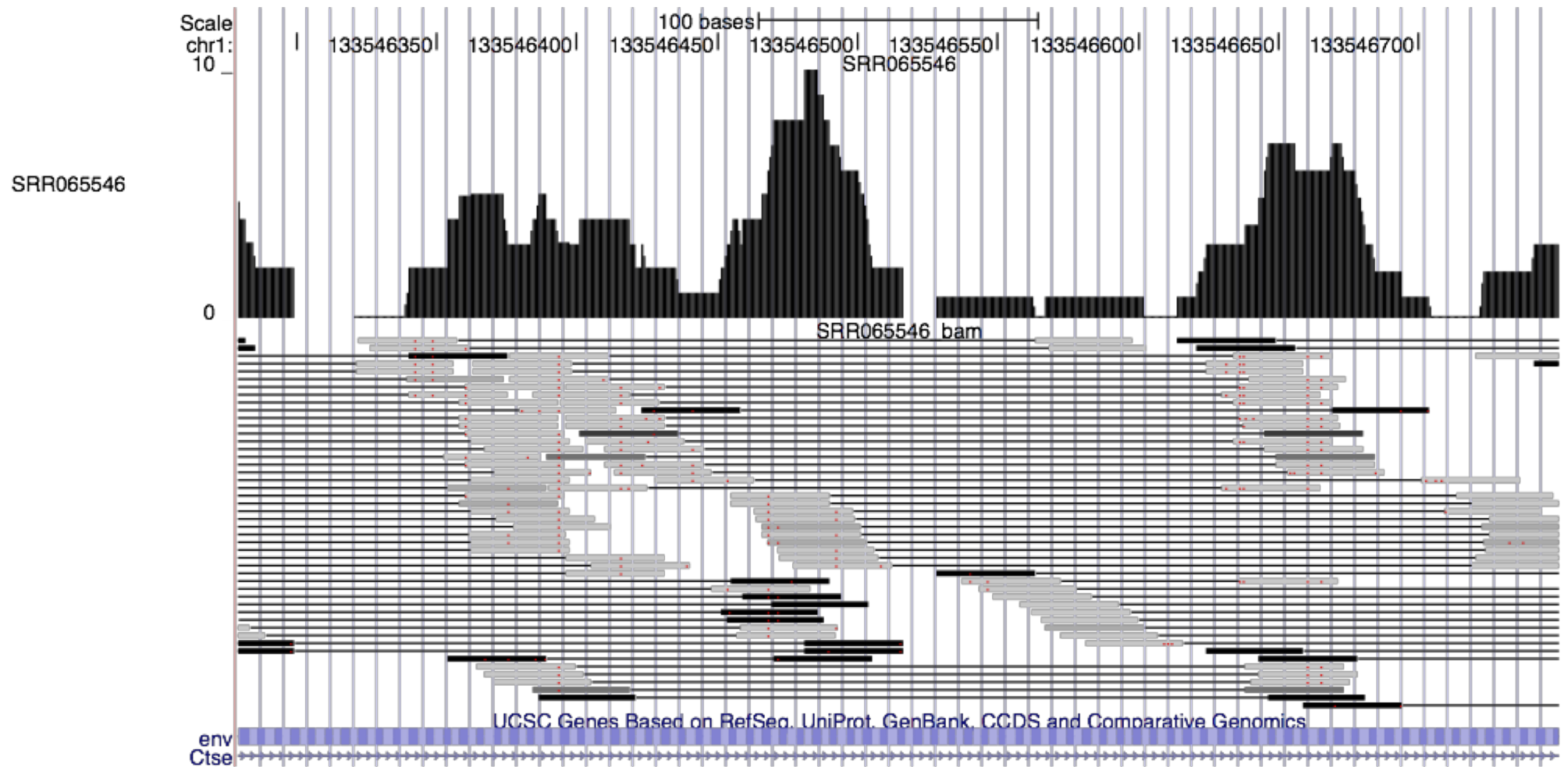
# HMM Interpretation

---

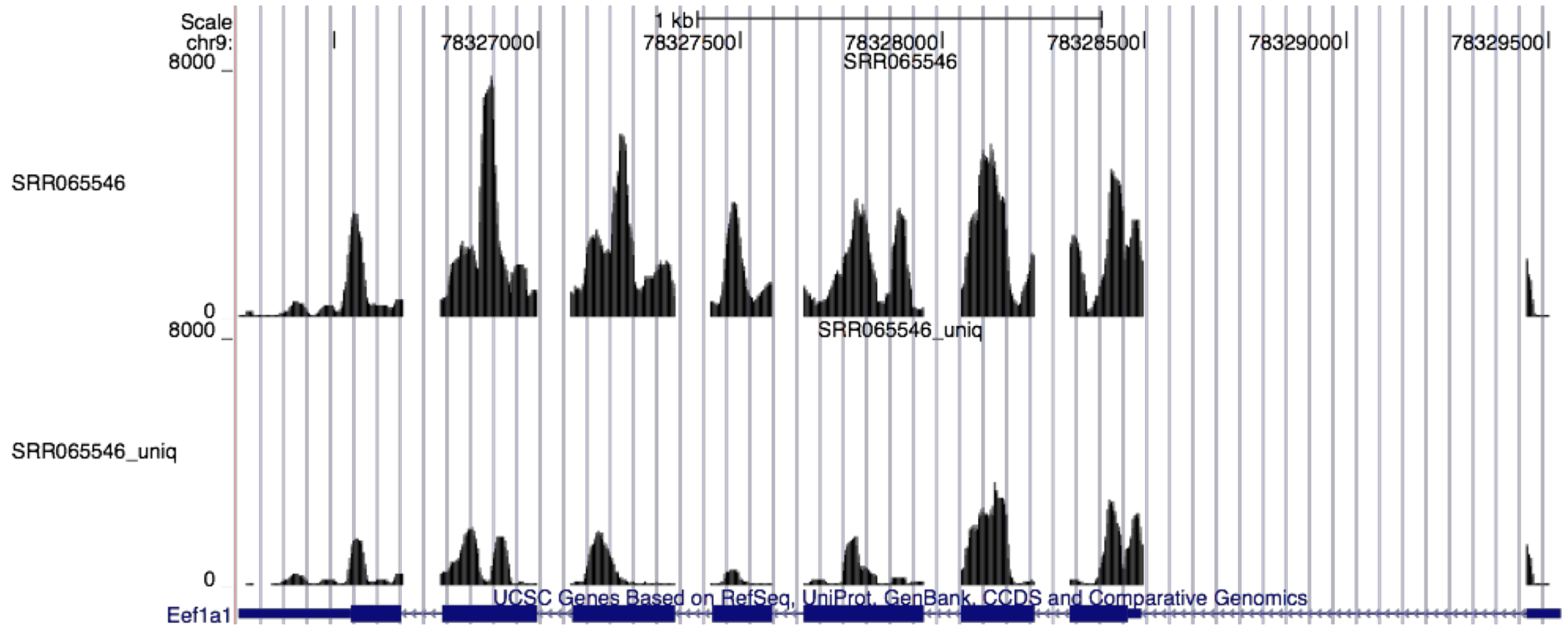


Learning parameters: Baum-Welch Algorithm (EM for HMMs)  
Approximation: Only consider a subset of paths for each read

# Probabilistically-weighted alignments

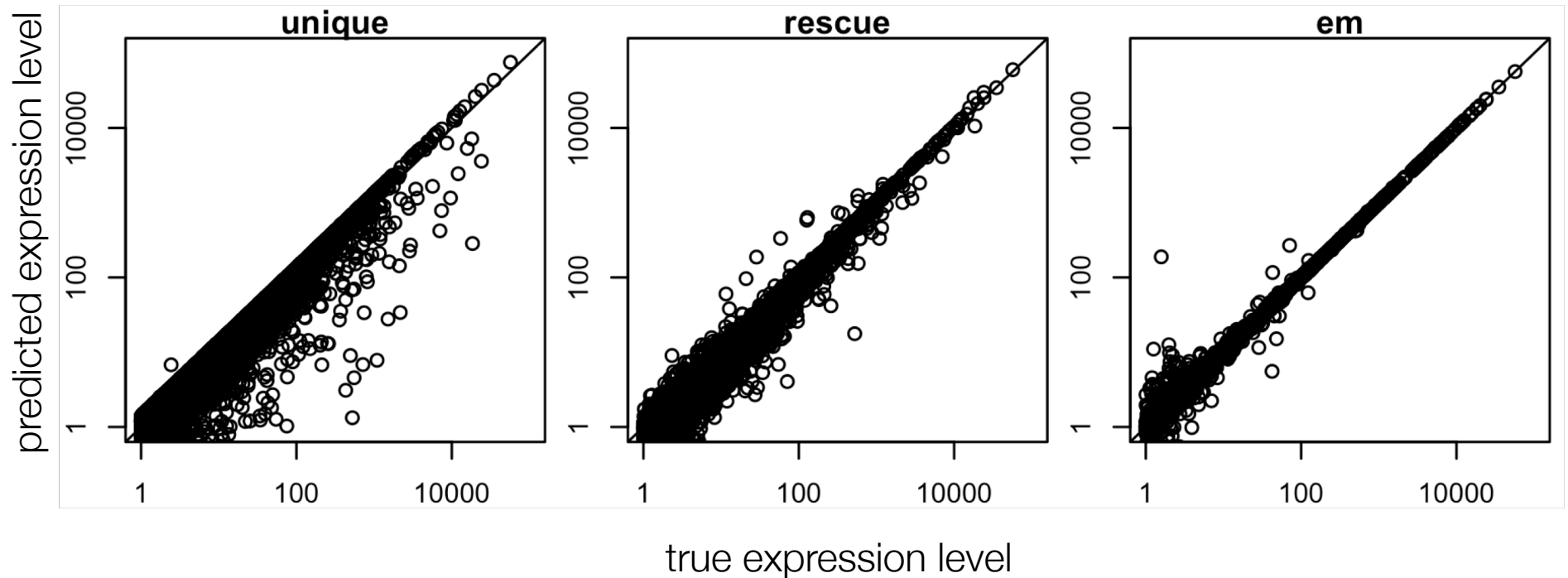


# Expected read count visualization



# Improved accuracy over unique and rescue

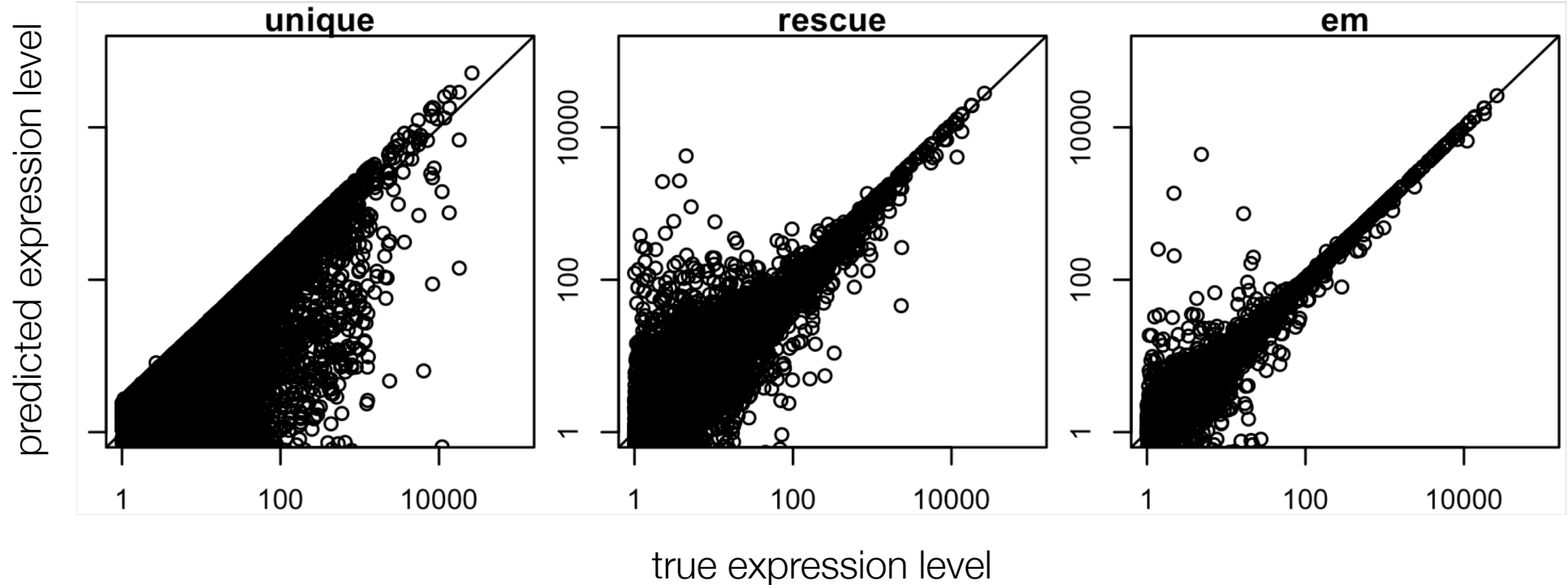
---



Mouse gene-level expression estimation

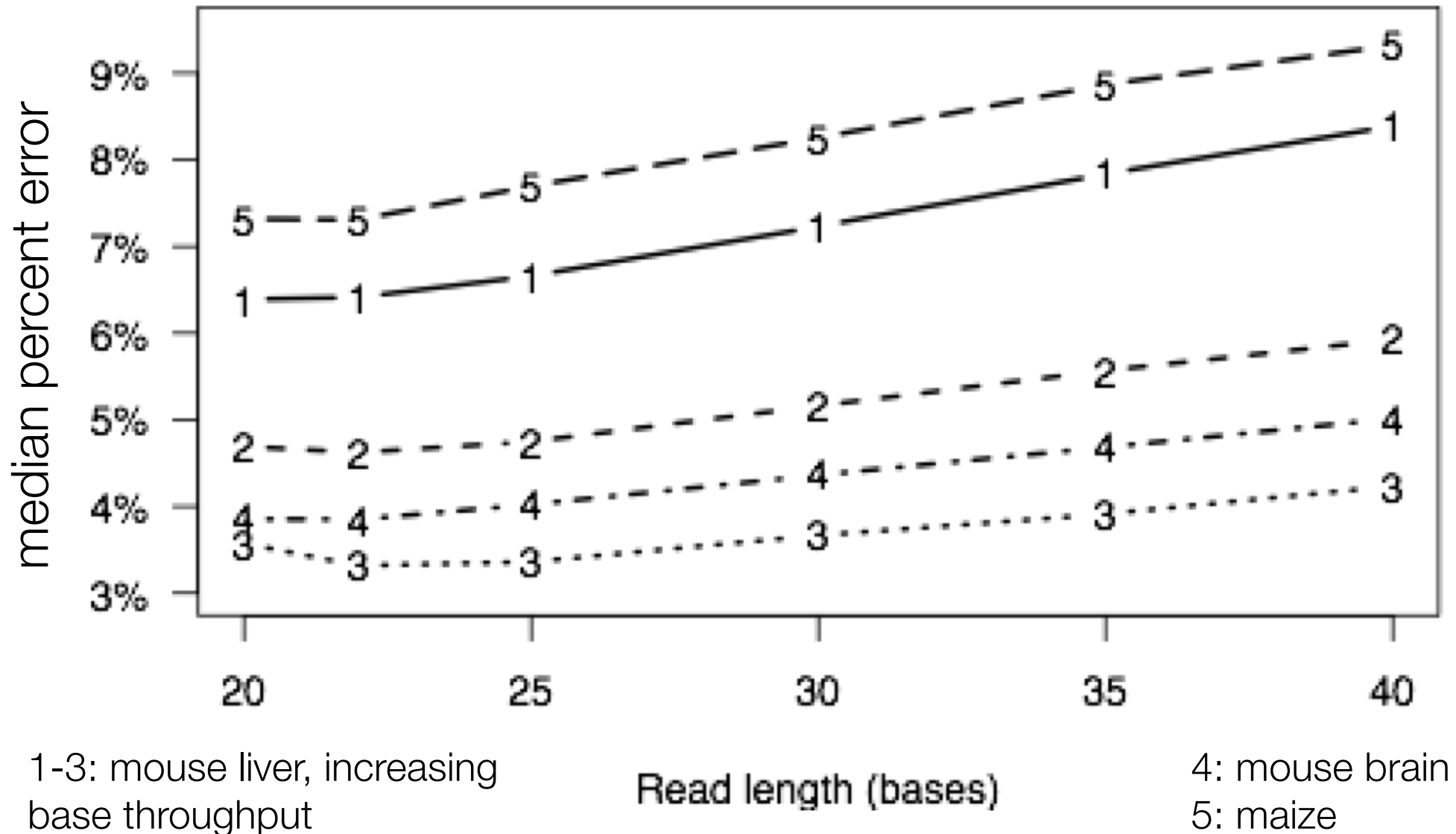
# Improving accuracy on repetitive genomes: maize

---



Maize gene-level expression estimation

# Finding the optimal read length





# RNA-Seq and RSEM summary

---

- RNA-Seq is the preferred technology for transcriptome analysis in most settings
- The major challenge in analyzing RNA-Seq data: the reads are much shorter than the transcripts from which they are derived
- Tasks with RNA-Seq data thus require handling hidden information: which gene/isoform gave rise to a given read
- The Expectation-Maximization algorithm is extremely powerful in these situations

# Recent developments in RNA-Seq

---

- Long read sequences: PacBio and Oxford Nanopore
- Single-cell RNA-Seq: [review](#)
  - Observe heterogeneity of cell populations
  - Model technical artifacts (e.g. artificial 0 counts)
  - Detect sub-populations
  - Predict pseudotime through dynamic processes
  - Detect gene-gene and cell-cell relationships
- [Alignment-free quantification](#):
  - [Kallisto](#)
  - [Salmon](#)

# Public sources of RNA-Seq data

---

- Gene Expression Omnibus (GEO): <http://www.ncbi.nlm.nih.gov/geo/>
  - Both microarray and sequencing data
- Sequence Read Archive (SRA): <http://www.ncbi.nlm.nih.gov/sra>
  - All sequencing data (not necessarily RNA-Seq)
- ArrayExpress: <https://www.ebi.ac.uk/arrayexpress/>
  - European version of GEO
- Homogenized data: [MetaSRA](#), [Toil](#), [recount2](#), [ARCHS4](#)